

# **Kapitel 13: Prozessmodellierung und Workflow-Management**

## **13.1 Prozessmodellierung**

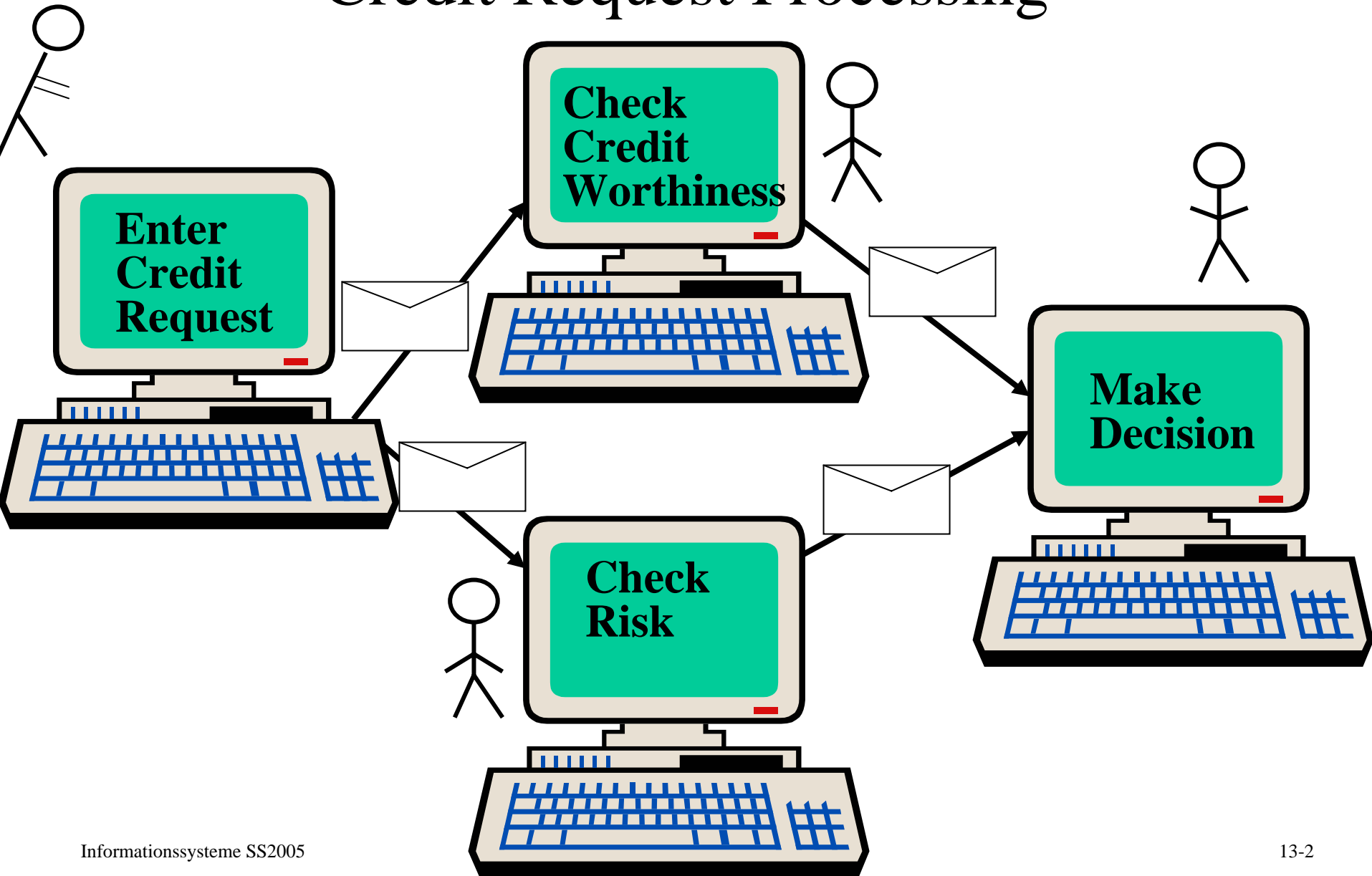
- **Statecharts**
- **Ereignis-Prozess-Ketten**

## **13.2 Workflow-Management für Geschäftsprozesse**

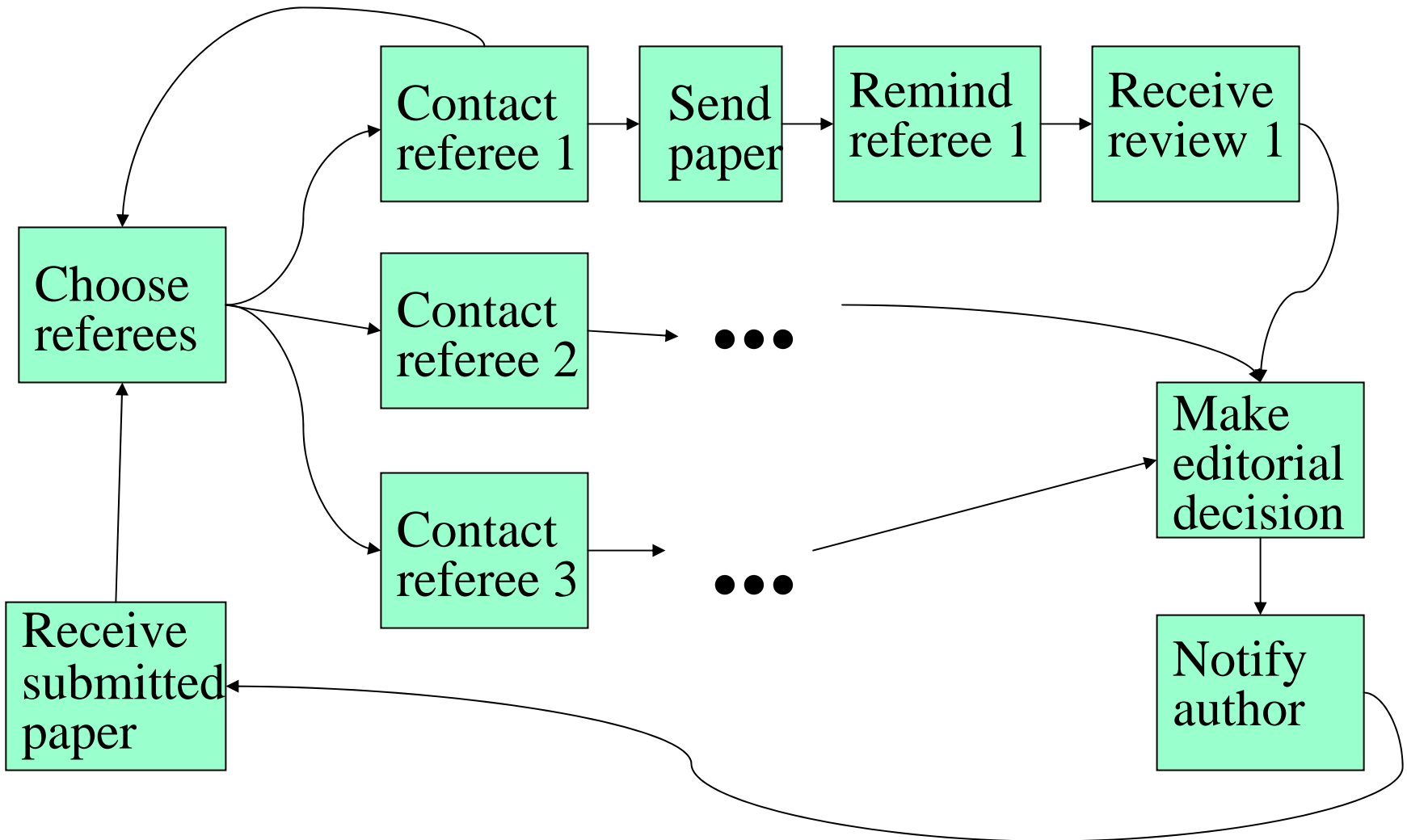
## **13.3 Semantik von Statecharts**

## **13.4 Eigenschaften von Statecharts und deren Verifikation**

# Workflow Application Example 1: Credit Request Processing



# Workflow Application Example 2: Journal Refereeing Process



# What is Workflow Management?

*Computer-supported business processes:  
coordination of control and data flow between  
distributed - automated or intellectual - activities*

## **Application examples:**

- ★ Credit requests, insurance claims, etc.
- ★ Tax declaration, real estate purchase, etc.
- ★ Student exams, journal refereeing, etc.
- ★ Electronic commerce, virtual enterprises, etc.

# Business Benefits of Workflow Technology



Business process automation  
(to the extent possible and reasonable)

- ➡ shorter turnaround time, less errors, higher customer satisfaction
- ➡ better use of intellectual resources for exceptional cases



Transparency

- ➡ understanding & analyzing the enterprise



Fast & easy adaptation

- ➡ Business Process Reengineering (BPR)

# 13.1 Specification Method and Environment

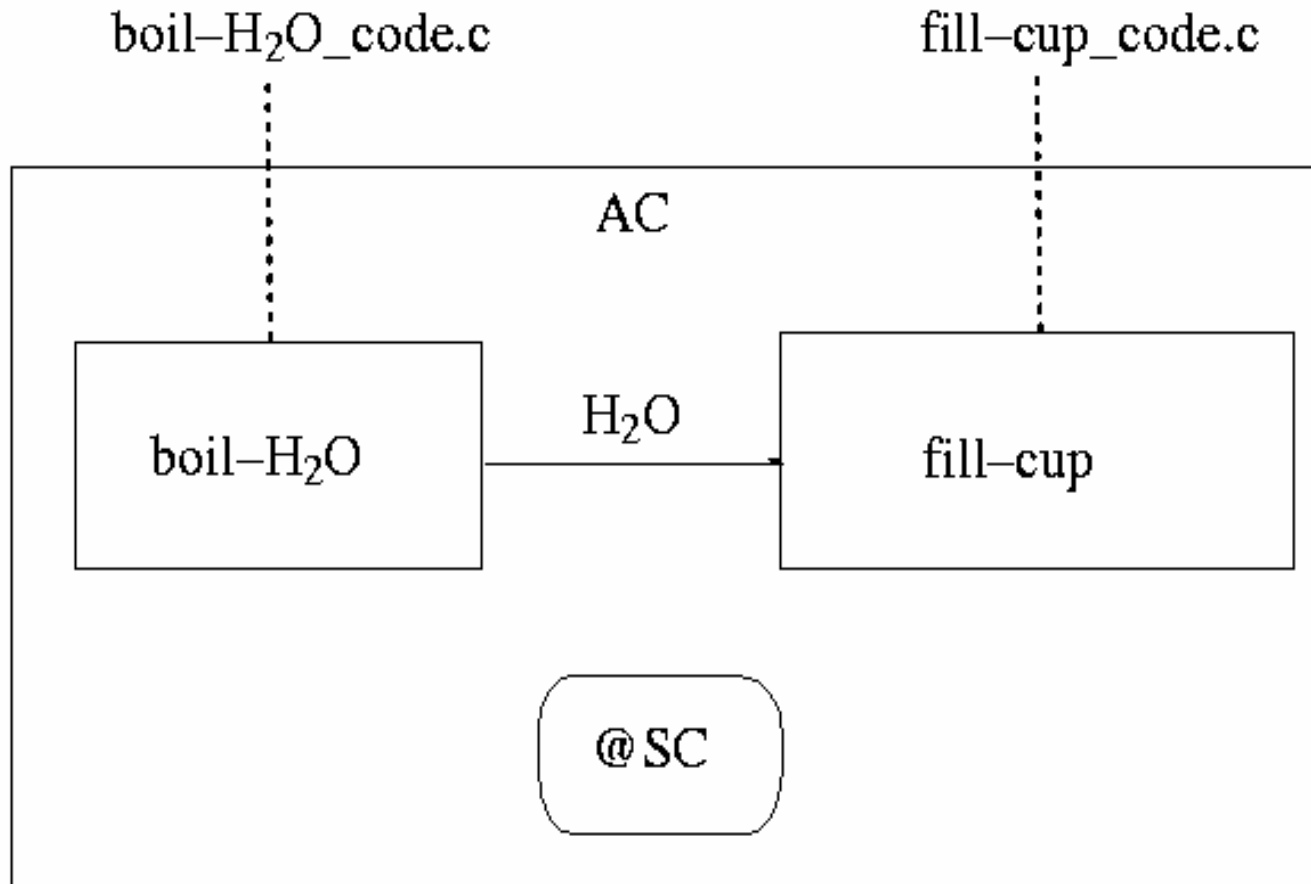
## *Requirements:*

- Visualization
- Refinement & Composability
- Rigorous Semantics
- Interoperability with other methods & tools
- Wide acceptance & standard compliance

## *Solutions:*

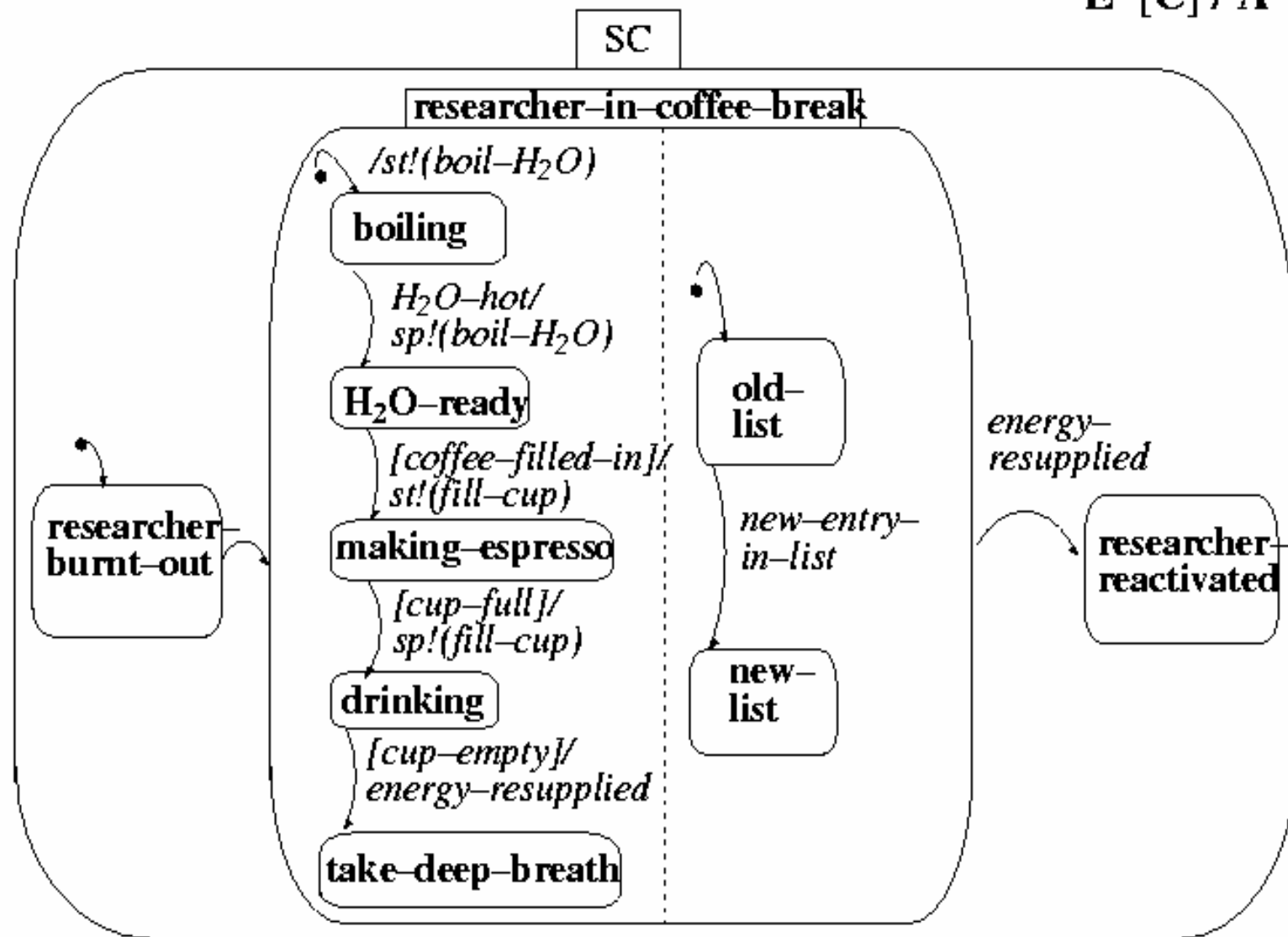
- ➡ *Statecharts* (Harel et al. 1987)  
(alt.: Petri Net variants, temporal logic, process algebra, script language)
- ➡ Import / export  
BPR tools → WFMS ↔ WFMS
- ➡ Statecharts included in UML industry standard (Unified Modeling Language, OMG 1997))

