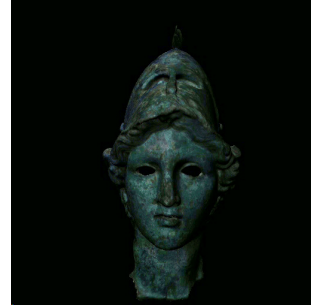

Reflectance Fields and Transport Matrices

Computational Photography

Hendrik Lensch, Summer 2007

Digitizing Real World Objects

images – no interaction

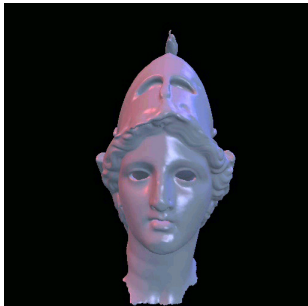


Computational Photography

Hendrik Lensch, Summer 2007

Digitizing Real World Objects

3D geometry – no color

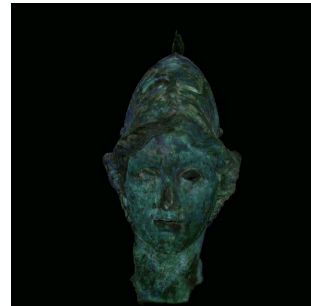


Computational Photography

Hendrik Lensch, Summer 2007

Digitizing Real World Objects

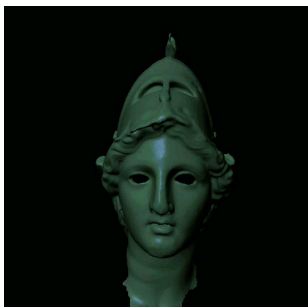
3D geometry plus texture – no relighting



Computational Photography

Hendrik Lensch, Summer 2007

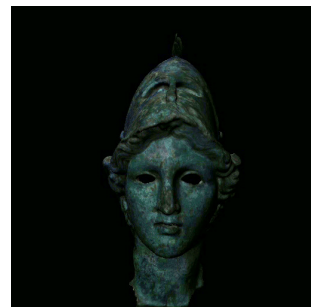
Single Material - BRDF



Computational Photography

Hendrik Lensch, Summer 2007

Spatially Varying Material - SVBRDF

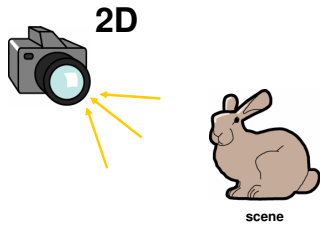


Computational Photography

Hendrik Lensch, Summer 2007

Digitizing Real-World Objects

taking a picture

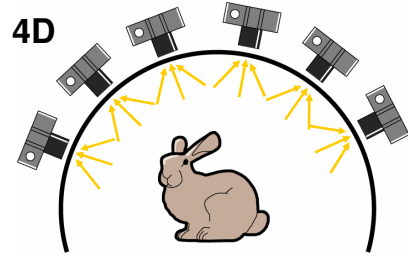


Computational Photography

Hendrik Lensch, Summer 2007

Light Field

[Gortler96], [Levoy96]

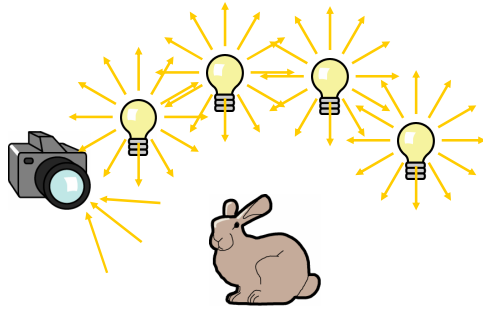


captures the distribution of all outgoing light rays

Computational Photography

Hendrik Lensch, Summer 2007

Relighting

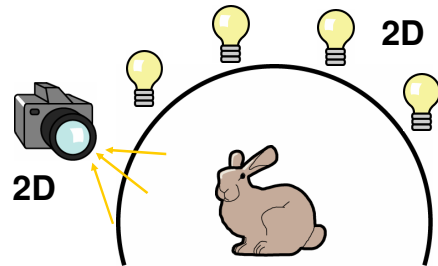


Computational Photography

Hendrik Lensch, Summer 2007

4D Reflectance Field

[Debevec2000]



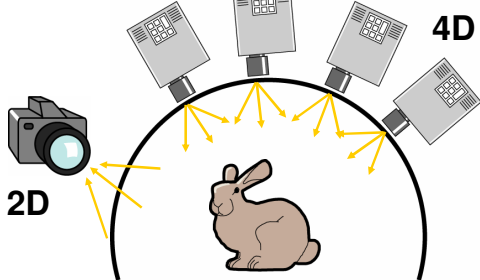
captures the scene for every light direction

Computational Photography

Hendrik Lensch, Summer 2007

6D Reflectance Field

[Masselus2003]

