



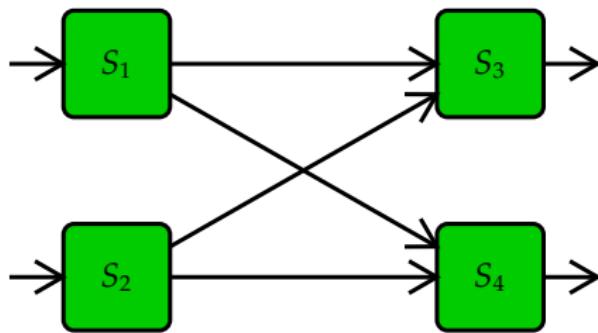
# Runtime Verification

Martin Leucker

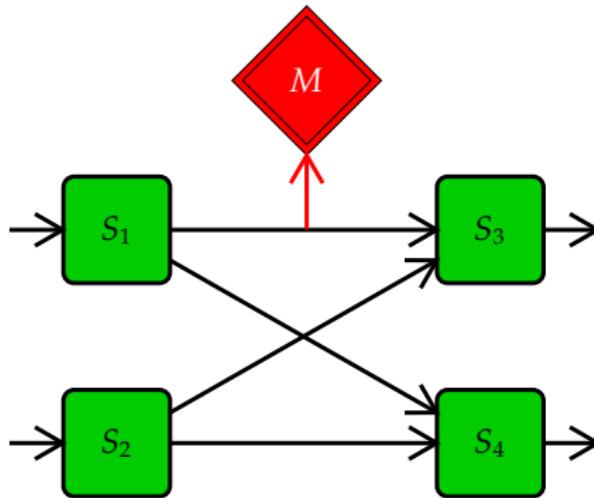
Institute for Software Engineering  
Universität zu Lübeck

VTSA 2023 - Runtime Verification

## Runtime Verification (RV)

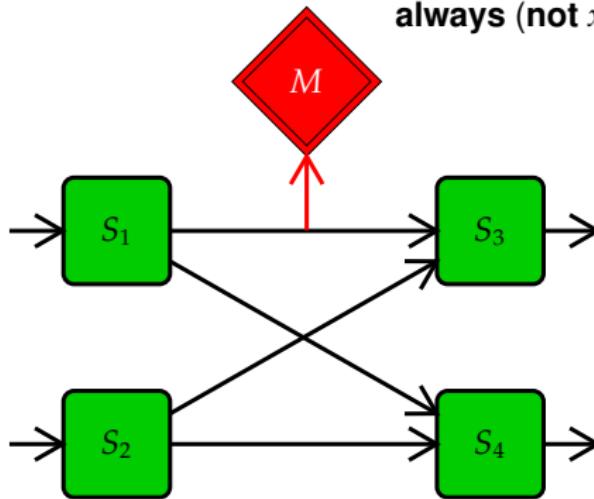


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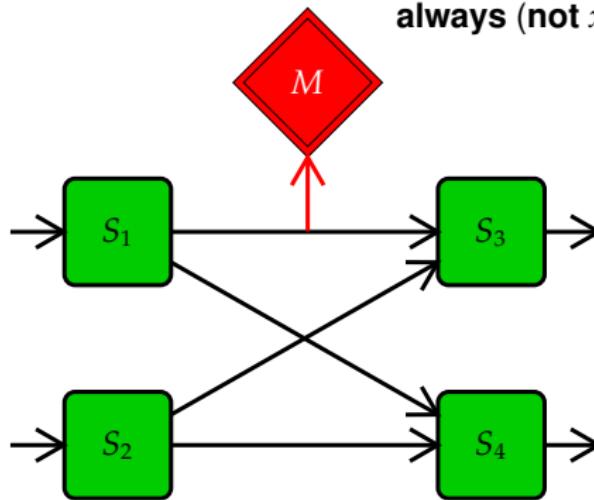