# Example of Activitychart



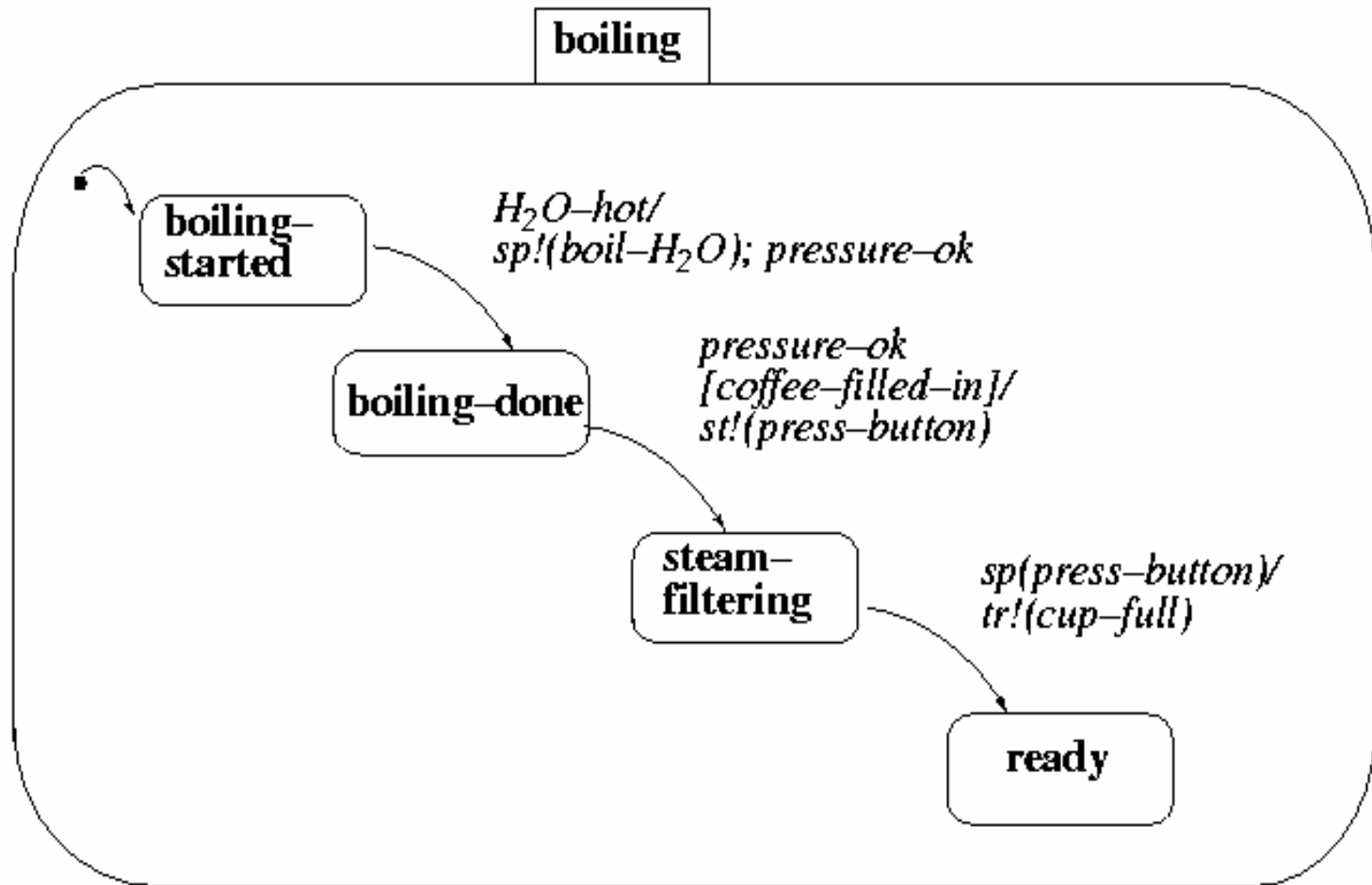
# Example of Statechart

E [C] / A

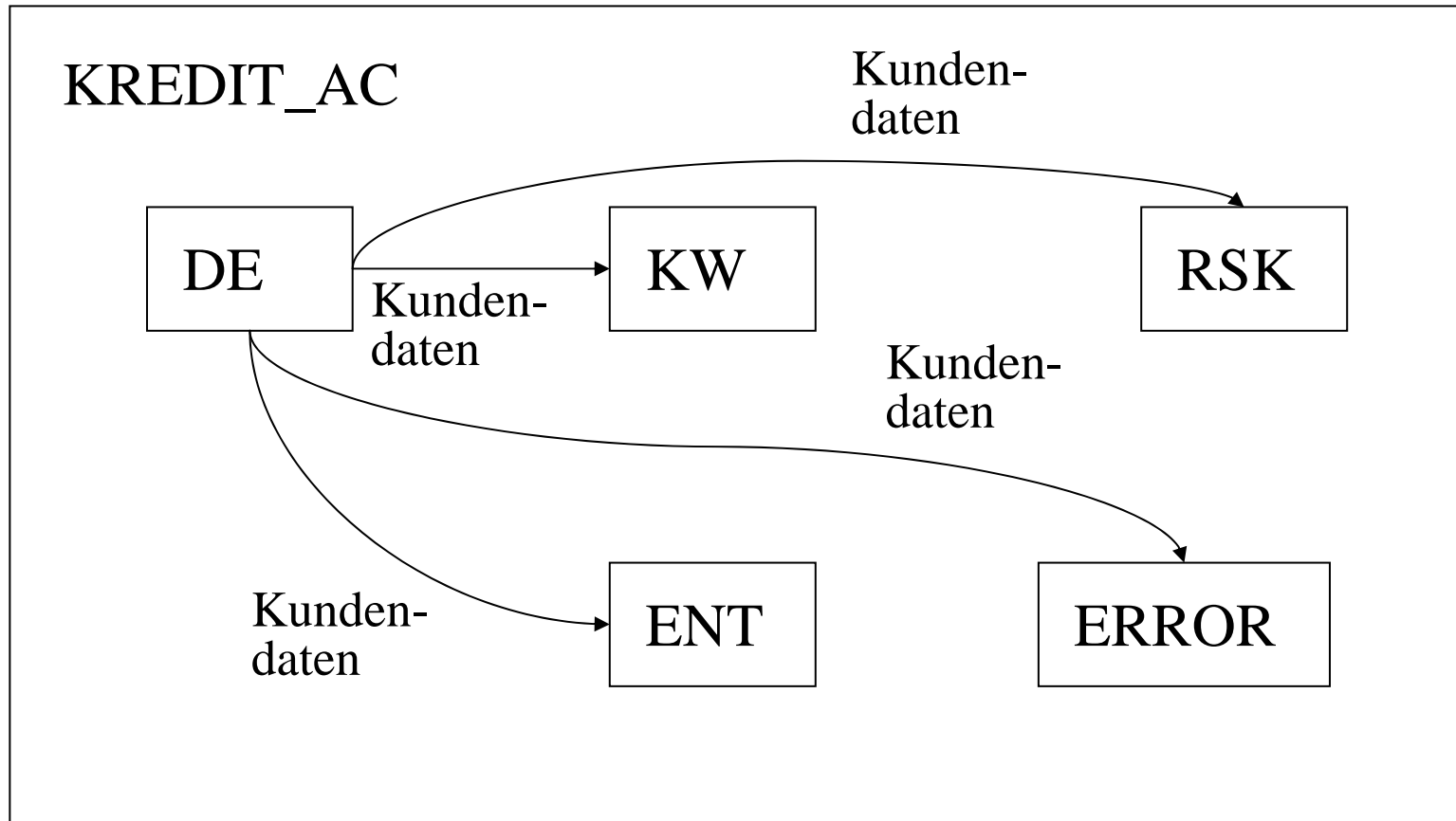




# Refinement of States

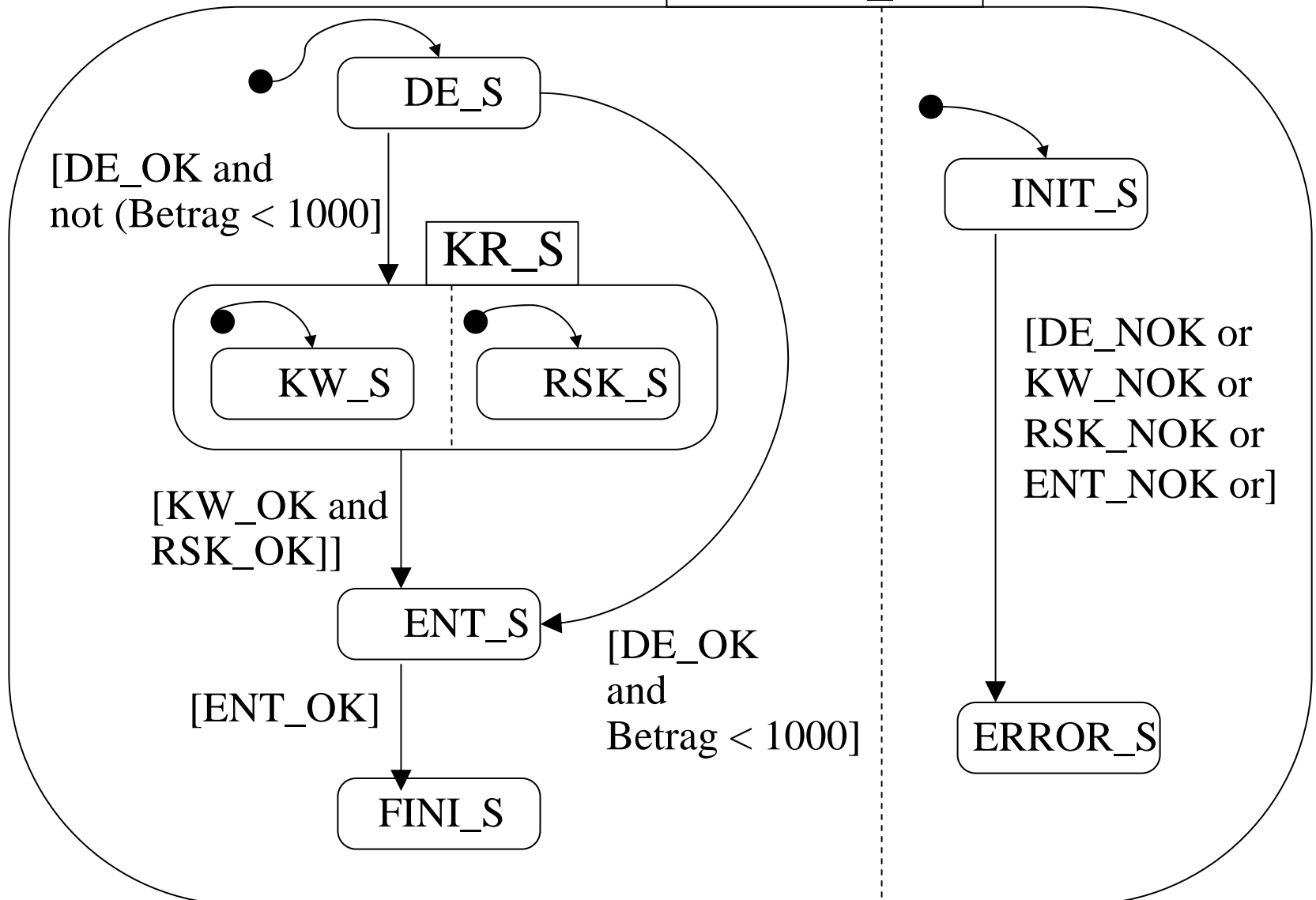


# Activitychart Example 1

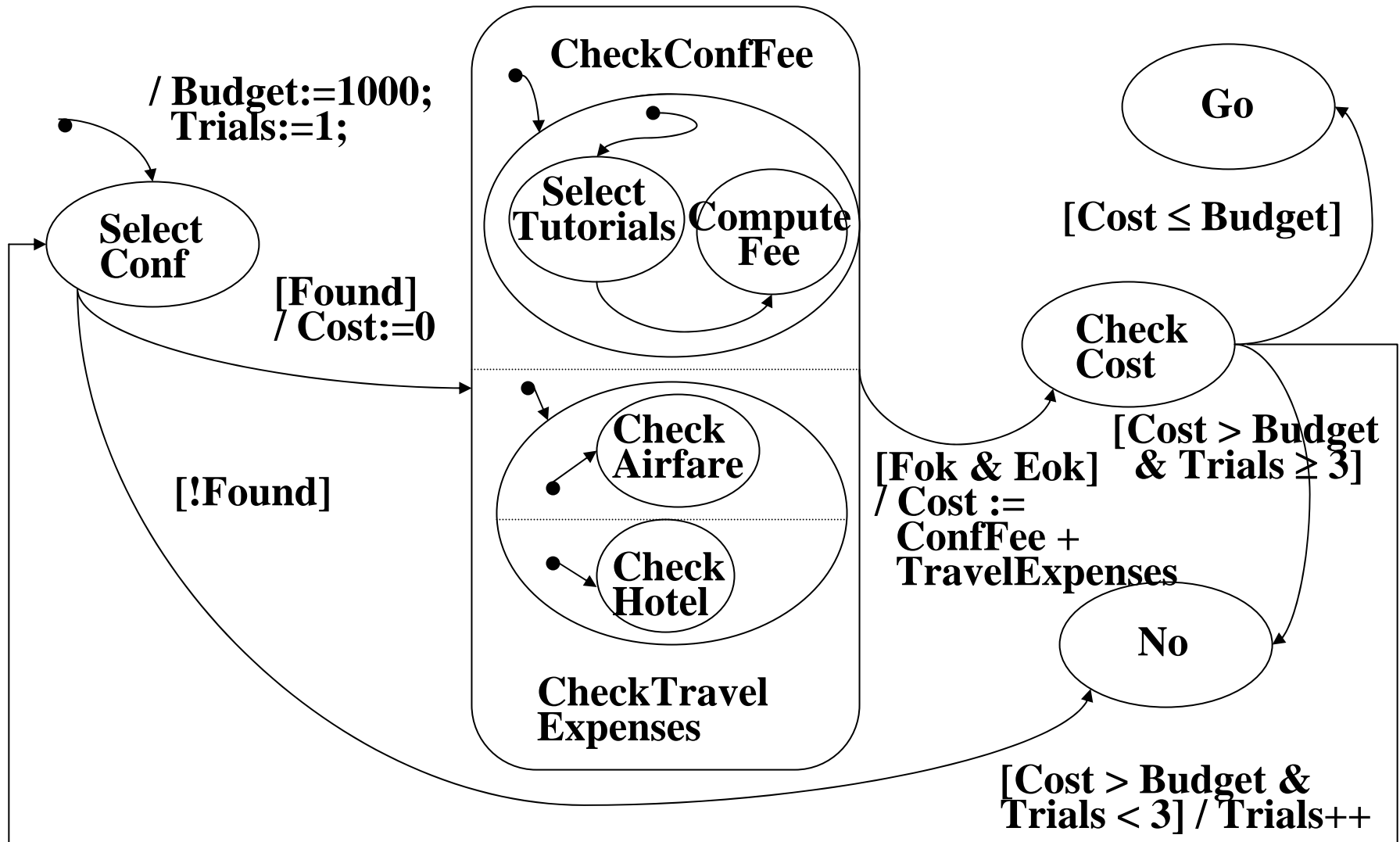


# Statechart Example 1

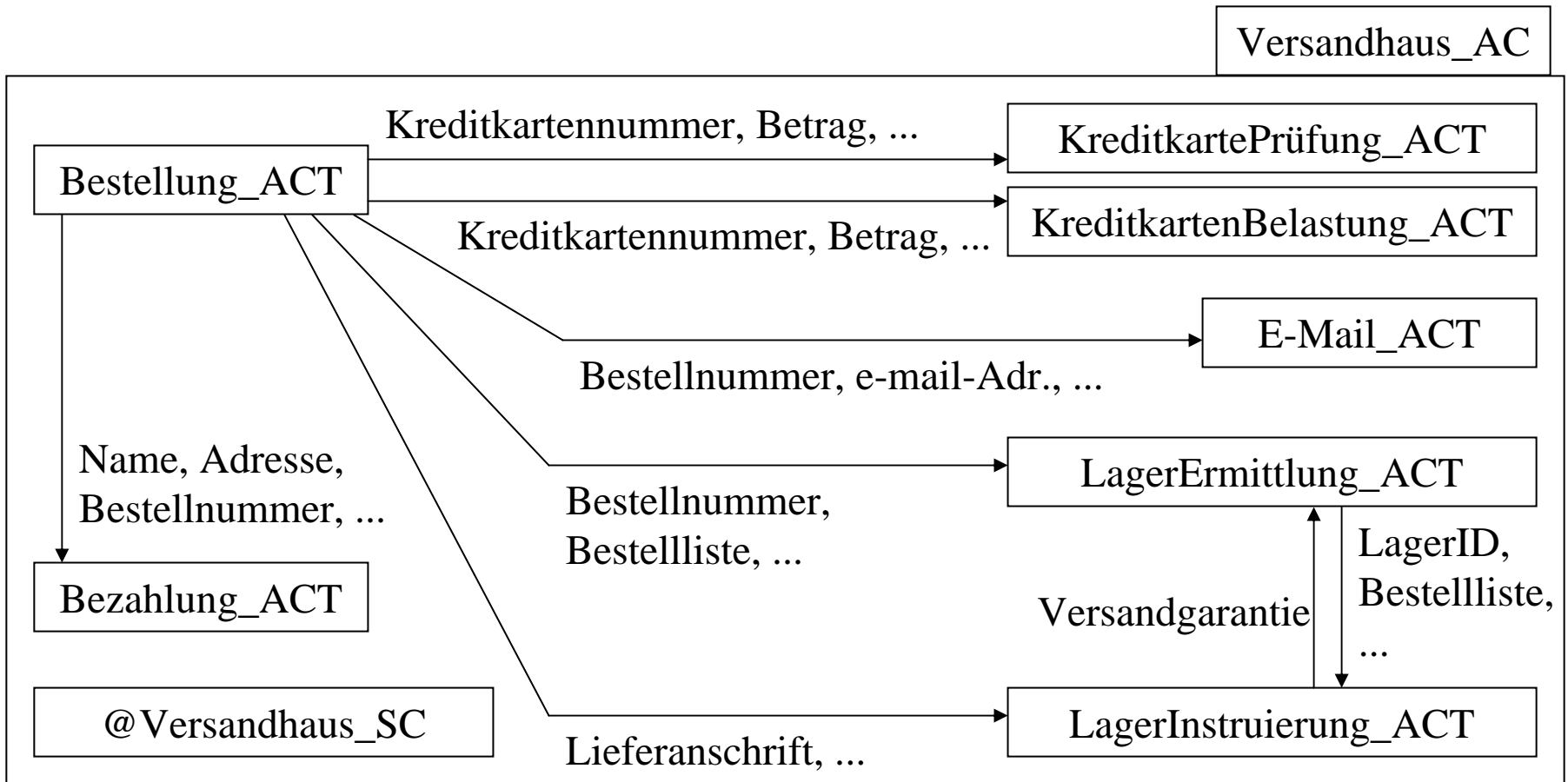