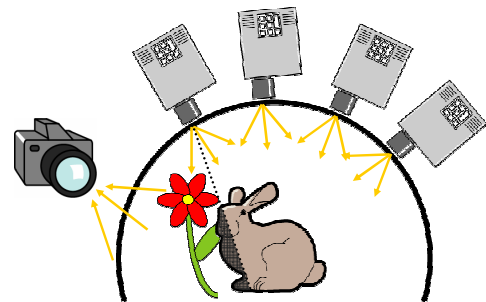


rendering with 4D incident light fields

Computational Photography

Hendrik Lensch, Summer 2007

6D Reflectance Field

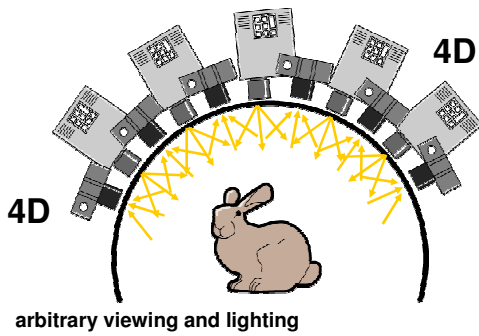


allows for projected light patterns, e.g. shadows

Computational Photography

Hendrik Lensch, Summer 2007

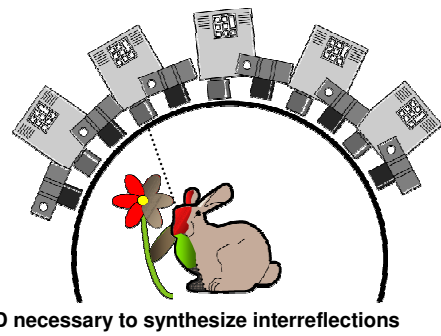
8D Reflectance Field



Computational Photography

Hendrik Lensch, Summer 2007

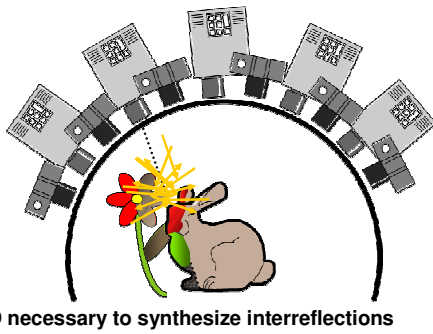
8D Reflectance Field



Computational Photography

Hendrik Lensch, Summer 2007

8D Reflectance Field



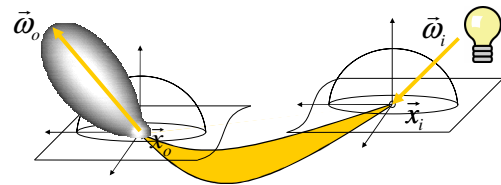
Computational Photography

Hendrik Lensch, Summer 2007

Definition – Reflectance Field

8D function

$$f_r((\vec{x}_i, \vec{\omega}_i) \rightarrow (\vec{x}_o, \vec{\omega}_o))$$



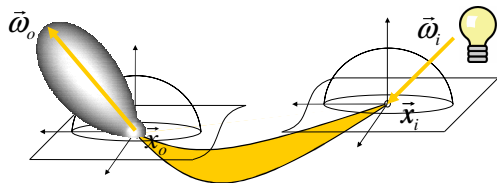
Computational Photography

Hendrik Lensch, Summer 2007

Definition – Reflectance Field

ratio of reflected radiance to incident flux

$$f_r((\vec{x}_i, \vec{\omega}_i) \rightarrow (\vec{x}_o, \vec{\omega}_o)) = \frac{dL_o(\vec{x}_o, \vec{\omega}_o)}{d\phi_i(\vec{x}_i, \vec{\omega}_i)}$$



Computational Photography

Hendrik Lensch, Summer 2007

Reflectance Field

Radiant light field from A under every possible incident field of illumination.

8 dimensional reflectance field function:

$$R = R(R_i; R_r) = R(u_i, v_i, \theta_i, \phi_i; u_r, v_r, \theta_r, \phi_r)$$

$R(u_i, v_i, \theta_i, \phi_i) \rightarrow$ incident light field arriving at A

$R(u_r, v_r, \theta_r, \phi_r) \rightarrow$ radiant light field leaving A

Computational Photography

Hendrik Lensch, Summer 2007

The Rendering Equation

[Kajiya et al. 1986]

$$L_o(\vec{x}_o, \vec{\omega}_o) = L_e(\vec{x}_o, \vec{\omega}_o) + \int_{A_i} \int_{\Omega_i} f_r((\vec{x}_i, \vec{\omega}_i) \rightarrow (\vec{x}_o, \vec{\omega}_o)) L_i(\vec{x}_i, \vec{\omega}_i) \cos \theta_i d\omega_i dx_i$$

How can we measure a reflectance field?