## Runtime Verification (RV)

**always (not  $x > 0$  implies next  $x > 0$ )**



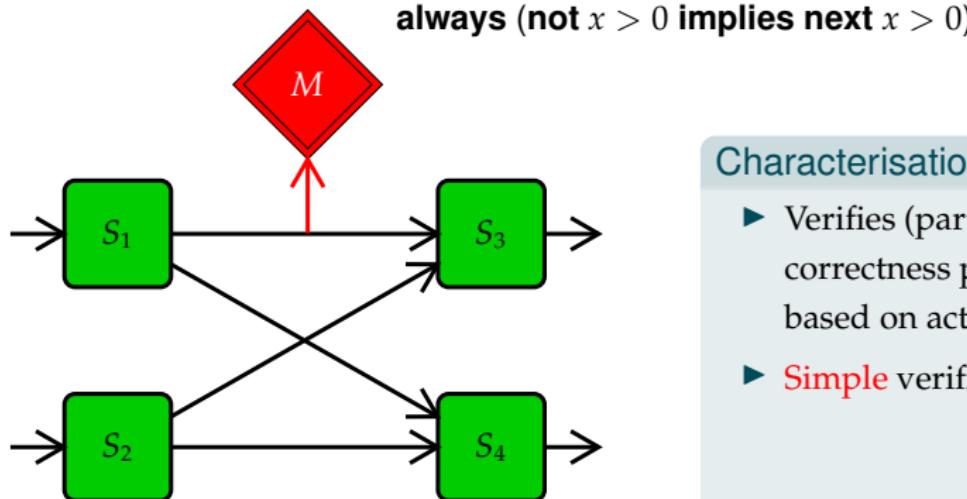
## Runtime Verification (RV)



### Characterisation

- ▶ Verifies (partially) correctness properties based on actual executions

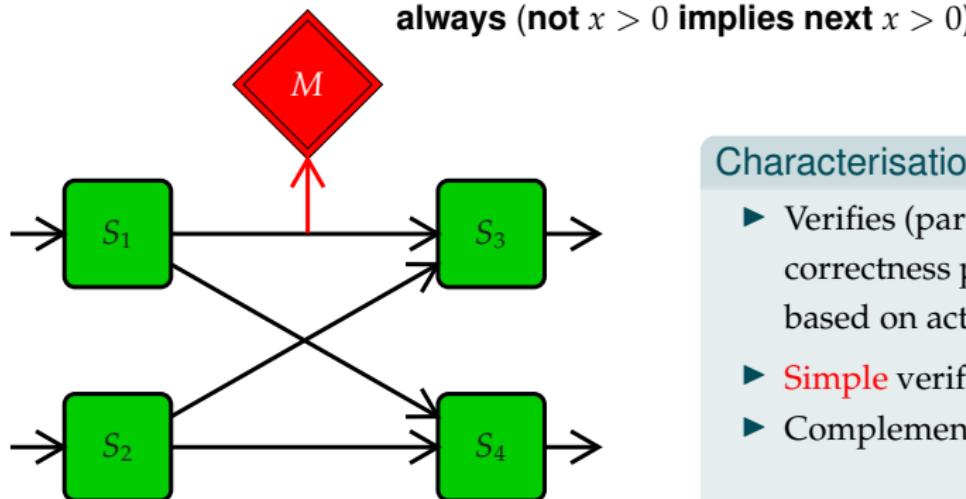
## Runtime Verification (RV)



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- ▶ Verifies (partially) correctness properties based on actual executions
- ▶ **Simple** verification technique

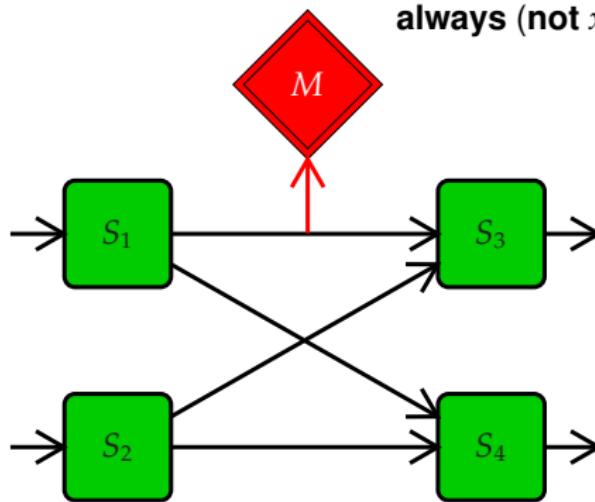
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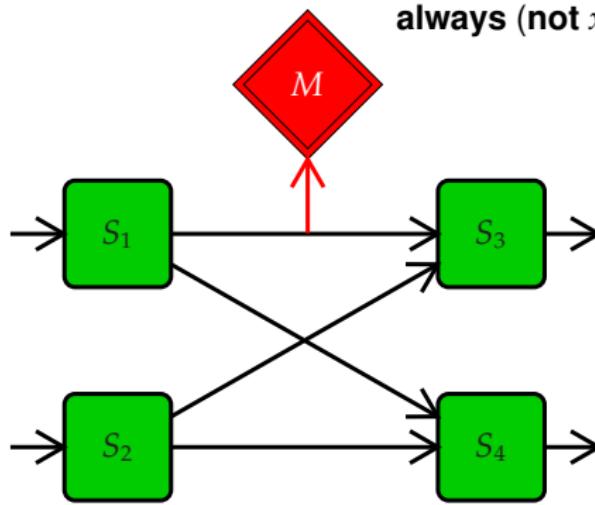
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- ▶ Complementing
  - ▶ Model Checking