KREDIT\_SC



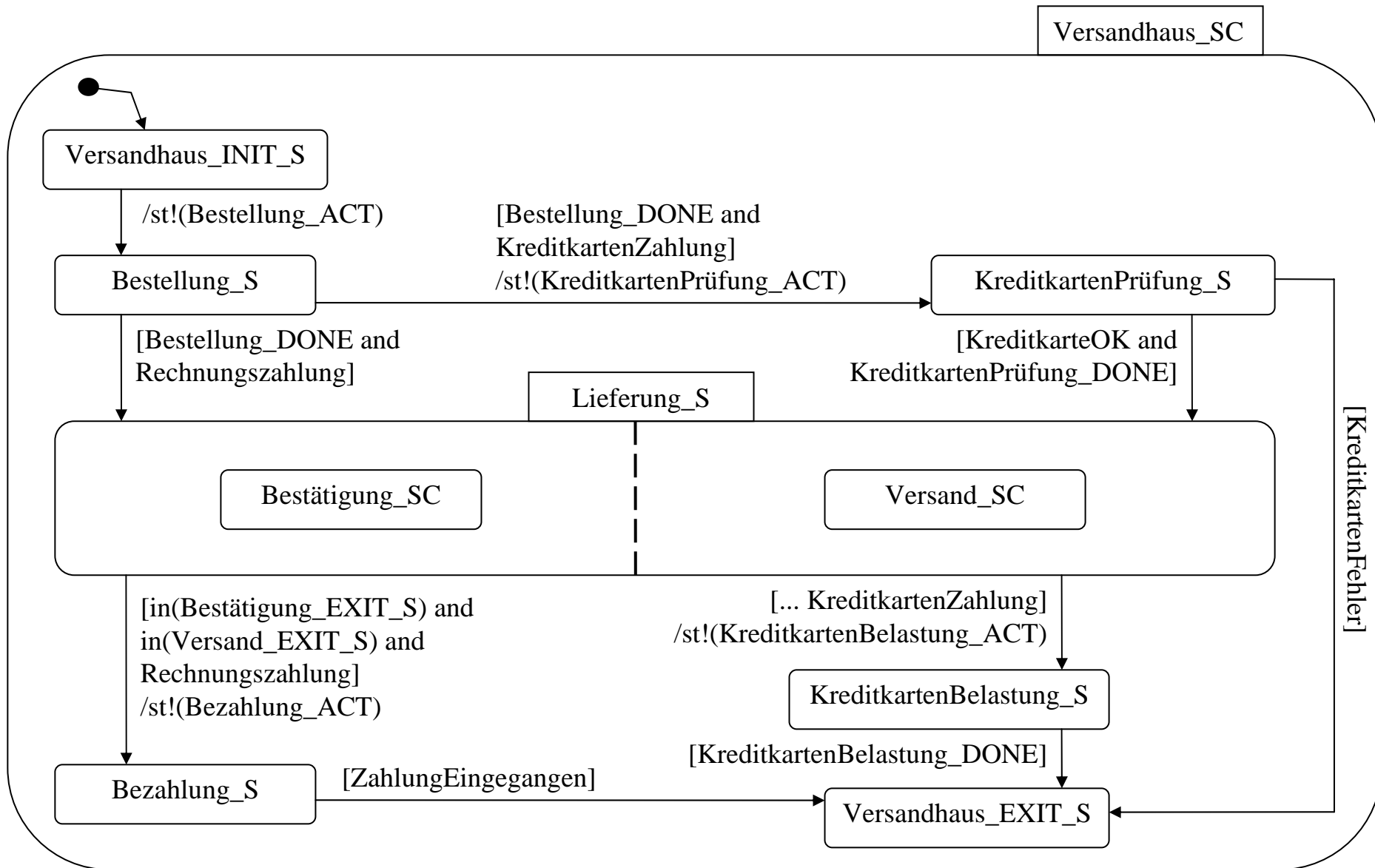
# Statechart Example 2



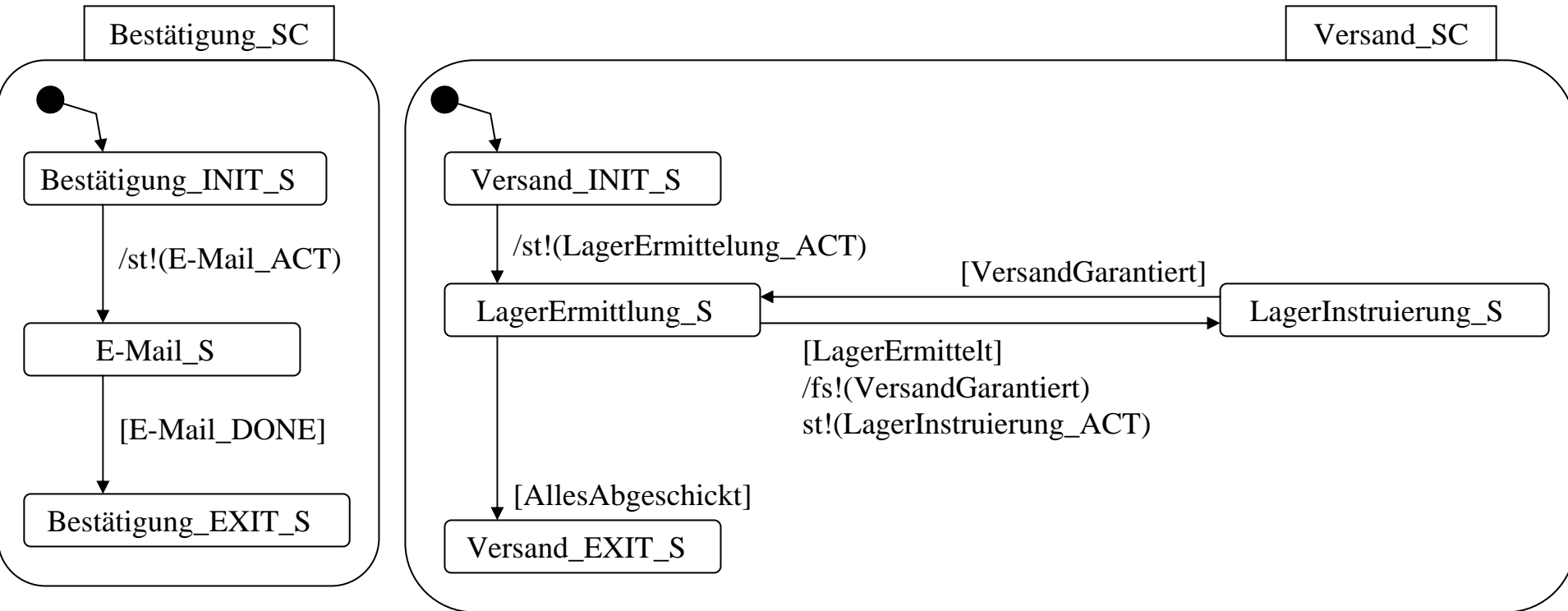
# E-Commerce Workflow: Activitychart



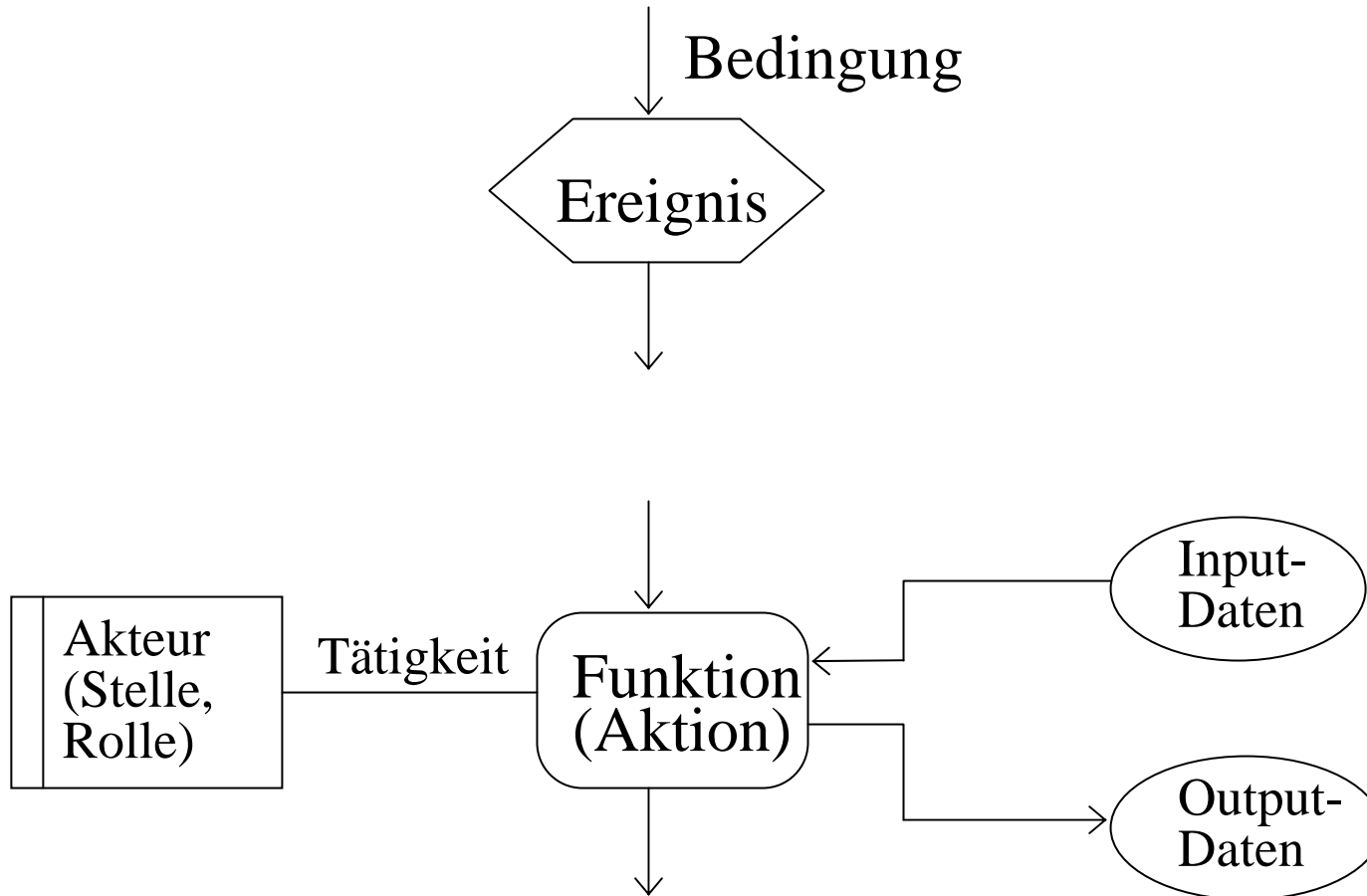
# E-Commerce Workflow: Statechart



# E-Commerce Sub-Workflows

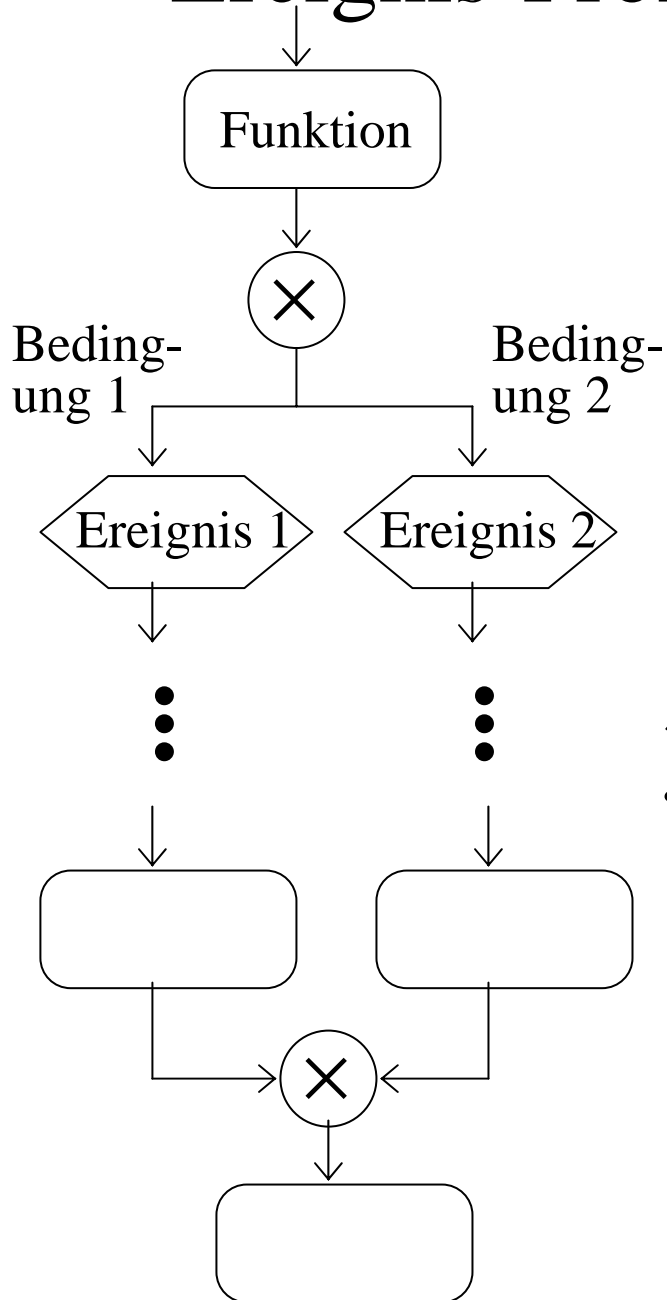