Computational Photography

Hendrik Lensch, Summer 2007



PROBLEM

data in... an 8D function

- using only 100 samples in each dimension
→ 10^{16} samples (12bytes/sample) = 109,139 TB
 - largest scanned 3D geometry: 10^8 points
- no solution for the full problem (yet)

Computational Photography

Hendrik Lensch, Summer 2007

Approaches

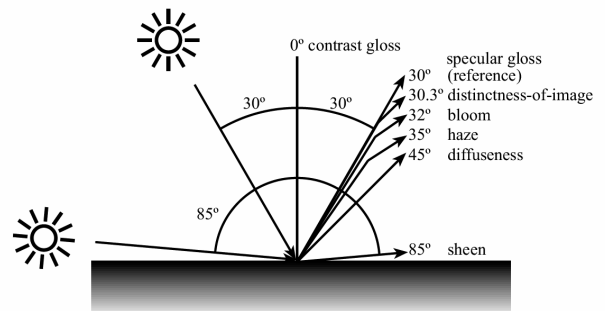
data is coherent in large parts
correlation

explore lower actual dimensionality of the data
restrict reflectance model
restrict viewing or illumination capabilities
adaptive parallel acquisition

Computational Photography

Hendrik Lensch, Summer 2007

Gloss Model



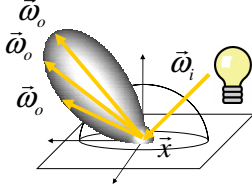
Computational Photography

Hendrik Lensch, Summer 2007

BRDF – 6D

(bidirectional reflectance distribution function)
ratio of reflected radiance to incident irradiance

$$f_r(\vec{x}; \vec{\omega}_i \rightarrow \vec{\omega}_o) = \frac{dL(\vec{x}, \vec{\omega}_o)}{dE(\vec{x}, \vec{\omega}_i)}$$



Computational Photography

Hendrik Lensch, Summer 2007

BRDF Models

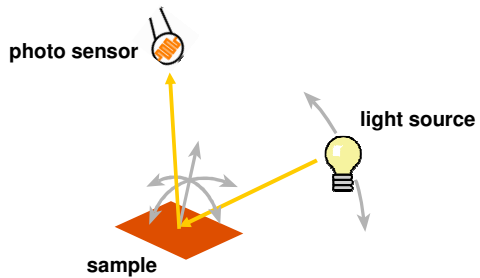
- tabulated
- analytic
- factorized
- spherical harmonics
- data-driven

Computational Photography

Hendrik Lensch, Summer 2007

4D-BRDF Measurement

Gonioreflectometer



Computational Photography

Hendrik Lensch, Summer 2007

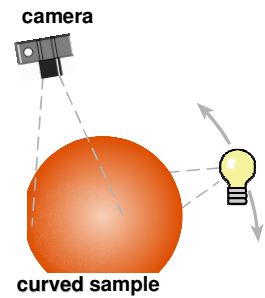
Image-Based BRDF Measurement

[Ward92], [Marschner99], [Lu&Koenderink99]

capture lots of
BRDF samples
at one shot by a
sensor array/camera

homogeneous
materials only!

How to get spatially
varying materials ?



Computational Photography

Hendrik Lensch, Summer 2007

Clustering of Materials



Computational Photography

Hendrik Lensch, Summer 2007

Spatially Varying Materials



Computational Photography

Hendrik Lensch, Summer 2007

Projection – good Title

goal: assign separate BRDF to each surface point

- too few reflectance samples for reliable fit
- represent the BRDF of each point by a weighted sum of basis BRDFs:

$$f_r(\vec{x}) = t_1 f_1 + t_2 f_2 + \dots + t_m f_m$$

- this is a *linear* problem

Computational Photography

Hendrik Lensch, Summer 2007

SBRDF - Results



Computational Photography

Hendrik Lensch, Summer 2007

SBRDF - Results

33 images, 2 hours → 120MB model

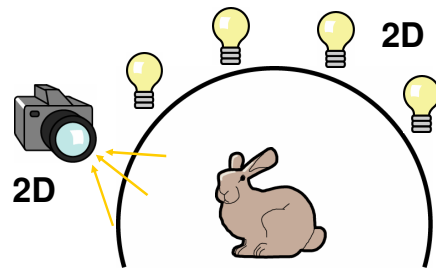


Computational Photography

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4D Reflectance Field

[Debevec2000]

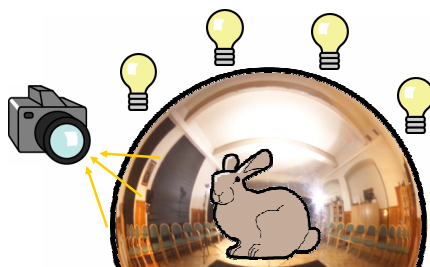


captures the scene for every light direction

Computational Photography

Hendrik Lensch, Summer 2007

4D Reflectance Field



allows for distant lights only

Computational Photography

Hendrik Lensch, Summer 2007

Light Stage



[Debevec2000]
single view point
assumes distant light sources
cannot relight with cast shadows

Computational Photography

Hendrik Lensch, Summer 2007

Performance Relighting

[Peers – SIGGRAPH 07]

video

Computational Photography

Hendrik Lensch, Summer 2007

Environment Matting

[Zongker et al. 1999]

Extension of Alpha Matting capable of capturing transparent and specular objects for one view.