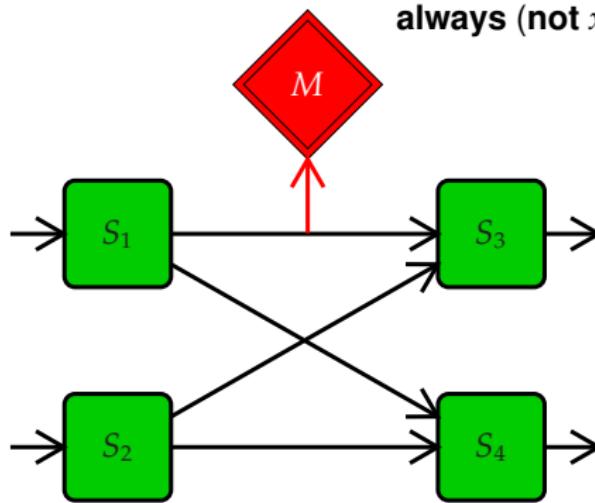
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  - ▶ Testing
- ▶ Formal:  $w \in \mathcal{L}(\varphi)$



# Model Checking

- ▶ Specification of System



# Model Checking

- ▶ Specification of System
  - ▶ as formula  $\varphi$  of linear-time temporal logic (LTL)



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**Do all runs of the system satisfy the specification**

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**Do all runs of the system satisfy the specification**
  - ▶  $\mathcal{L}(S) \subseteq \mathcal{L}(\varphi)$



## Model Checking versus RV

- Model Checking: infinite words



## Model Checking versus RV

- ▶ Model Checking: **infinite words**
- ▶ Runtime Verification: **finite words**



## Model Checking versus RV

- ▶ Model Checking: infinite words
- ▶ Runtime Verification: finite words
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- ▶ Runtime Verification: also **Black-Box-Systems**



## Testing

### Testing: Input/Output Sequence

- **incomplete** verification technique



## Testing

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### Testing: with Oracle

- ▶ **test case:** finite sequence of input actions
- ▶ **test oracle:** monitor
- ▶ **test execution:** send test cases, let oracle report violations
- ▶ **similar to runtime verification**



## Testing versus RV

- ▶ Test oracle **manual**



## Testing versus RV

- ▶ Test oracle **manual**
- ▶ RV monitor **from high-level specification (LTL)**



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- ▶ Test oracle **manual**
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## Testing versus RV

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*How to find good test suites?*
- ▶ Runtime Verification:  
*How to generate good monitors?*

## Outline

Runtime Verification

Runtime Verification for LTL

LTL over Finite, Completed Words

LTL over Finite, Non-Completed Words: Impartiality

LTL over Non-Completed Words: Anticipation

Monitorable Properties

RV-LTL

LTL with a Predictive Semantics

LTL wrap-up

Extensions

Monitoring Systems/Logging

Steering

RV frameworks

jUnit<sup>RV</sup> – Testing Temporal Properties

Motivating Example

jUnit<sup>RV</sup> – Idea

Using jUnit<sup>RV</sup>



## Presentation outline

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## Runtime Verification

### Definition (Runtime Verification)

**Runtime verification** is the discipline of computer science that deals with the study, development, and application of those verification techniques that allow checking whether a *run* of a system under scrutiny (SUS) satisfies or violates a given correctness property.

Its distinguishing research effort lies in *synthesizing monitors from high level specifications*.



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### Definition (Monitor)

A monitor is a device that reads a finite trace and yields a certain verdict.

A verdict is typically a truth value from some truth domain.

# Taxonomy



## Presentation outline

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### Runtime Verification for LTL

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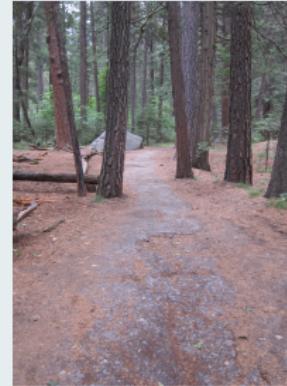
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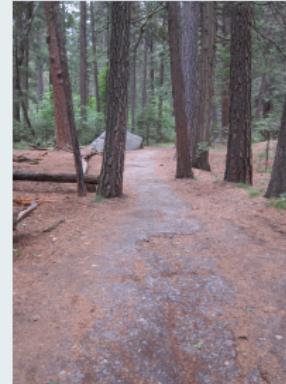
## Runtime Verification for LTL