# Ereignis-Prozeß-Ketten (EPKs) (1)

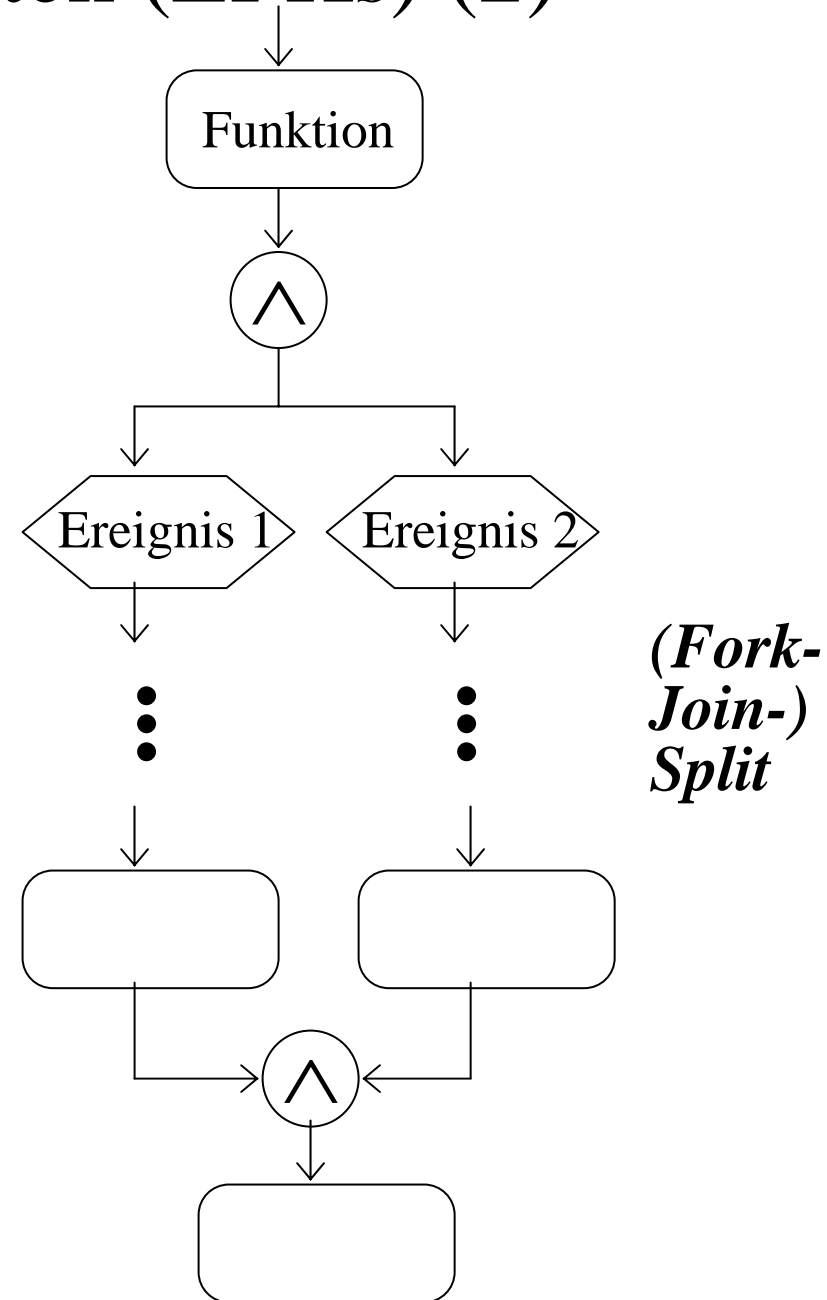




# Ereignis-Prozeß-Ketten (EPKs) (2)

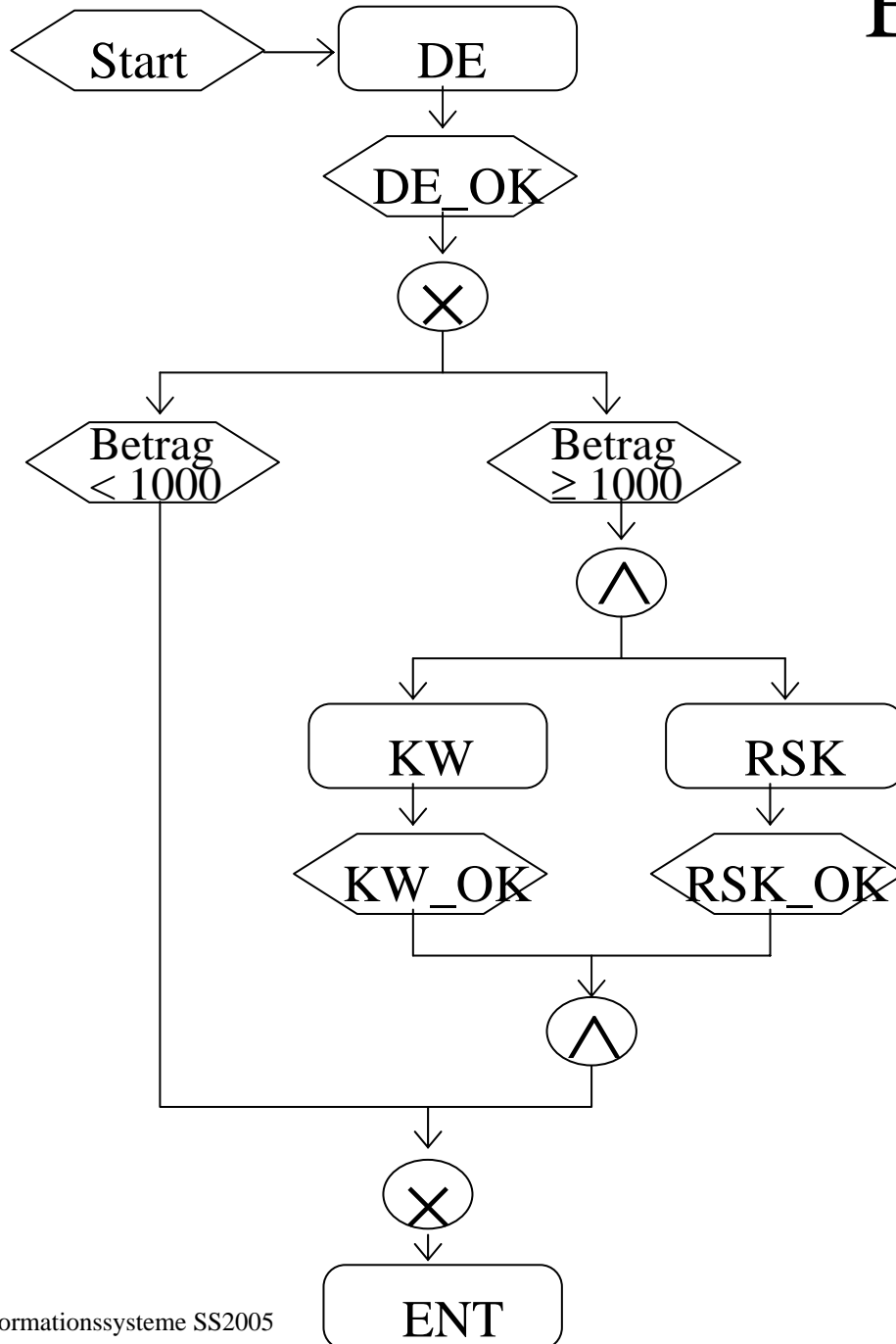


*Verzweigung*



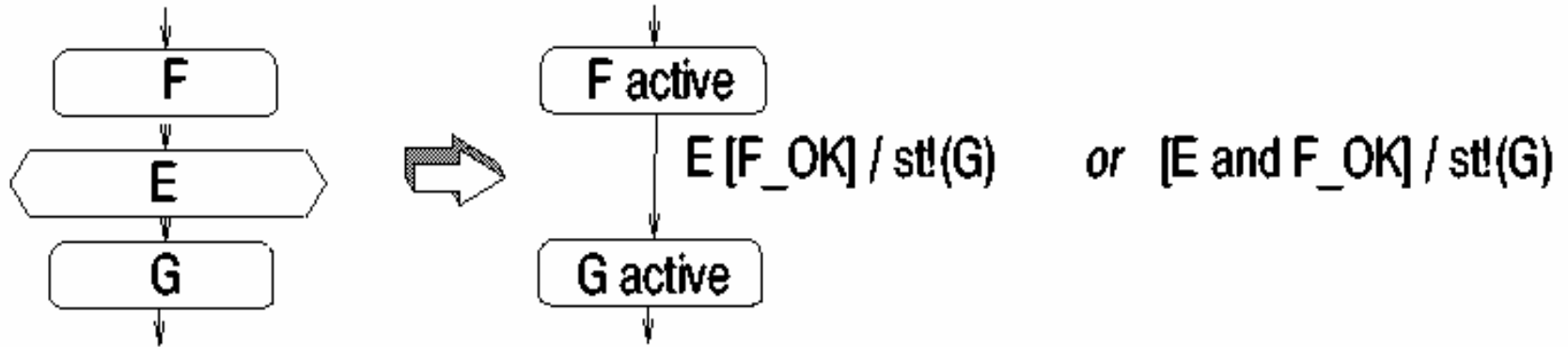
*(Fork-Join-) Split*

# EPK-Beispiel



# Import from BPR Tools

*Principle:*



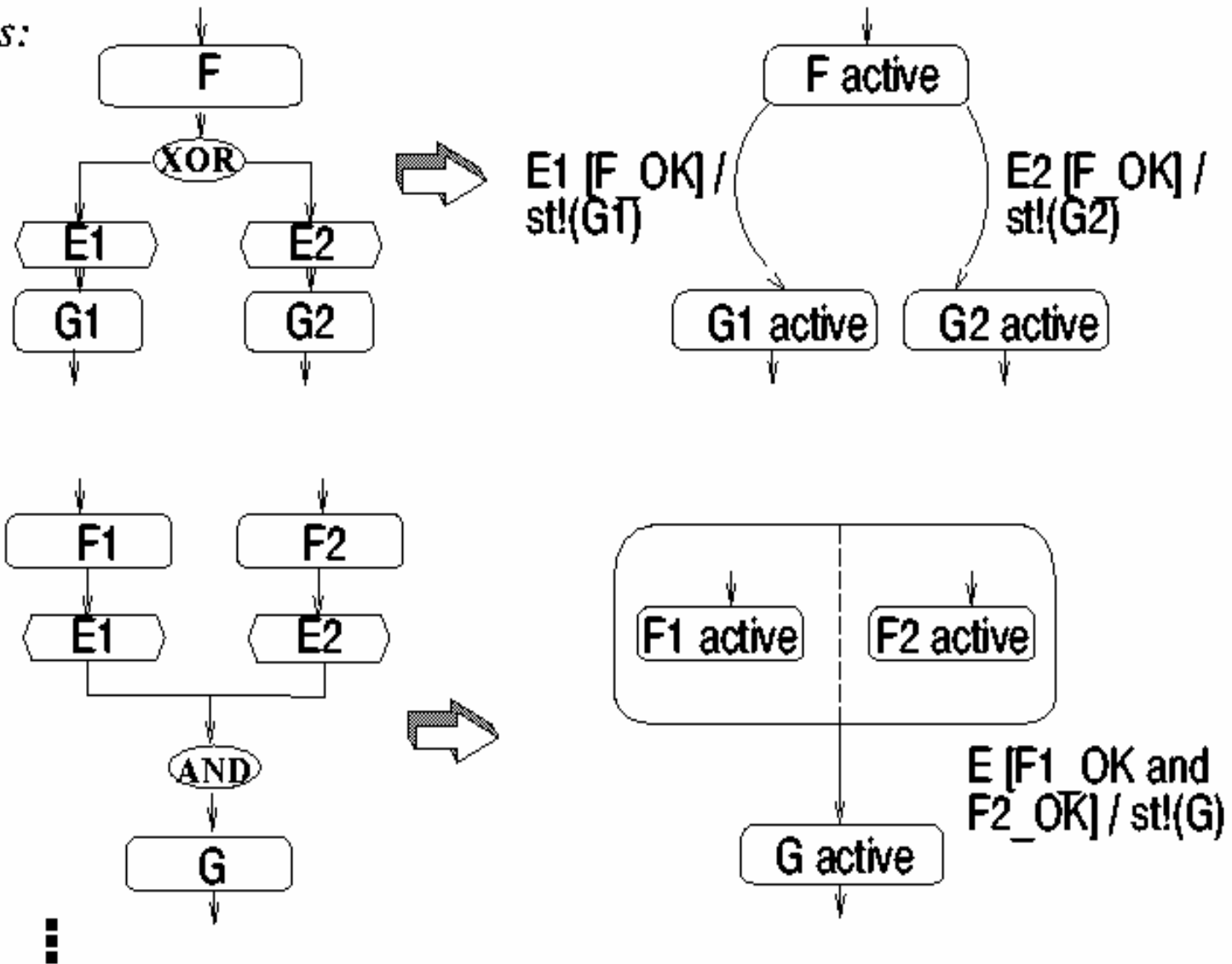
Event process chains

(EPCs à la Aris Toolset):

