Kurt Mehlhorn





- better understanding for Informatics (Computer Science)
- my fascination for the field and glimpses at my work
- a bit entertaining

slides available on my home page



Outline of Talk

Information Technology has changed the world







- Early Fascination
- Algorithms and Programs
 - What is an Algorithm, what is a Program?
 - Laws of Computation
 - Connections to Other Fields
 - Theory and Practice, Mathematics and Engineering
- Future



My first Encounter with Informatics

- Informatics was introduced as an area of study in Germany in 1968; I started to study in 1968.
- I had no idea what informatics is about; I had never seen a computer except on pictures.
- The lectures
 - Math: polished, even difficulty, basement of a tower of knowledge, instructor had material at his finger tips.
 - Informatics: rough, uneven difficulty, bits and pieces, instructor (F. L. Bauer) struggled with content.



Ena and I, 73

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F.L. Bauer

Early Fascination

Formal Languages and Programming Languages

- syntax and semantics defined without any ambiguity
- programming language = language for specifying computations
- Algol 68: definition finished in Dec. 68; given to read in Jan. 69



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Algorithms and Programs

- An algorithm is a step-by-step procedure for solving a certain class of problems.
- two examples



Al-Khwarizmi, 780 – 850

The Compendious Book on Calculation by Completion and Balancing



1-pound piece calf's liver, 3/4 pound onions, sliced paper-thin, 4 tablespoons unsalted butter, 1/3 cup water, 1 tablespoon chopped parsley

- Rinse liver to remove any traces of blood and discard membrane and any tough veins. Cut crosswise into 1/8-inch-thick slices.
- 2. Cook onions in 2 tablespoons butter in a 12-inch heavy skillet over moderate heat, stirring, 1 minute. Cover skillet and continue to cook, stirring occasionally, until softened and golden brown, about 10 minutes. Transfer to a bowl and keep warm, covered.
- 3. Pat half of liver slices dry and toss with salt and pepper to taste. ...



A Second Algorithm: Solving a Quadratic Equation

Algorithm

Sample Execution

write the equation as $x^2 + bx + c = 0$ $x^2 + 8x - 9 = 0$ move the constant term to the other side $x^2 + 8x = 9$ add $(b/2)^2$ on both sides $x^2 + 8x + 4^2 = 9 + 4^2$ write LHS as $(x + b/2)^2$, simplify RHS $(x + 4)^2 = 25$ if RHS is negative, STOP (no solution)remove 2 on LHS, replace RHS by $\pm\sqrt{\text{RHS}}$ $x + 4 = \pm\sqrt{25}$ move constant term from LHS to RHS $x = -4 \pm \sqrt{25}$

Algorithm is in Al-Kwarizmi's book.



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Both algorithms are for human computers, programs for real computers are much more detailed.



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Formative Insights

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Formative Insights

- Intellectually demanding tasks can be mechanized.
- Computers amplify brain power.
- Algorithm design and programming are acts of creation.



Physicists discover laws of nature, informaticians discover laws of computation,



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in particular, limits of efficiency for performing certains tasks.

We measure efficiency in terms of

- time (number of elementary steps needed), and
- space (number of symbols needed to store intermediate results).



Der MIPS R10K Prozessorchip.



The block FP-Mult multiplies numbers.

It occupies about 3 by 4 mm of space.

It multiplies numbers in 5 microseconds

Is this good?



- Complexity measures
 - A = area of the circuit

$$T = execution time$$

- There are many different circuits for multiplication:
 - circuits that are fast, but also large,
 - circuits that are small, but also slow.

Is there a circuit that is small and fast?



Is there a Circuit that is Small and Fast?

NO



Is there a Circuit that is Small and Fast?



Every combination of A and T in red region is impossible.

Every combination of A and T in green region can be realized.



Connections to Other Fields



- engineering embedded systems, circuit design, autonomous systems, computer vision linguistics machine translation, speech recognition, information retrieval bioinformatics, computations in nature biology and medicine economics business processes, game theory,
- art computer graphics

natural sciences

- algorithmic economics
- - high performance computing







(b)





Physarum, a slime mold

single cell, several nuclei

show video







Mathematical Model (Tero et al., J. Theor. Biology 2007)

- Physarum is a network of pipes.
- Flow of liquids is determined by concentration differences and lengths and diameters of pipes.
- Pipes adapt: if flow through a pipe is high (low) relative to diameter of the pipe, the diameter grows (shrinks).





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Theorem (Bonifaci, KM, Varma, 2012, J. Theor. Biology)

Network converges to shortest path, i.e.,

the diameter of tubes not on the shortest path converges to zero.



Mathematician in the Morning, Engineer in the Afternoon

Mathematician

works on problems of a fundamental nature that

- are intrinsic to the field,
 e.g. laws of computation or new algorithms or
- come up in applications (and are too hard for engineers)

Engineer

- turns algorithms into programs
- designs and builds systems
- turns ideas into working systems
- identifies the needs for further theory



Library of Efficient Data Structures and Algorithms

joint work with S. Näher and C. Uhrig

when I asked former students,



Library of Efficient Data Structures and Algorithms

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- when I asked former students,
- Insight (1990): Writing books and articles does not suffice.