Allows for reproduction with arbitrary backdrops.

A high-resolution 4D reflectance field.



Computational Photography

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Traditional Alpha Matte

$$C = F + (1 - \alpha)B$$

Composite color C

Foreground color F

Background color B

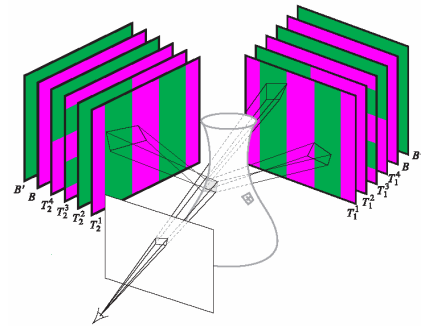
Pixel coverage α

Acquired by blue/green screening

Computational Photography

Hendrik Lensch, Summer 2007

Environment Matte Acquisition



Computational Photography

Hendrik Lensch, Summer 2007

Environment Matting Acquisition



Computational Photography

Hendrik Lensch, Summer 2007

Environment Matting Definition

Add reflected and refracted rays
(sum over backdrops)

$$C = F + (1 - \alpha)B + \sum_{i=1}^m R_i M(T_i, A_i)$$

Reflectance R

Texture T

Axis-aligned area A

Averaging operator $M(T, A)$

Computational Photography

Hendrik Lensch, Summer 2007

Environment Matte Extensions

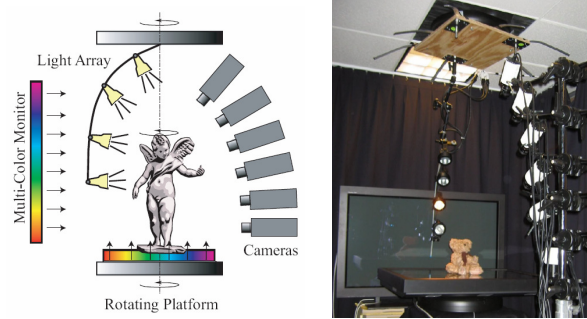
- Gaussian Filter kernel [Chuang et al. 2000]
- Real-time acquisition [Chuang et al. 2000]
- Wavelets in acquisition [Peers et al. 2003]
- Multiple View Points (Opacity hulls) [Matusik 2002]

Computational Photography

Hendrik Lensch, Summer 2007

Opacity Hulls [Matusik 2002]

combines Debevec's reflectance fields with environment mattes (~ 60,000 images).



Opacity Hulls [Matusik 2003]

combines Debevec's reflectance fields with environment mattes.



Computational Photography

Hendrik Lensch, Summer 2007

Bidirectional Texture Functions (BTFs)

[Dana et al. 1999]

- Reflectance field of a planar texture
- Replicated over a synthetic surface
- Captures shadowing and masking effects due to macro structure.
- (Tabulated Spatially Varying BRDF)
- No geometry at silhouettes

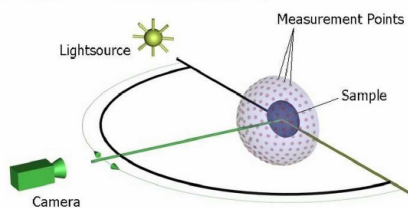
Computational Photography

Hendrik Lensch, Summer 2007

BTF Acquisition



[Sattler et al. 2003]



Computational Photography

Hendrik Lensch, Summer 2007

BTF Acquisition

Material sample



Computational Photography

Hendrik Lensch, Summer 2007

BTF - Rendering

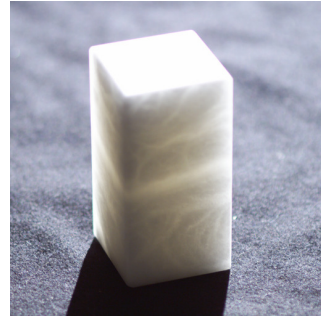


virtual prototyping [Gero Müller2005]

Computational Photography

Hendrik Lensch, Summer 2007

What about this?