- process decomposed into functions
- completed functions raise events that trigger further functions
- control-flow connectors

# Import from BPR Tools (continued)

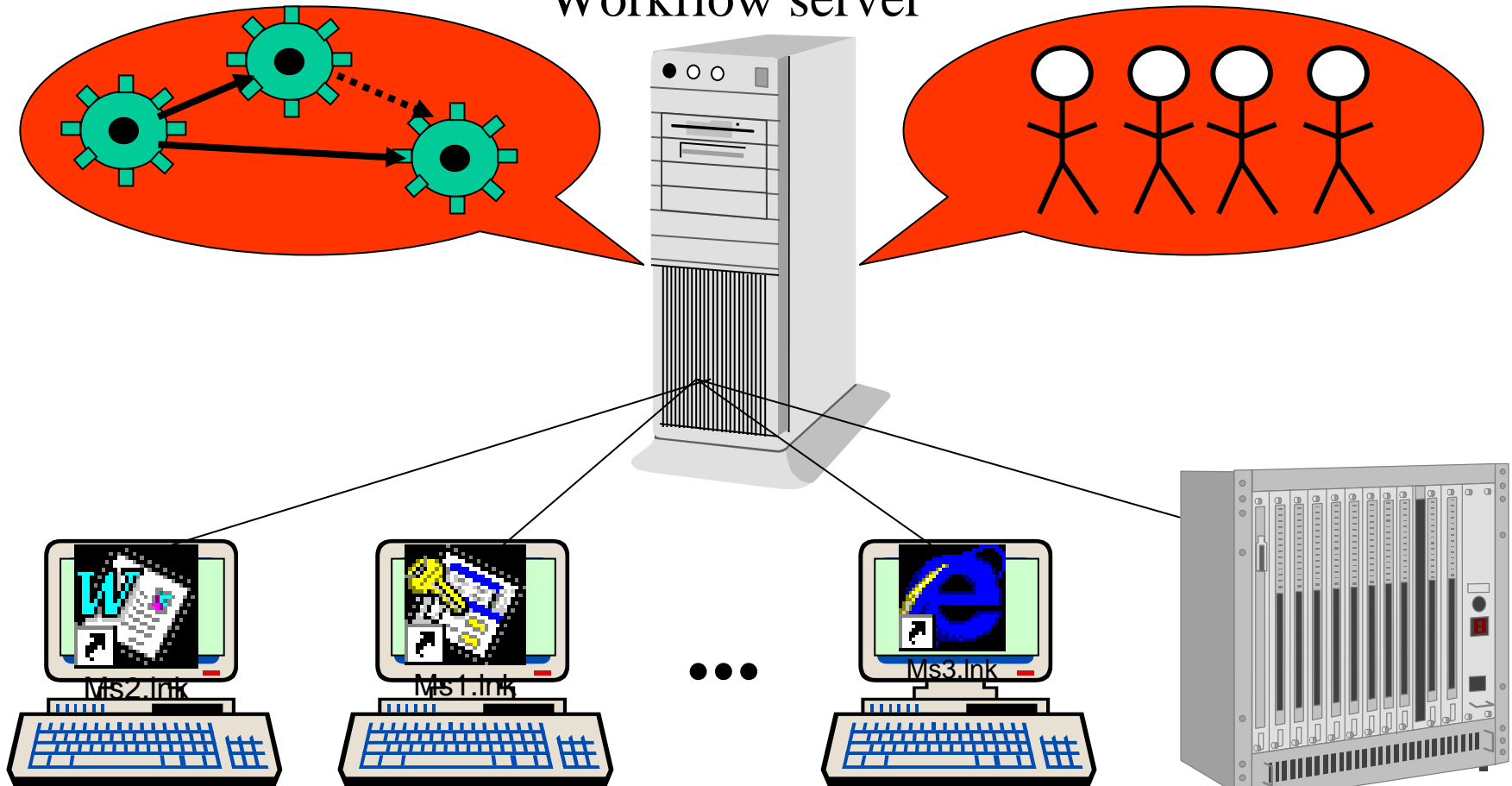
*Some Subtleties:*



# 13.2 Workflow Management System Architecture

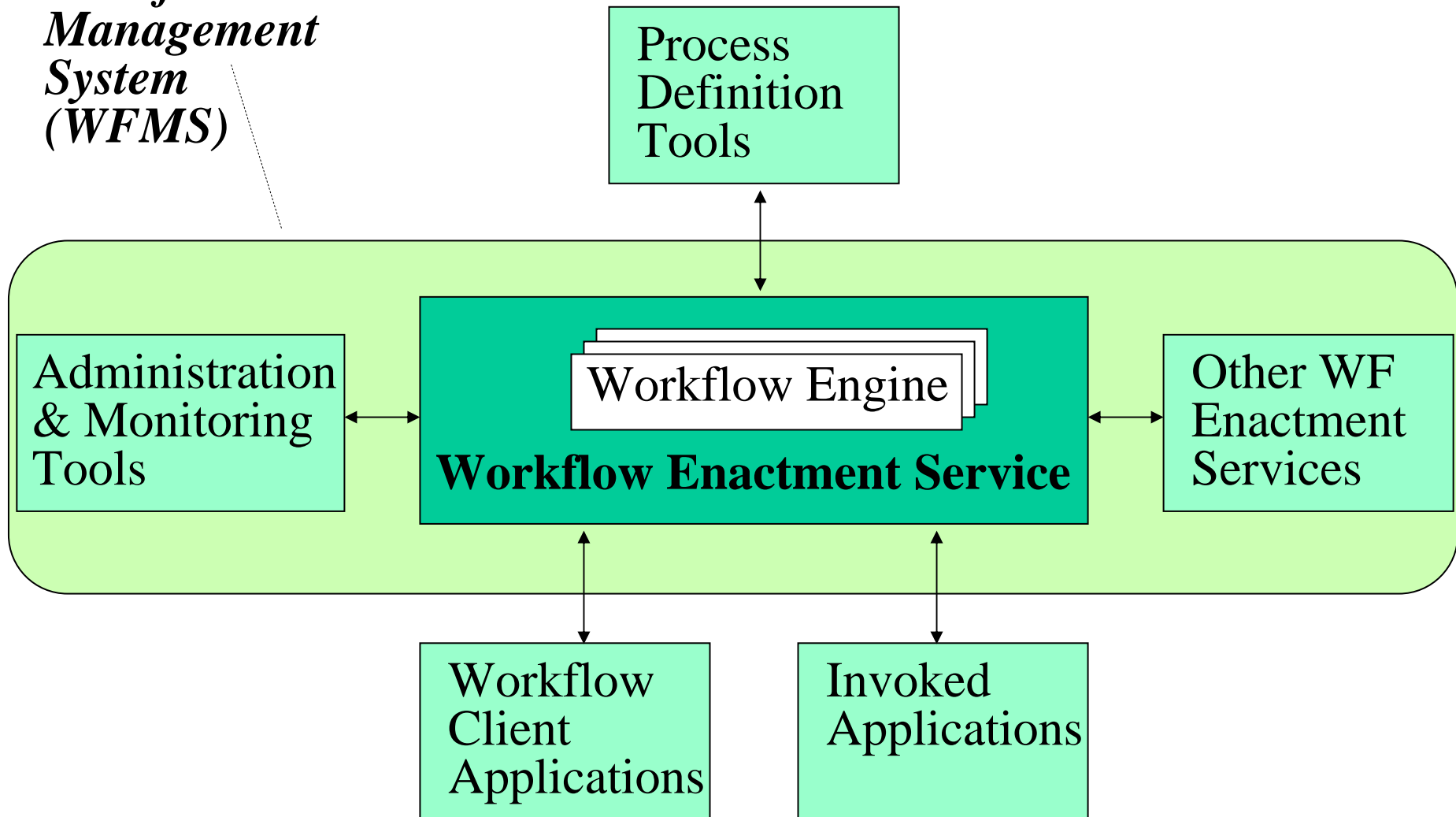
Workflow specification

Workflow server

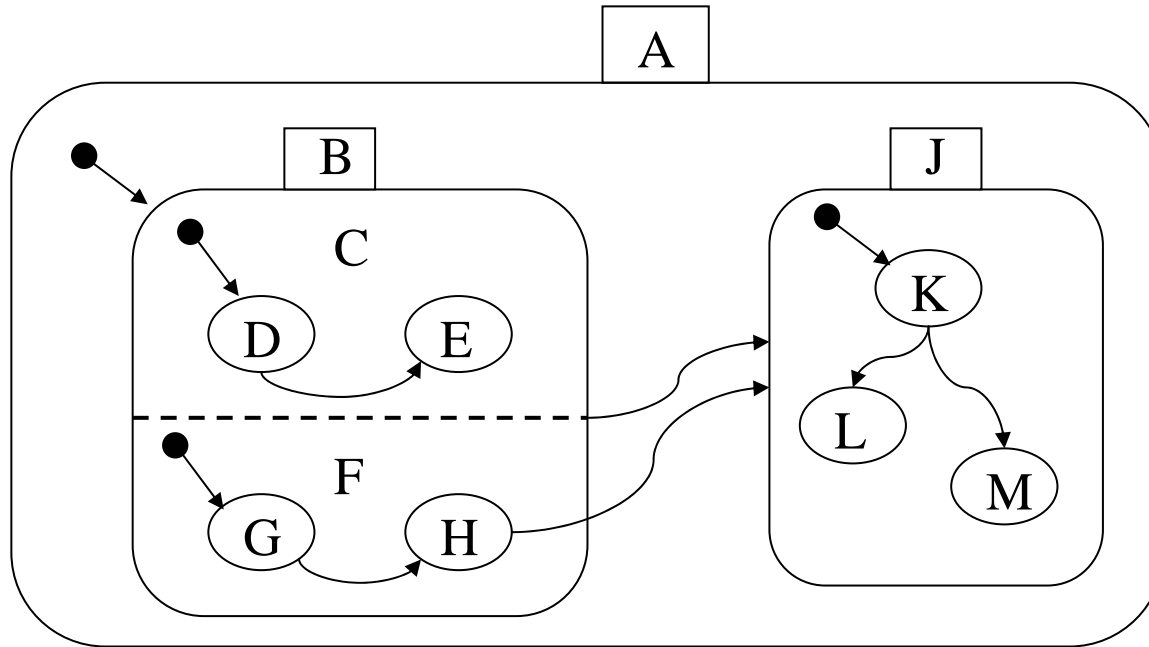


# WfMC Reference Architecture

*Workflow  
Management  
System  
(WFMS)*



# 13.3 Abstract Syntax of Statecharts (1)



State set  $S$

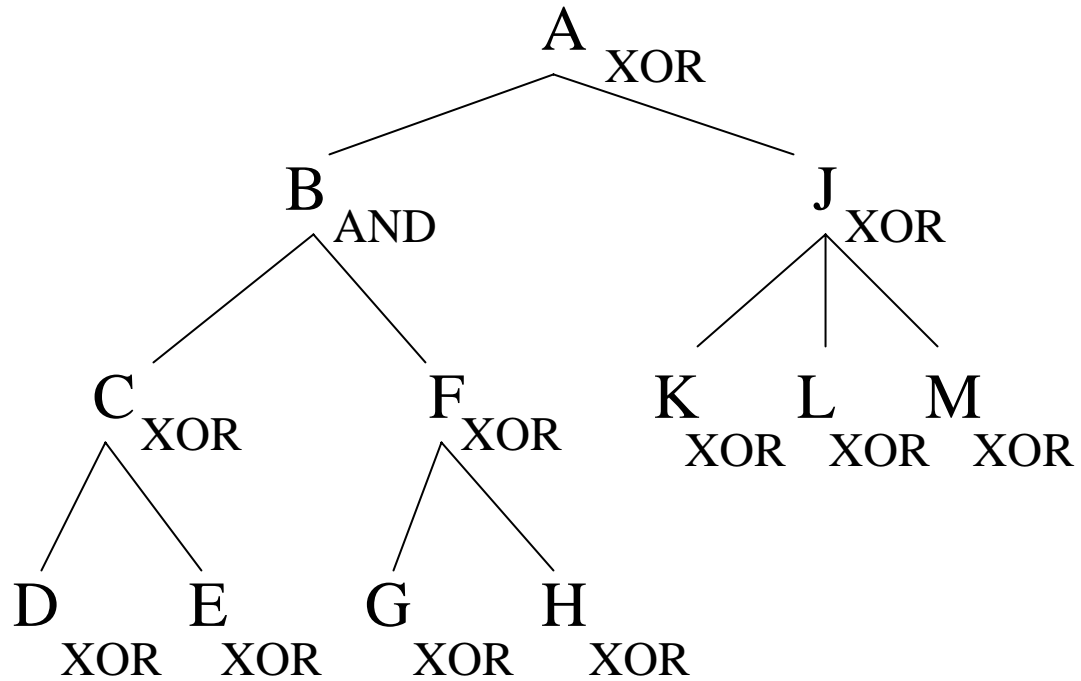
**State tree** (with node types AND or XOR)

Transition  $t$ : (source, target, [c]/a)

**Transition set**  $T$

Variable set  $V$

# Abstract Syntax of Statecharts (2)





# Operational Semantics of Statecharts (1)

**Execution state** of statechart  $(S, T, V)$ :

subset  $states \subseteq S$  of currently active states s.t.

- root of  $S$  is in states
- if  $s$  in states and type of  $s$  is AND then all children of  $s$  are in states
- if  $s$  in states and type of  $s$  is XOR then exactly one child of  $s$  is in states

**Execution context** of statechart  $(S, T, V)$ :

current values of variables defined by  $val: V \rightarrow \text{Dom}$

**Configuration** of statechart  $(S, T, V)$ :  $(states, val)$

**Initial configuration**

# Operational Semantics of Statecharts (2)

**Evaluation** of expression in configuration:  
eval (expr, conf) defined inductively

**Effect** of action on context:  
modification of variable values in val

**fire(conf)** = set of transitions

$t = (\text{source}, \text{target}, [\text{cond}]/\text{action})$

with source(t) in states for which eval(cond, conf) = true

# Operational Semantics of Statecharts (3)

for transition  $t$ :

- $a = \text{lca}(\text{source}(t), \text{target}(t))$
- $\text{src}(t) = \text{child of } a \text{ in subtree of } \text{source}(t)$
- $\text{tgt}(t) = \text{child of } a \text{ in subtree of } \text{target}(t)$

when  $t$  fires:

- set of left states  **$\text{source}^*(t)$** :
  - $\text{src}(t)$  is in  $\text{source}^*(t)$
  - if  $s$  in  $\text{source}^*(t)$  then all children of  $s$  are in  $\text{source}^*(t)$
- set of entered states  **$\text{target}^*(t)$** :
  - $\text{tgt}(t)$  and  $\text{target}(t)$  are in  $\text{target}^*(t)$
  - if  $s$  in  $\text{target}^*(t)$  and type of  $s$  is AND then all children of  $s$  are in  $\text{target}^*(t)$
  - if  $s$  in  $\text{target}^*(t)$  and type of  $s$  is XOR then exactly one child of  $s$  with initial transition is in  $\text{target}^*(t)$

# Operational Semantics of Statecharts (4)

For a given configuration  $\text{conf} = (\text{states}, \text{val})$  a **successor configuration**  $\text{conf}' = (\text{states}', \text{val}')$  is derived by selecting one transition  $t$  from  $\text{fire}(\text{conf})$  with the effect:

- $\text{states}' = \text{states} - \text{source}^*(t) \cup \text{target}^*(t)$
- $\text{val}'$  captures the effect of  $\text{action}(t)$  and equals  $\text{val}$  otherwise

The operational semantics of a statechart  $(S, V, T)$  is the set of all possible executions along configurations

$\text{conf}_0, \text{conf}_1, \text{conf}_2, \dots$  with

- initial configuration  $\text{conf}_0$  and
- $\text{conf}_{i+1}$  being a successor configuration of  $\text{conf}_i$

# Digression: Finite State Automata

## Definition:

Ein endlicher Automat (finite state automaton) ist ein 5-Tupel

$M = (Z, \Sigma, \delta, z_0, E)$  mit

- einer endlichen Zustandsmenge  $Z$
- einem Alphabet (d.h. einer endlichen Menge von Zeichen)  $\Sigma$
- einer Transitionsfunktion  $\delta: Z \times \Sigma \rightarrow Z$
- einem Startzustand  $z_0$
- einer Menge von Endzuständen  $E \subseteq Z$

$M$  geht in  $z \in Z$  mit Eingabe  $x \in \Sigma$  in  $\delta(z,x) \in Z$  über.