Must turn knowledge of the field into software that is

- easy-to-use,
- correct,
- efficient.



- started LEDA project in 1990, later CGAL, STXXL, SCIL
- in use at thousands of academic and industrial sites
 Algorithmic Solutions GmbH



The Project Almost Ruined My Reputation

Some of our programs were incorrect.



What had gone wrong and what did we do about it?

We had followed the state of the art, however



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• we made mistakes and wrote incorrect programs.

Adopted new design principle: certifying algorithms.



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we made mistakes and wrote incorrect programs.

Adopted new design principle: certifying algorithms.

Today, LEDA is a main source of my reputation.





- A user feeds *x* to the program, the program returns *y*.
- How can the user be sure that, indeed,

y is the correct output for input x?

The user has no way to know.

analogy: construction company



Programs must justify (prove) their answers in a way that is easily checked by their users.



Certifying Algorithms



On input x, a certifying algorithm computes

- the function value y and
- a witness w. (convincing evidence that y is the correct output for x)



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- a witness *W*. (convincing evidence that *y* is the correct output for *x*)

w is inspected by either the human user of the certifying program

or more elegantly by a checker program C.



Planar Graph

A graph is planar if it can be drawn in the plane without edge crossings.



planar drawing planar graph

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nonplanar graphs

Fact: Every non-planar graph contains a Kuratowski graph. Story and Demo



- I do not claim that I invented the concept; it is rather an old concept
 - al-Kwarizmi (780 850): multiplication
 - extended Euclid (\approx 1700): gcd
 - primal-dual algorithms in combinatorial optimization
 - Blum et al.: Programs that check their work
- I do claim that Stefan N\u00e4her and I were the first (1995) to adopt the concept as the design principle for a software project:

LEDA (Library of Efficient Data Types and Algorithms)



McConnell/M/Näher/Schweitzer (2010): 80 page survey









Answer till 2011: checkers are simple programs and hence we get them correct.





Answer till 2011: checkers are simple programs and hence we get them correct.

Today's answer: checkers are simple programs and hence we can prove their correctness using formal mathematics.



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Formal Mathematics

- Mathematics is carried in a formal language without any ambiguities.
- Proofs are machine-checked.
- Isabelle/HOL (L. Paulson/T. Nipkow)

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 $\begin{array}{l} \mbox{definition } disjoint-edges :: (\alpha, \beta) \ pre-graph \Rightarrow \beta \Rightarrow \beta \Rightarrow bool \ \mbox{where} \\ disjoint-edges G \ e_1 \ e_2 = (\\ & start \ G \ e_1 \ e_2 \ = (\\ & start \ G \ e_1 \ e_2 \ e_2 \ \land \ target \ G \ e_1 \ \neq target \ G \ e_2 \ \land \ target \ G \ e_1 \ \neq target \ G \ e_2 \ \land \ target \ G \ e_1 \ \neq target \ G \ e_2 \ \land \ target \ G \ e_1 \ \neq target \ G \ e_2 \ \land \ target \ G \ e_2 \ \land \ target \ G \ e_1 \ \neq target \ G \ e_2 \ \land \ target \ G \ e_1 \ \neq target \ G \ e_2 \ \land \ target \ G \ e_2 \ \land \ target \ G \ e_1 \ \neq target \ G \ e_2 \ \land \ target \ G \ e_2 \ \ target \ farget \$

using assms by (auto simp add: edge_as_set_def disjoint_arcs_def matching_def)

shows edge_as_set $e_1 \cap$ edge_as_set $e_2 = \{\}$

101 (B) (E) (E) (E) E 900



Formal Mathematics

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using assms by (auto simp add: edge_as_set_def disjoint_arcs_def matching_def)

We formally verify

(D) (B) (E) (E) (E) (D)

- the witness property (e.g., Kuratowski \rightarrow non-planarity),
- termination of the checker program, and
- correctness of the checker program.

Formal Instance Correctness

If a formally verified checker accepts a triple (x, y, w),

we have a formal proof that y is the correct output for input x.

- highest achievable trust (only Isabelle kernel to be trusted)
- a way to build large libraries of trusted algorithms

Alkassar/Böhme/M/Rizkallah: Verification of Certifying Computations, JAR 2014 Noshinski/Rizkallah/M: Verification of Certifying Computations through AutoCorres and Simpl, NASA Formal Methods Symposium 2014





Trends

from information to knowledge

big data and machine learning

autonomous systems

security, privacy, and accountability









Ideas of Informatics

- an introduction to informatics for non-specialists (Studium Generale)
- goal: informatics litteracy
- presents concepts and their applications, e.g.,
 - cryptography and electronic banking
 - shortest path algs and

navigation systems

machine learning and

automatic translation

- in WS 14/15: (internal) online-course
- in WS 15/16: public on-line course (lversity) with credit points.



Thank You