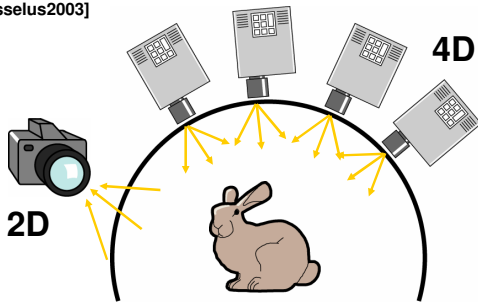
... requires per-ray measurements

Computational Photography

Hendrik Lensch, Summer 2007

6D Reflectance Field

[Masselus2003]



rendering with 4D incident light fields

Computational Photography

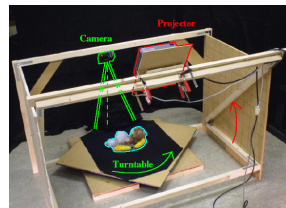
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Relighting with 4D Incident Light Fields



[Masselus2003]

6D reflectance field
spatially varying illumination
low resolution 16x16
~20 hours/acquisition

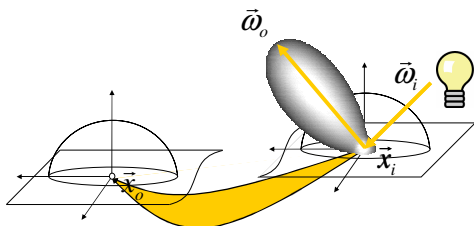


Computational Photography

Hendrik Lensch, Summer 2007

Subsurface Scattering

light penetrates the surface
light scatters inside the object



Computational Photography

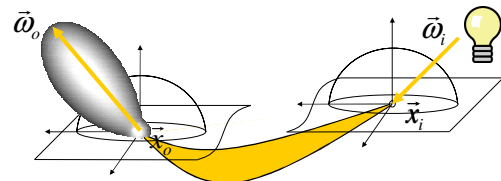
Hendrik Lensch, Summer 2007

BSSRDF - 8D

bidirectional scattering-surface reflectance distribution function [Nicodemus77]

= Reflectance Field

$$f_r((\vec{x}_i, \vec{\omega}_i) \rightarrow (\vec{x}_o, \vec{\omega}_o)) = \frac{dL_o(\vec{x}_o, \vec{\omega}_o)}{d\phi_i(\vec{x}_i, \vec{\omega}_i)}$$



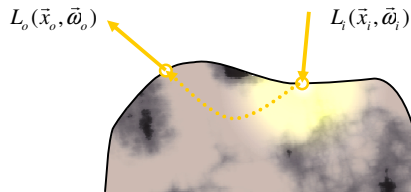
Computational Photography

Hendrik Lensch, Summer 2007

Modeling Translucent Objects

BSSRDF – 8D

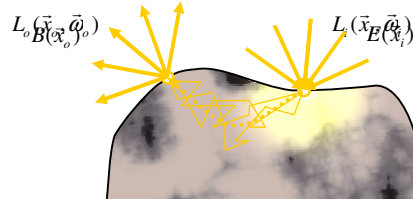
$$f_r((\vec{x}_i, \vec{\omega}_i) \rightarrow (\vec{x}_o, \vec{\omega}_o))$$



Diffuse Approximation

neglect directional dependence [Jensen 2001]

- frequent scattering events in optically dense media lead to diffuse scattering inside the media

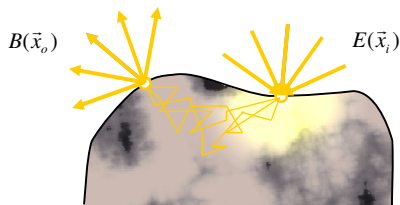


Diffuse Approximation

diffuse reflectance function

$$R_d(\vec{x}_i, \vec{x}_o)$$

- only 4 dimensions
- possible to acquire



Diffuse Reflectance Function R_d

discretize the surface

- enumerate all points on the surface
- vectors of irradiance E and radiosity B

represent R_d as matrix

- light transport or each pair of points
- linear transport

$$\begin{bmatrix} B_i \end{bmatrix} = \begin{bmatrix} R_d \end{bmatrix} \begin{bmatrix} E_j \end{bmatrix}$$

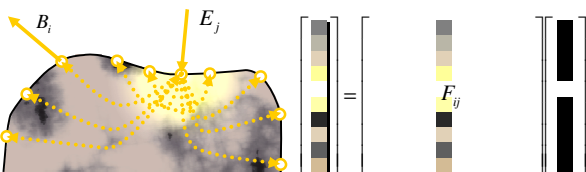
Computational Photography

Hendrik Lensch, Summer 2007

Key Idea

directly record F_{ij} for real objects

- illuminate individual surface points of an object
- record impulse response function
- results in a point-to-point throughput factor matrix



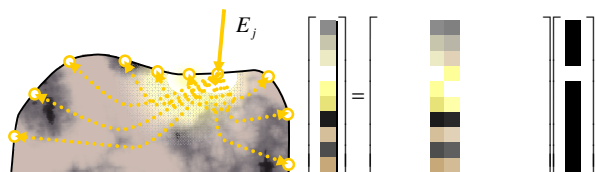
Computational Photography

Hendrik Lensch, Summer 2007

Key Idea

directly record R_d for real objects

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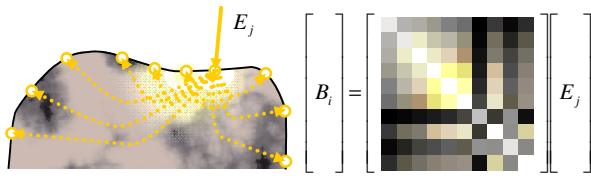
Computational Photography