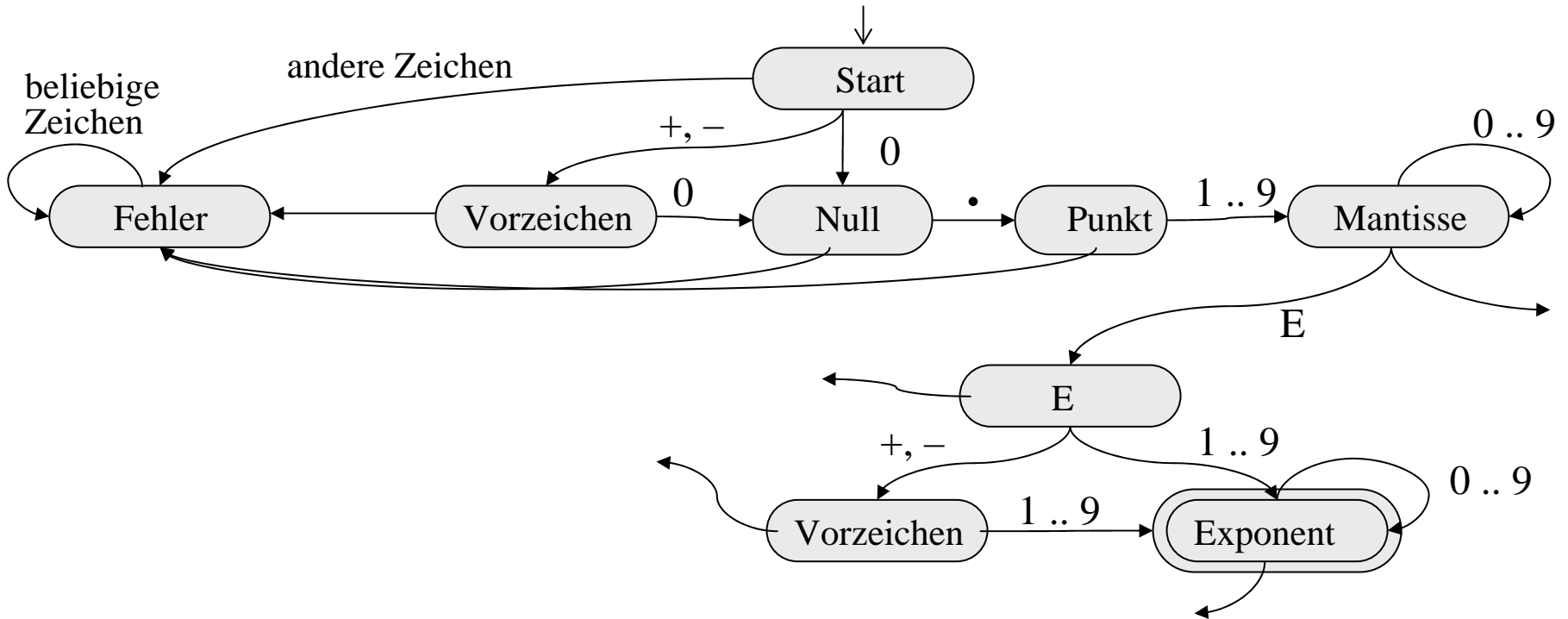
$\delta$  wird homomorph zur Funktion  $\delta^*: Z \times \Sigma^* \rightarrow Z$  erweitert:

$$\delta^*(z, au) = \delta^*(\delta(z,a),u) \text{ mit } z \in Z, a \in \Sigma, u \in \Sigma^*.$$

Die Menge  $L(M) = \{w \in \Sigma^* \mid \delta^*(z_0,w) \in E\} \subseteq \Sigma^*$

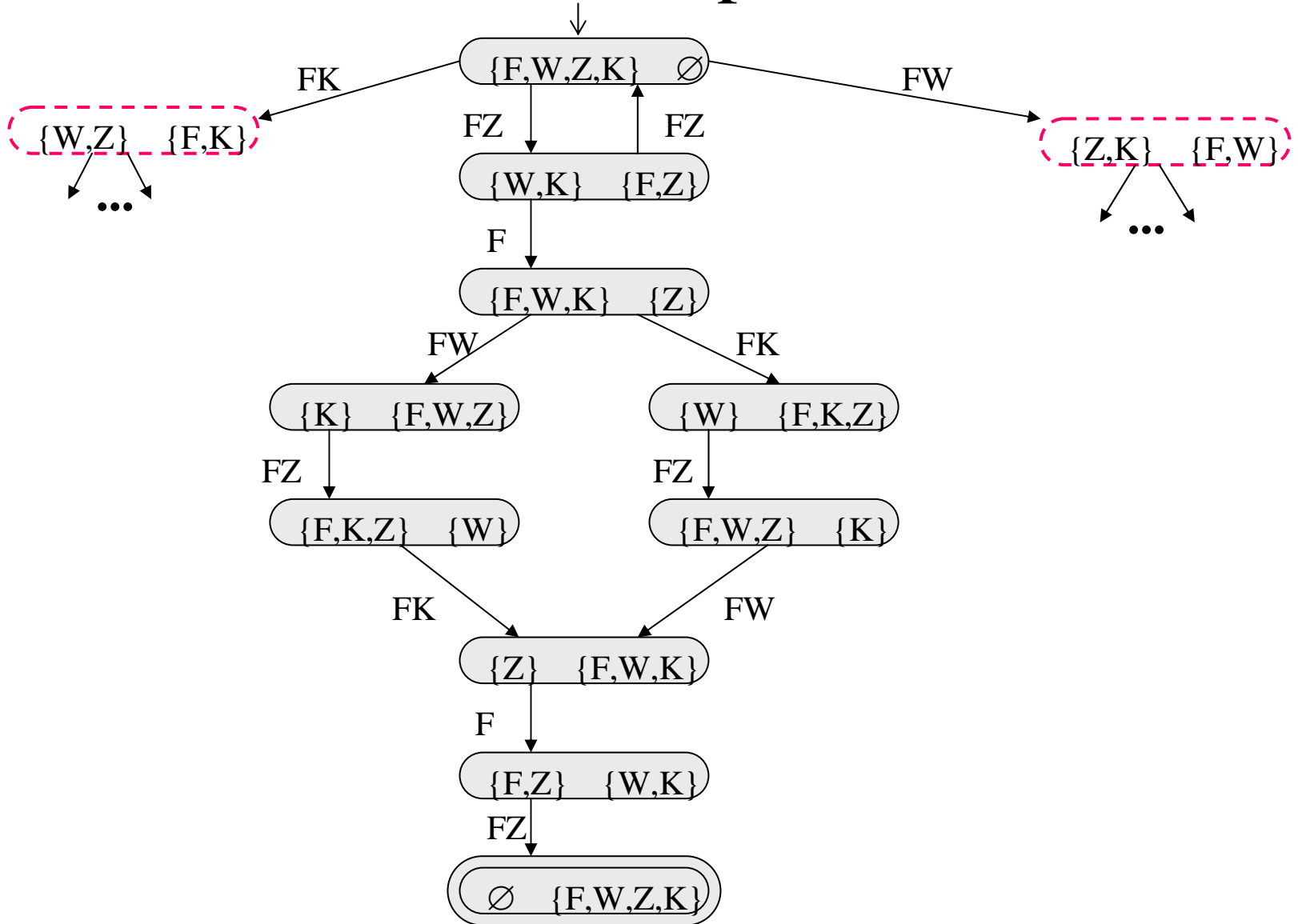
ist die vom Automat  $M$  akzeptierte Sprache.

# FSA Example 1



(offene Transitionen gehen zum Zustand „Fehler“)

# FSA Example 2



# Mapping Statecharts into FSAs

**Represent SC configurations as states of a FSA:**

**Step 1:**

**abstract conditions on infinite-domain variables into Boolean vars**

**formal mapping:  $\psi_1: \text{val} \rightarrow B_1 \times B_2 \times \dots \times B_m$**

**Step 2:**

**capture set of active SC states (in SC hierarchy and in components)**

**by powerset automaton  $\psi_2: \text{states} \rightarrow 2^S =: Z$**

**Step 3:**

**encode SC context into extended state space of FSA**

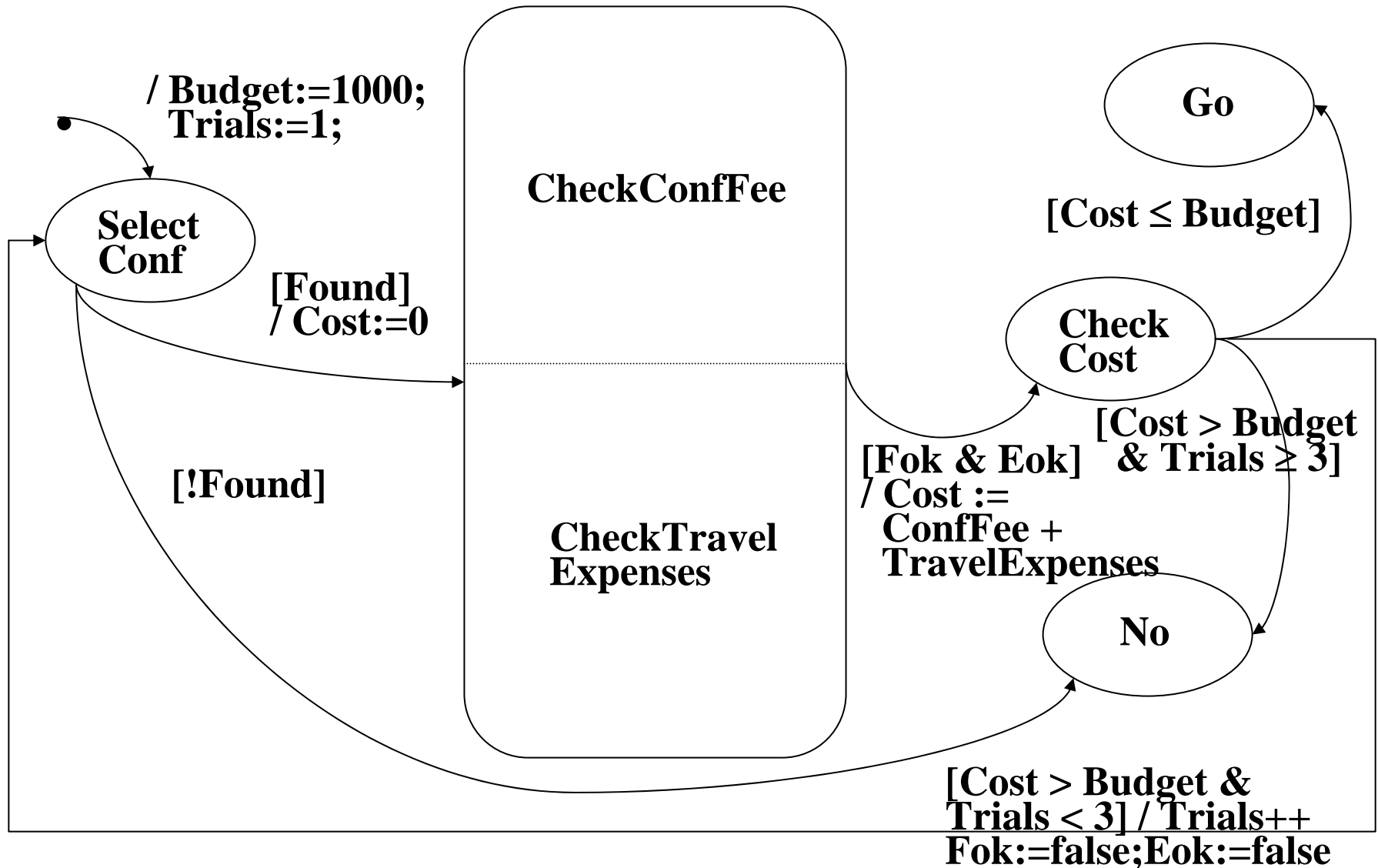
**by an injective mapping  $\psi_3: Z \times B_1 \times B_2 \times \dots \times B_m \rightarrow Z'$**

**such that there is a transition from  $z_1$  to  $z_2$  in the FSA**

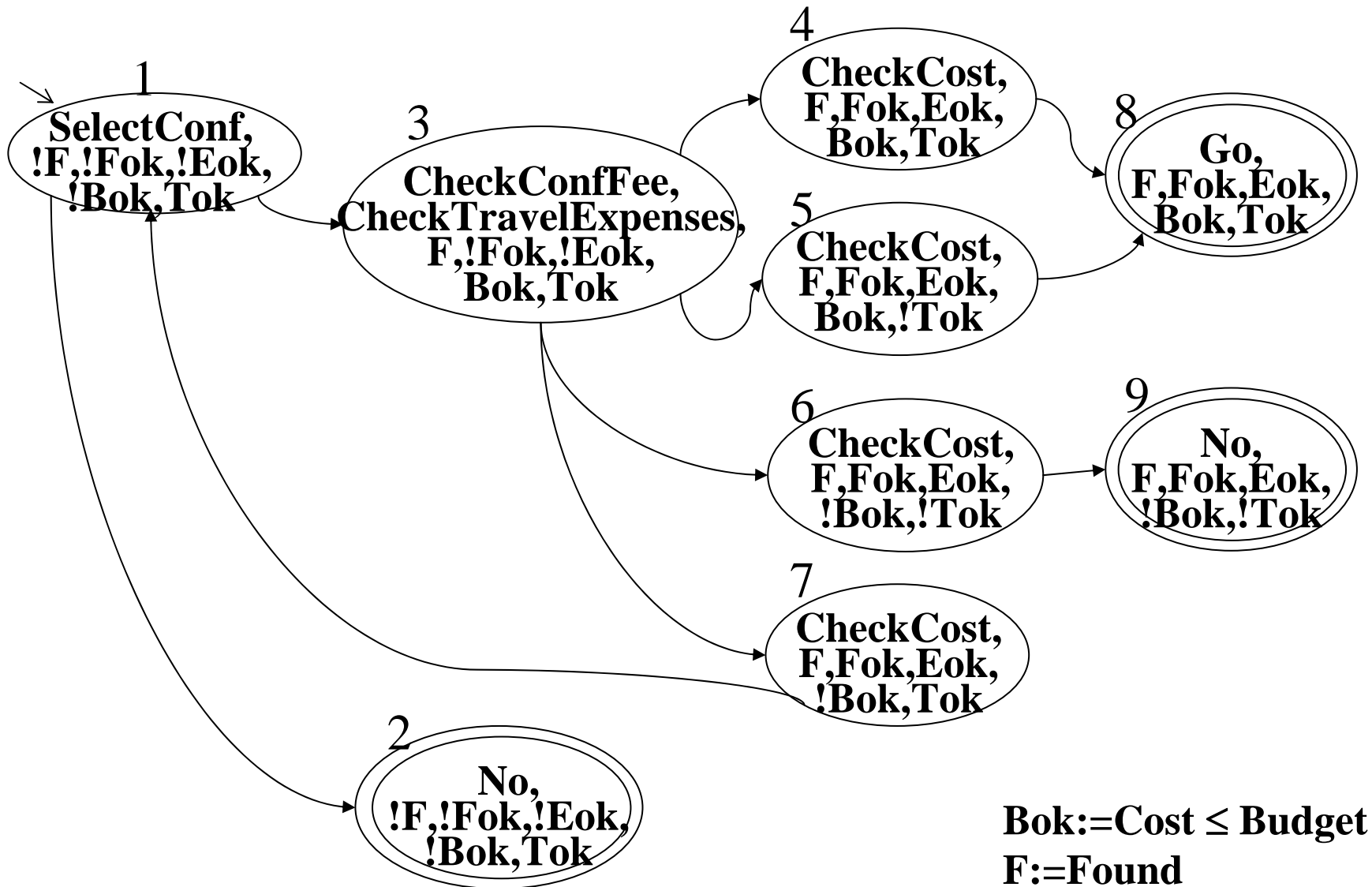
**iff  $\psi_3^{-1}(z_2)$  is a possible successor configuration of  $\psi_3^{-1}(z_1)$  in the SC**



# Example: From SC To FSA (1)



# Example: From SC To FSA (2)



**Bok:=Cost ≤ Budget**  
**F:=Found**  
**Tok:=Trials<3**

# 13.4 Guaranteed Behavior and Outcome of Mission-critical Workflows

Crucial for workflows in banking, medical applications, electronic commerce, etc.

- **Safety** properties (invariants):  
nothing bad ever happens
- **Liveness** properties (termination, fairness, etc.):  
something good eventually happens

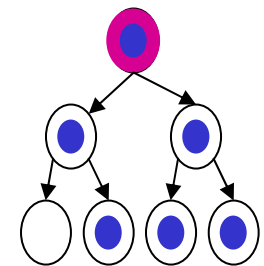
● Mathematical model	→	Finite-state automaton
● Formalization of properties	→	Temporal logic
● Verification method	→	Model checking

# CTL: Computation Tree Logic

- propositional logic formulas
- quantifiers ranging over execution paths
- modal operators referring to future states

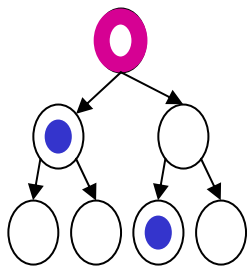
all  
next:

**AX p**



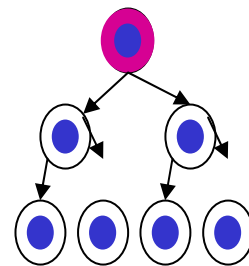
exists  
next:

**EX p**



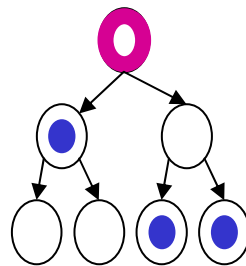
all  
globally:

**AG p**



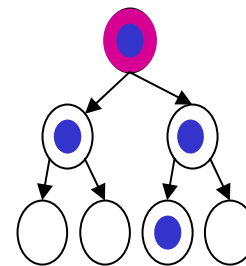
all finally  
(inevitably):

**AF p**



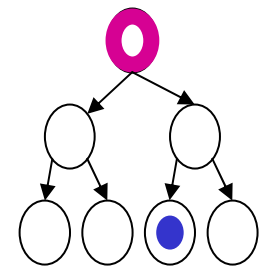
exists  
globally:

**EG p**



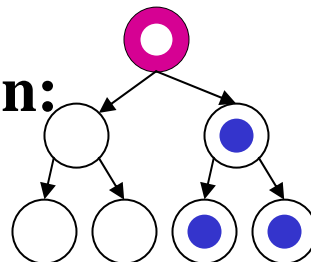
exists finally  
(possibly):

**EF p**



combination:

**EF AG p**



# Critical Properties of the Example Workflow

formalized in CTL (Computation Tree Logic)

- *Can we ever exceed the budget ?*

**not EF ( in(Go) and !Bok )**

**≡ AG ( not in(Go) or Bok )**

- *Do we always eventually reach a decision ?*

**AF ( in(Go) or in(No) )**

- *Can the trip still be approved after a proposal that would have exceeded the budget ?*

**EF ( (in(CheckCost) and !Bok) => ( EF (in(Go)) ) )**

# CTL Syntax

## Definition:

Eine atomare *CTL-Formel* ist eine aussagenlogische Formel über elementaren Aussagen (bzw. Booleschen Variablen).

Die Menge der in CTL erlaubten Formeln ist induktiv wie folgt definiert:

- Jede atomare CTL-Formel ist eine Formel.
- Wenn P und Q Formeln sind, dann sind auch EX (P), AX (P), EG (P), AG (P), EF (P), AF (P), (P),  $\neg P$ ,  $P \wedge Q$ ,  $P \vee Q$ ,  $P \Rightarrow Q$  und  $P \Leftrightarrow Q$  Formeln.

# CTL Semantik (1)

## Definition:

Gegeben sei eine Menge  $P$  atomarer aussagenlogischer Formeln.

Eine *Kripke-Struktur*  $M$  über  $P$  ist ein 4-Tupel  $(S, s_0, R, L)$  mit

- einer endlichen Zustandsmenge  $S$ ,
- einem Startzustand  $s_0 \in S$ ,
- einer Transitionsrelation  $R \subseteq S \times S$ ,
- einer Funktion  $L: S \rightarrow 2^P$ , die einem Zustand wahre Aussagen zuordnet.

## Definition:

Eine Kripke-Struktur  $M = (S, s_0, R, L)$  ist ein *Modell* einer Formel  $F$ , wenn  $M, s_0 \models F$ .

Eine Formel heißt *erfüllbar*, wenn sie mindestens ein Modell hat, ansonsten *unerfüllbar*.

Eine Formel  $F$  heißt *allgemeingültig* (oder Tautologie), wenn jede Kripke-Struktur über den atomaren Aussagen von  $F$  ein Modell von  $F$  ist.

# CTL Semantik (2)

## Definition:

Die *Interpretation*  $\psi$  einer Formel  $F$  mit atomaren Aussagen  $P$  ist eine Abbildung auf eine Kripke-Struktur  $M=(S, s_0, R, L)$  über Aussagen  $P$  so dass die Wahrheitswerte von Teilformeln  $p$  bzw.  $p_1, p_2$  von  $F$  in den Zuständen  $s$  von  $M$ , in Zeichen:  $M, s \models p$ , wie folgt sind:

- (i)  $M, s \models p$  mit einer aussagenlogischen Formel  $p$  gilt g.d.w.  $p \in L(s)$ ;
- (ii)  $M, s \models \neg p$  g.d.w. nicht  $M, s \models p$  gilt;
- (iii)  $M, s \models p_1 \wedge p_2$  g.d.w.  $M, s \models p_1$  und  $M, s \models p_2$ ;
- (iv)  $M, s \models p_1 \vee p_2$  g.d.w.  $M, s \models p_1$  oder  $M, s \models p_2$ ;
- (v)  $M, s \models EX p$  g.d.w. es  $t \in S$  gibt mit  $(s, t) \in R$  und  $M, t \models p$ ;
- (vi)  $M, s \models AX p$  g.d.w. für alle  $t \in S$  mit  $(s, t) \in R$  gilt:  $M, t \models p$ ;
- (vii)  $M, s \models EG p$  g.d.w. es  $t_1, \dots, t_k \in S$  gibt mit  $t_1 = s, (t_i, t_{i+1}) \in R$  für alle  $i$  und  $t_k = t_j$  für ein  $j: 1 \leq j < k$  oder  $t_k$  ohne Nachfolger, so dass  $M, t_i \models p$  für alle  $i$ ;
- (viii)  $M, s \models AG p$  g.d.w. für alle  $t \in S$  mit  $(s, t) \in R^*$  gilt:  $M, t \models p$ ;
- (ix)  $M, s \models EF p$  g.d.w. es  $t \in S$  gibt mit  $(s, t) \in R^*$  und  $M, t \models p$ ;
- (x)  $M, s \models AF p$  g.d.w. es für alle  $t \in S$  mit  $(s, t) \in R^*$  einen Zustand  $t' \in S$  gibt mit a)  $(t, t') \in R^*$  oder b)  $(s, t') \in R^*$  und  $(t', t) \in R^*$ , so dass  $M, t' \models p$  gilt.



# Model Checking

**Für CTL-Formel  $F$  und Transitionssystem (Kripke-Struktur)  $M$  teste, ob  $M$  ein Modell von  $F$  ist, indem man induktiv alle Zustände von  $M$  mit  $q$  markiert, in denen die Teilformel  $q$  von  $F$  wahr ist.**

**Sei  $q$  eine Teilformel von  $F$ , seien  $p, p_1, p_2$  direkte Teilformeln von  $q$  und seien  $P, P_1, P_2$  die mit  $p, p_1, p_2$  markierten Zustände von  $M$ .**

**(i)  $q$  ist eine atomare Aussage (Boolesche Variable):**

**Markiere alle Zustände  $s$  mit  $q \in L(s)$  mit  $q$**

**(ii)  $q$  hat die Form  $\neg p$ : Markiere  $S - P$  mit  $q$**

**(iii)  $q$  hat die Form  $p_1 \wedge p_2$ : Markiere  $P_1 \cap P_2$  mit  $q$**

**(iv)  $q$  hat die Form  $p_1 \vee p_2$ : Markiere  $P_1 \cup P_2$  mit  $q$**

**(v)  $q$  hat die Form  $EX p$ :**

**Markiere alle Vorgänger von  $P$  mit  $q$ , also alle  $s \in S$ , für die es ein  $x \in P$  gibt mit  $R(s, x)$**

**(vi)  $q$  hat die Form  $AX p$ :**

**Markiere  $s$  mit  $q$ , wenn alle Nachfolger von  $s$  mit  $p$  markiert sind**

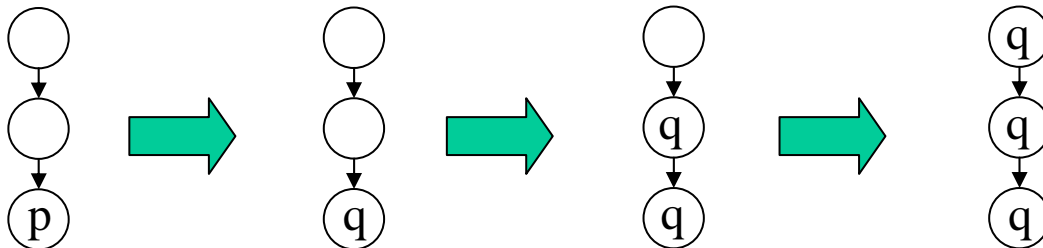
# Model Checking: Fall EF

(vii)  $q$  hat die Form  $EF\ p$ :

Löse Rekursion  $EF\ p \Leftrightarrow p \vee EX\ (EF\ p)$ .

(Fixpunktgleichung  $Q = P \cup \text{pred}(Q)$ )

```
Q := P;  
Qnew := Q  $\cup$  pred(Q);  
while not (Q = Qnew) do  
  Q := Qnew;  
  Qnew := Q  $\cup$  pred(Q);  
od;
```

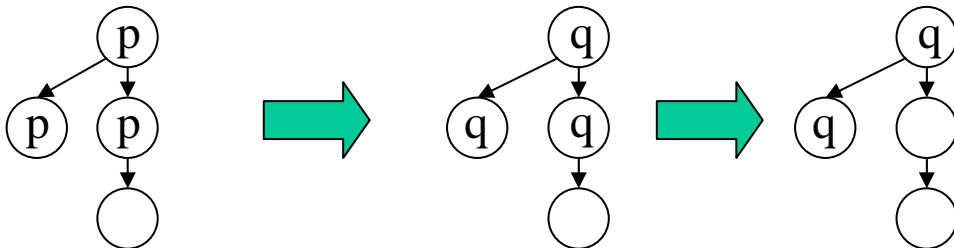


# Model Checking: Fall EG

(viii)  $q$  hat die Form  $EG\ p$ :

Löse Rekursion  $EG\ p \Leftrightarrow p \wedge EX\ (EG\ p)$  :

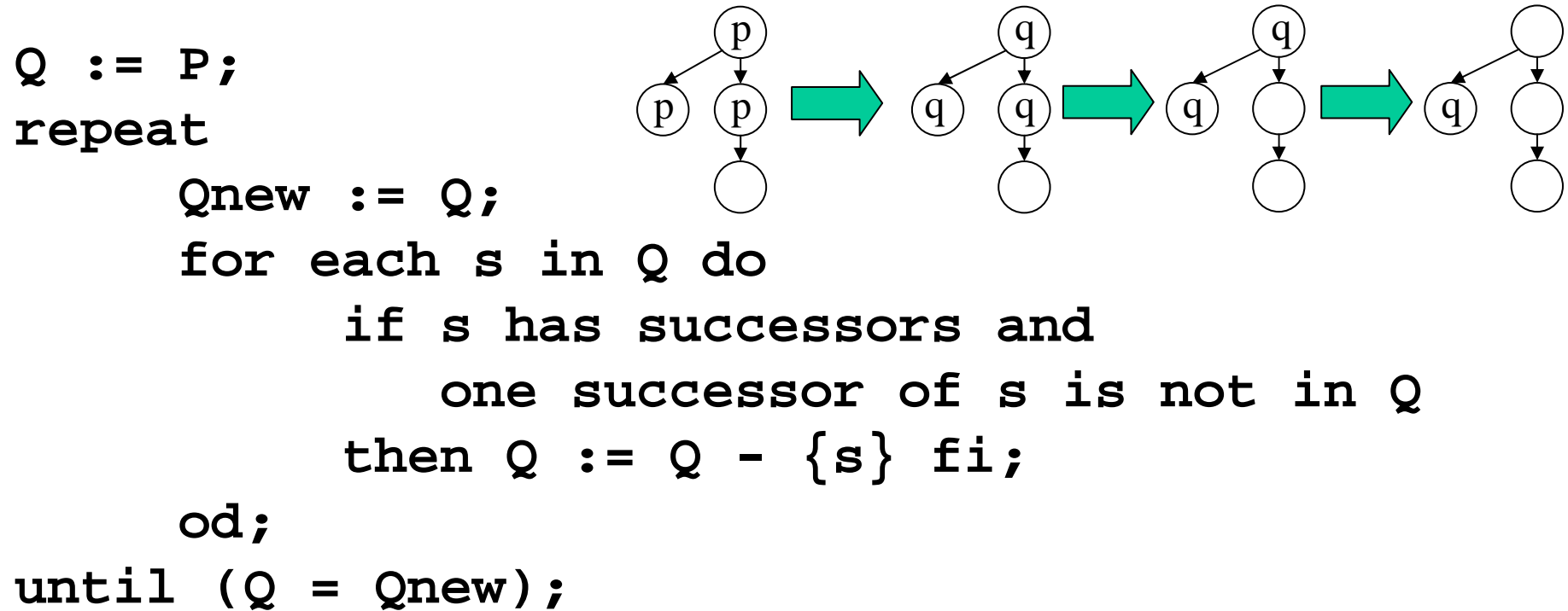
```
Q := P;  
repeat  
  Qnew := Q;  
  for each s in Q do  
    if s has successors and  
       no successor of s is in Q  
    then Q := Q - {s}; fi;  
od;  
until (Q = Qnew);
```



# Model Checking: Fall AG

(ix)  $q$  hat die Form  $AG\ p$ :

Löse Rekursion  $AG\ p \Leftrightarrow p \wedge AX\ (AG\ p)$



Alternativ wegen  $AG\ p \Leftrightarrow \neg EF\ (\neg p)$ :

Berechne Zustandsmenge  $Q'$  zur Formel  $EF\ (\neg p)$   
und markiere dann die Zustandsmenge  $S - Q'$  mit  $q$ .