Hendrik Lensch, Summer 2007

Key Idea

directly record R_d for real objects

- illuminate individual surface points of an object
- record impulse response function
- results in a point-to-point throughput factor matrix



Computational Photography

Hendrik Lensch, Summer 2007



Results



photograph

Computational Photography



rendering

Hendrik Lensch, Summer 2007

Results

[SIGGRAPH 2004]

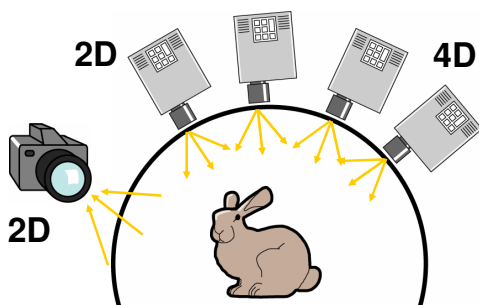
1,000,000 images, 22hours → 800MB model



Computational Photography

Hendrik Lensch, Summer 2007

Fixed View + Arbitrary Lighting



Computational Photography

Hendrik Lensch, Summer 2007

Approach

goals:

- no constraint on the type of scene
- high resolution

1,200,000 pictures for each projector

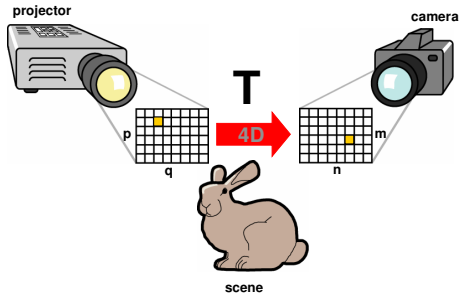
explore sparseness through adaptive multiplexed acquisition

exploit Helmholtz reciprocity

Computational Photography

Hendrik Lensch, Summer 2007

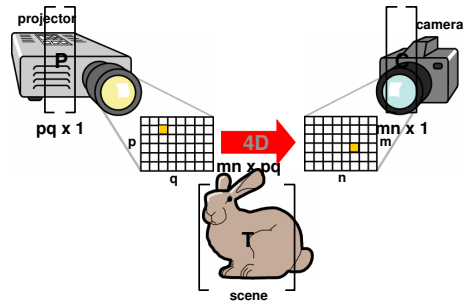
Pixel-to-Pixel Transport



Computational Photography

Hendrik Lensch, Summer 2007

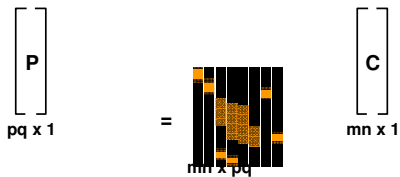
Mathematical Notation



Computational Photography

Hendrik Lensch, Summer 2007

Mathematical Notation



matrix properties

- little interreflection \leftrightarrow T rather sparse
- many interreflections \leftrightarrow T rather dense

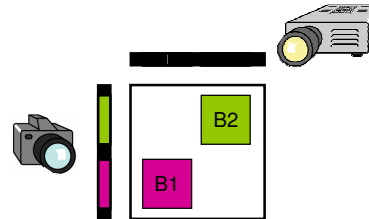
Computational Photography

Hendrik Lensch, Summer 2007

Adaptive Parallel Acquisition

assumption: sparse matrix

radiometrically independent blocks can be sensed in parallel

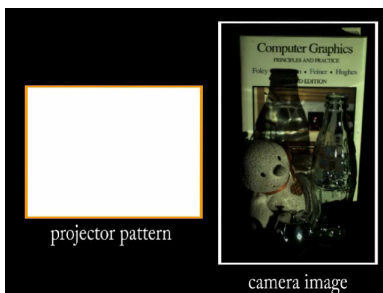


Computational Photography

Hendrik Lensch, Summer 2007

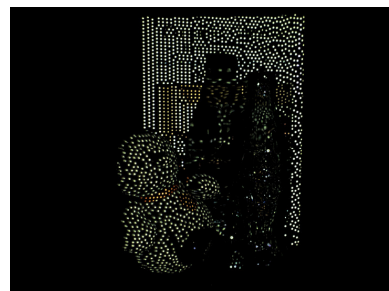
Adaptive Multiplexed Acquisition

parallel investigation if regions do not overlap in camera image



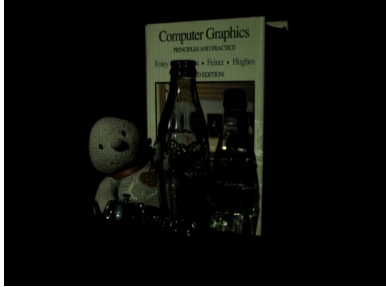
Adaptive Acquisition

parallel investigation if regions do not overlap in camera image



Relighting with 2D Patterns

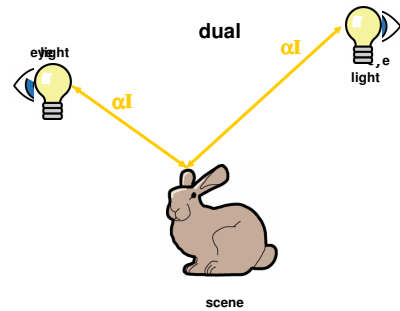
[SIGGRAPH 2005]