# Model Checking: Fall AF

(x)  $q$  hat die Form  $AF\ p$ :

Löse Rekursion  $AF\ p \Leftrightarrow p \vee AX\ (AF\ p)$

```
Q := P;
```

```
repeat
```

```
    Qnew := Q;
```

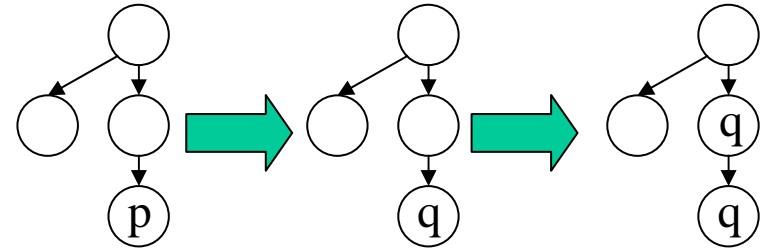
```
    for each  $s$  in  $\text{pred}(Q)$  do
```

```
        if all successors of  $s$  are in  $Q$ 
```

```
            then  $Q := Q \cup \{s\}$ ; fi;
```

```
    od;
```

```
until ( $Q = Q_{\text{new}}$ );
```



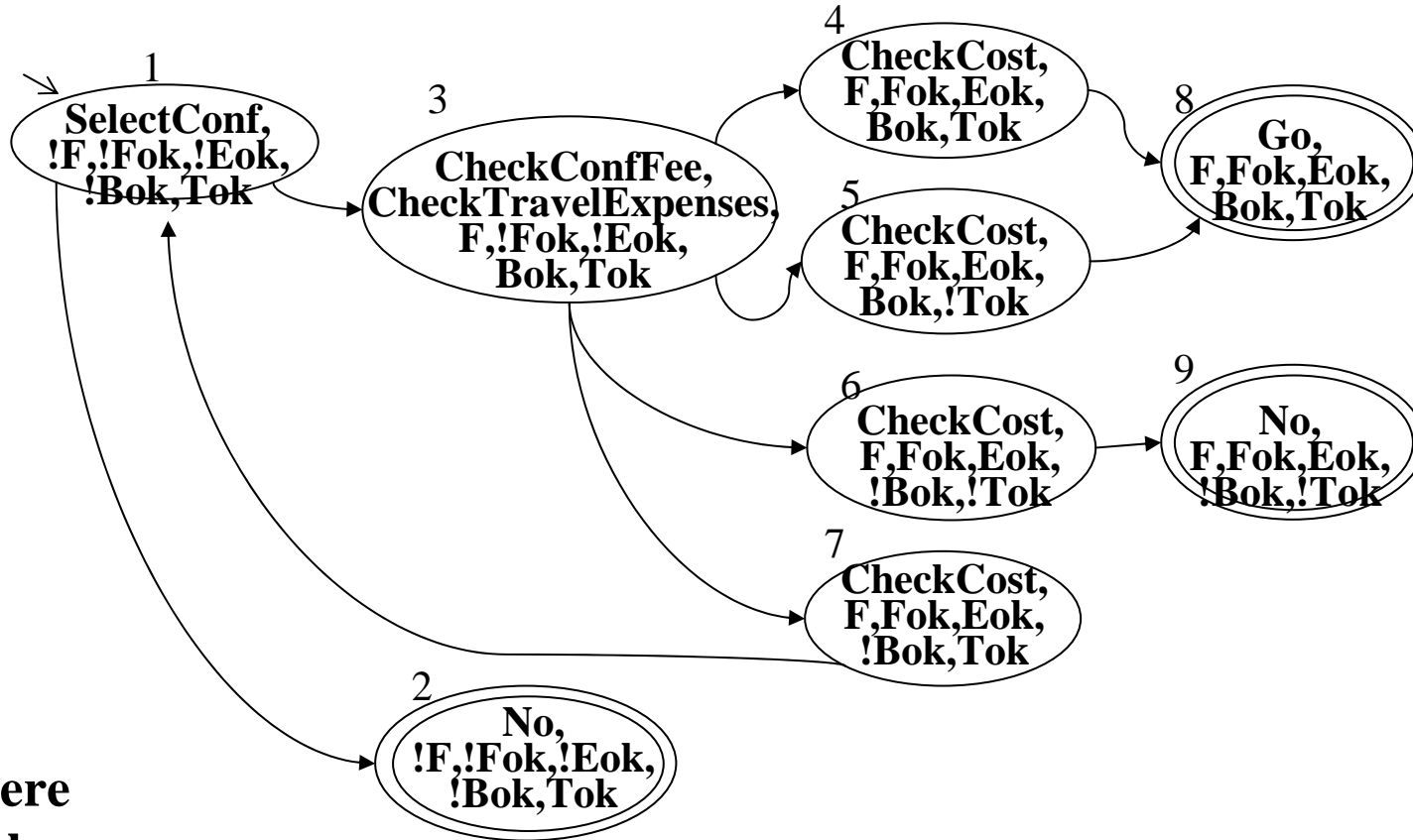
Alternativ wegen  $AF\ p \Leftrightarrow \neg EG\ (\neg p)$ :

Berechne Zustandsmenge  $Q'$  zur Formel  $EG\ (\neg p)$

und markiere dann die Zustandsmenge  $S - Q'$  mit  $q$ .

# Model Checking: Beispiel 1

**AG ( not in(Go) or Bok )**



**Markiere**

**mit Bok:**

**mit in(Go):**

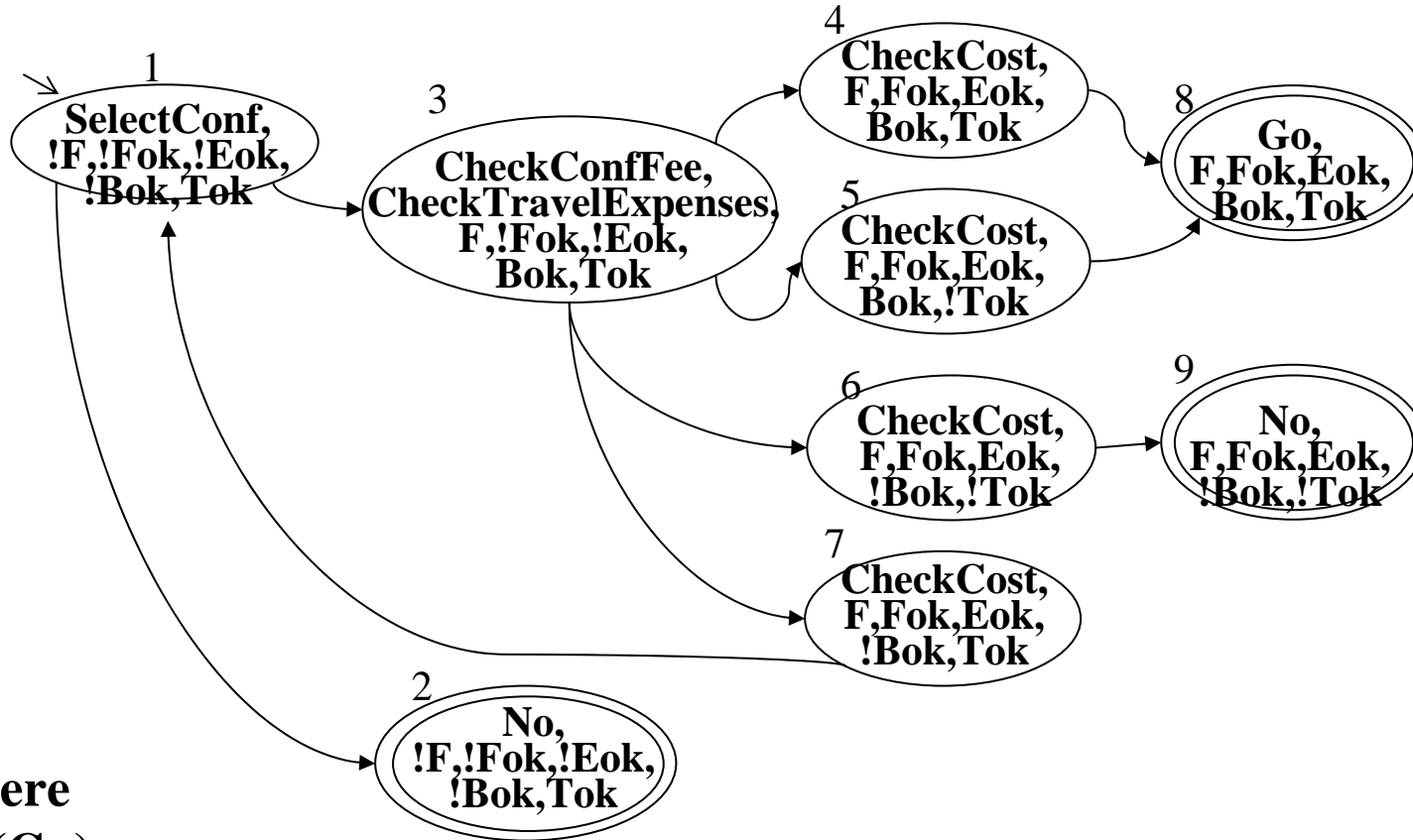
**mit  $\neg$ in(Go):**

**mit  $(\neg$ Bok  $\Rightarrow$   $\neg$ in(Go)):**

**mit AG  $(\neg$ Bok  $\Rightarrow$   $\neg$ in(Go)):**

# Model Checking: Beispiel 2

AF ( $\text{in}(\text{Go}) \vee \text{in}(\text{No})$ )



Markiere

mit  $\text{in}(\text{Go})$ :

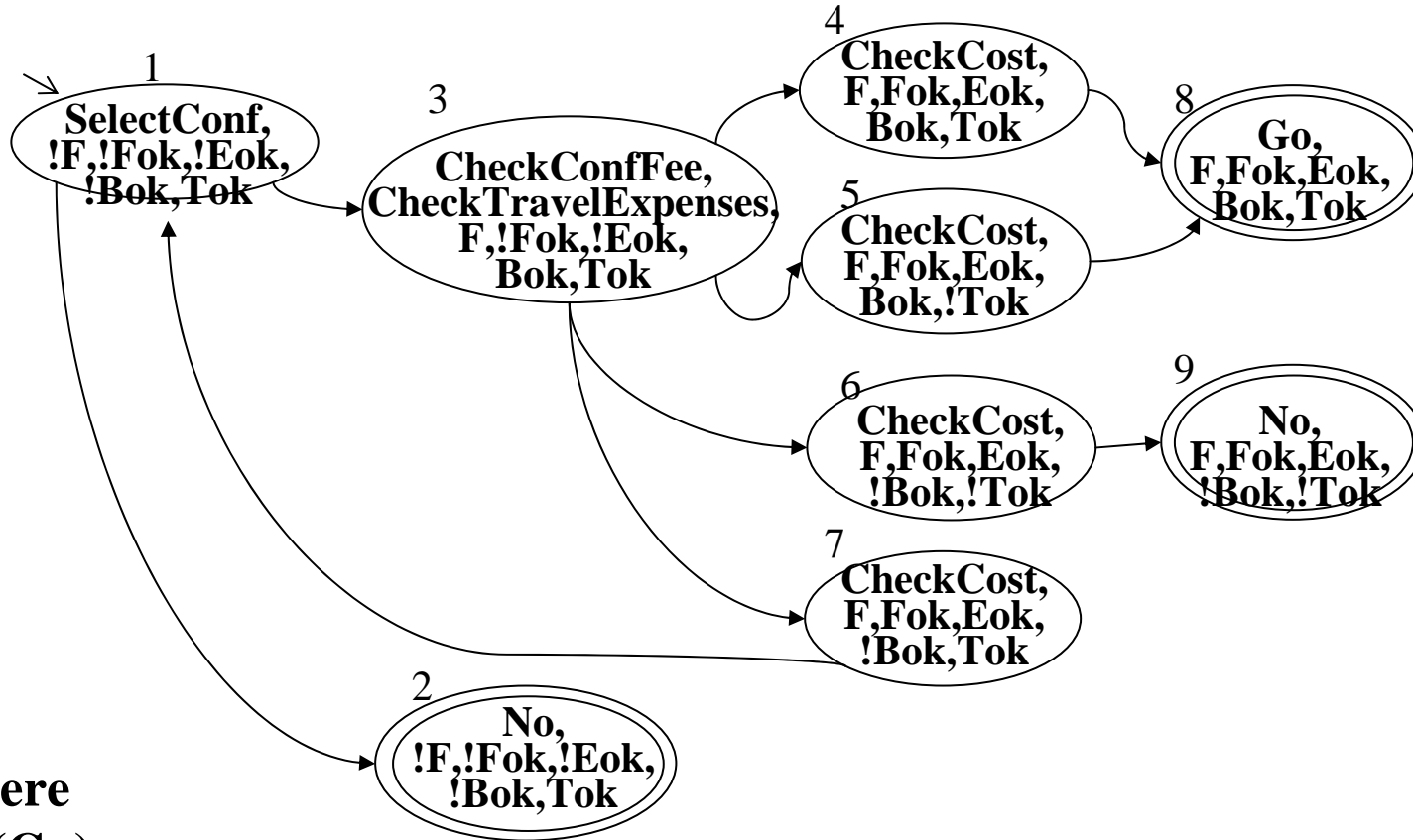
mit  $\text{in}(\text{No})$ :

mit  $\text{in}(\text{Go}) \vee \text{in}(\text{No})$ :

mit AF ( $\text{in}(\text{Go}) \vee \text{in}(\text{No})$ ):

# Model Checking: Beispiel 3

**EF ( (in(CheckCost) and !Bok) => ( EF (in(Go)) ) )**



**Markiere**

**mit in(Go):**

**mit EF (in(Go)):**

**mit not in(CheckCost) or Bok:**

**mit (in(CheckCost) and !Bok) => ( EF (in(Go))):**

**mit EF ( (in(CheckCost) and !Bok) => ( EF (in(Go)) ) ):**



# Guaranteed Behavior of Workflows

- **Leverage computer-aided verification techniques for finite-state concurrent systems**
- **Efficiency gain with encoding of FSM as OBDD**
- **Further requirements:**
  - **User-friendly macros for CTL**
  - **More expressive logic**
  - **Adding assertions on behavior of invoked apps**
  - **Adding real-time (clock variables)**

- **Preserving guaranteed behavior in distributed, failure-prone system environment**  
→ **System guarantees**