Computational Photography

Hendrik Lensch, Summer 2007

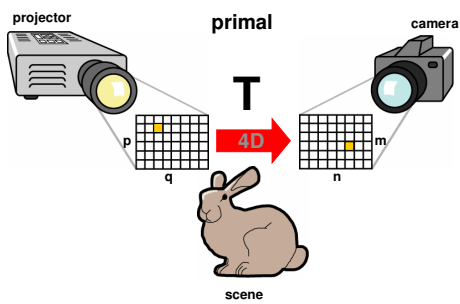
Helmholtz Reciprocity



Computational Photography

Hendrik Lensch, Summer 2007

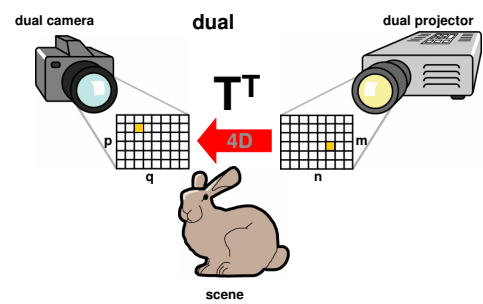
Dual Photography for Relighting



Computational Photography

Hendrik Lensch, Summer 2007

Dual Photography for Relighting

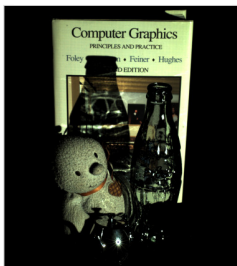


Computational Photography

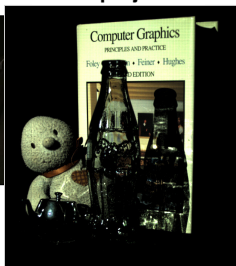
Hendrik Lensch, Summer 2007

Using the Transposed T Matrix

standard photograph
from camera



dual photograph
from projector



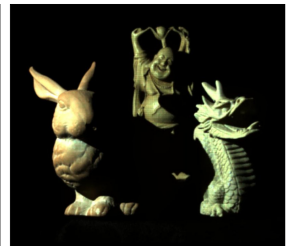
Computational Photography

Hendrik Lensch, Summer 2007

Sample Results



primal



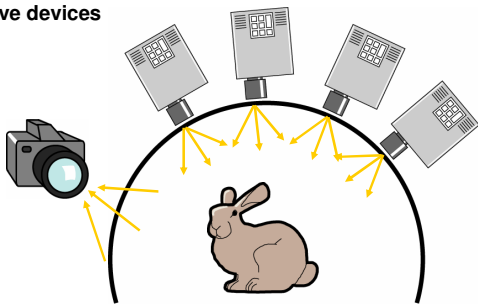
dual

Computational Photography

Hendrik Lensch, Summer 2007

Capturing 6D Reflectance Fields

active devices

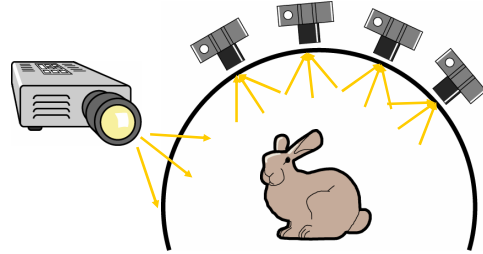


Computational Photography

Hendrik Lensch, Summer 2007

Dual Capture Process

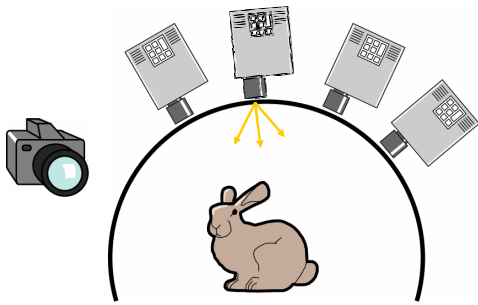
parallelization using passive devices



Computational Photography

Hendrik Lensch, Summer 2007

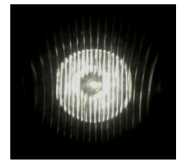
Light Source Interpolation [VMV2005]



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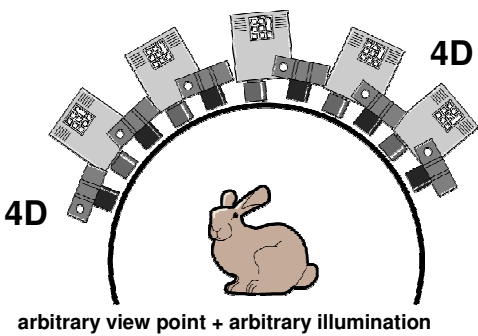
Relighting with 4D Incident Light Fields



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8D Reflectance Fields



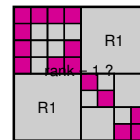
arbitrary view point + arbitrary illumination

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H-Matrices

[Hackbusch2000]



efficient representation of dense but data-sparse matrices

- subdivision hierarchy
- local low-rank approximation
- efficient evaluation

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Direct vs. Indirect Reflexions

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Direct vs. Indirect Reflexions

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Direct vs. Indirect Reflexions

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2D Slices through a Reflectance Field

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Symmetric Acquisition

symmetric 8th
rank-1 approximation from two images only
parallel acquisition of dense matrices

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Symmetric Exploration

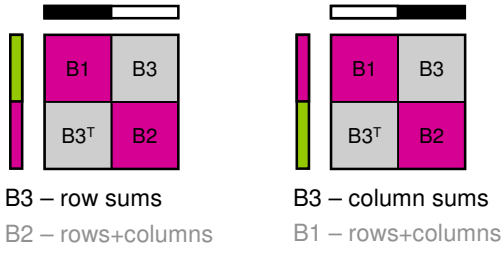
B3 – row sums
B2 – rows+columns

B3 – column sums
B1 – rows+columns

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Symmetric Exploration



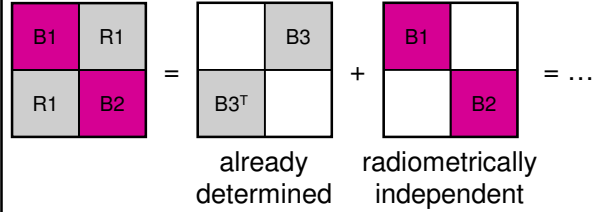
rank-1 approximation?



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Hierarchical Rank-1 Decomposition

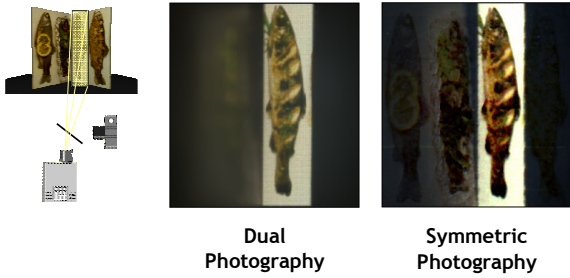


B1 and B2 are investigated in parallel.
parallel acquisition even for dense matrices

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Dual vs. Symmetric



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An 8D Reflectance Field

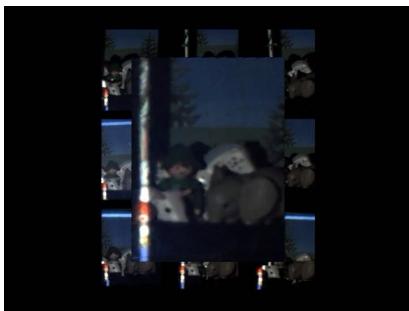
3.300 images, 6 hours → model – 1.4 GB



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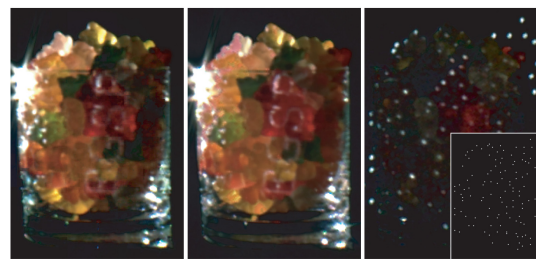
An 8D-Reflectance Field



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Virtual Photography



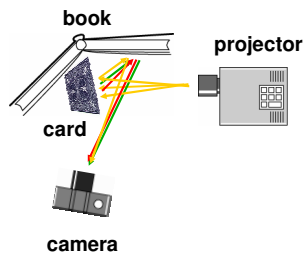
Computational Photography

[Garg, Talvala, Levoy, Lensch – EGSR 2006]

Card Experiment



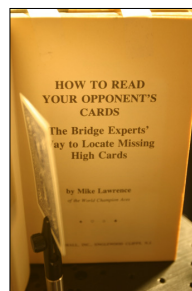
primal



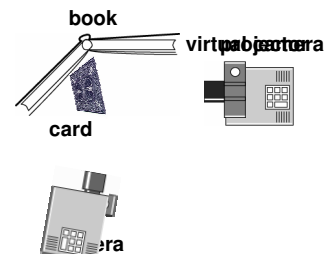
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Card Experiment



primal



virtual projector

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Card Experiment



primal



dual

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