### Observing executions/runs



## Runtime Verification for LTL

Observing executions/runs

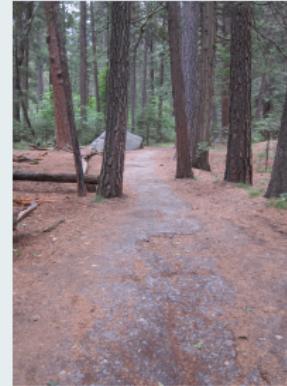


Idea

Specify correctness properties in LTL

## Runtime Verification for LTL

Observing executions/runs



### Idea

Specify correctness properties in LTL

### Commercial

Specify correctness properties in Regular LTL

## Runtime Verification for LTL

### Definition (Syntax of LTL formulae)

Let  $p$  be an atomic proposition from a finite set of atomic propositions AP. The set of LTL formulae, denoted with LTL, is inductively defined by the following grammar:

$$\begin{aligned}\varphi ::= & \quad true \mid p \mid \varphi \vee \varphi \mid \varphi U \varphi \mid X\varphi \mid \\ & false \mid \neg p \mid \varphi \wedge \varphi \mid \varphi R \varphi \mid \bar{X}\varphi \mid \\ & \neg \varphi\end{aligned}$$

## Linear-time Temporal Logic (LTL)

### Semantics

over  $w \in (2^{AP})^\omega = \Sigma^\omega$



## Linear-time Temporal Logic (LTL)

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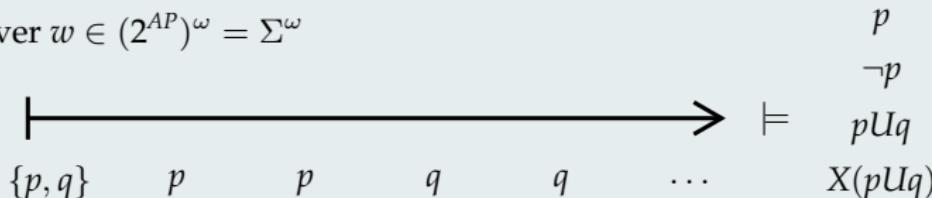
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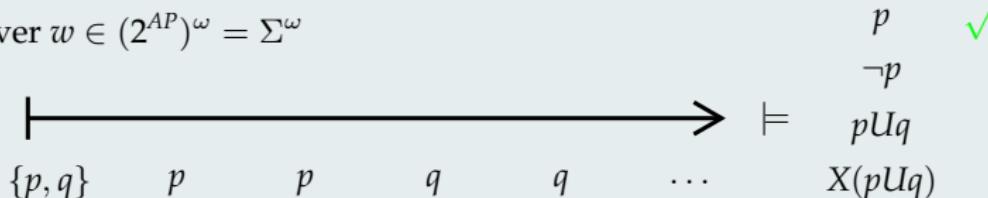
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{ $p, q$ }

$p$

$p$

$q$

$q$

...

$X(pUq)$



$\models$

$p$

✓

$\neg p$

✗

$pUq$

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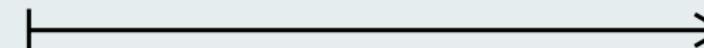
### Abbreviation

$$F\varphi \equiv \text{true} U \varphi \quad G\varphi \equiv \neg F \neg \varphi$$

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$p$	✓
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$\{p, q\}$

$p$

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$q$

...

### Abbreviation

$$F\varphi \equiv \text{true} U \varphi \quad G\varphi \equiv \neg F \neg \varphi$$

### Example

$$G \neg(critic_1 \wedge critic_2), G(\neg alive \rightarrow X alive)$$

## LTL on infinite words

### Definition (LTL semantics (traditional))

Semantics of LTL formulae over an infinite word  $w = a_0a_1 \dots \in \Sigma^\omega$ , where

$$w^i = a_i a_{i+1} \dots$$

$$w \models \text{true}$$

$$w \models p \quad \text{if } p \in a_0$$

$$w \models \neg p \quad \text{if } p \notin a_0$$

$$w \models \neg \varphi \quad \text{if not } w \models \varphi$$

$$w \models \varphi \vee \psi \quad \text{if } w \models \varphi \text{ or } w \models \psi$$

$$w \models \varphi \wedge \psi \quad \text{if } w \models \varphi \text{ and } w \models \psi$$

$$w \models X\varphi \quad \text{if } w^1 \models \varphi$$

$$w \models \bar{X}\varphi \quad \text{if } w^1 \models \varphi$$

$$w \models \varphi U \psi \quad \text{if there is } k \text{ with } 0 \leq k < |w|: w^k \models \psi$$

$$\text{and for all } l \text{ with } 0 \leq l < k w^l \models \varphi$$

$$w \models \varphi R \psi \quad \text{if for all } k \text{ with } 0 \leq k < |w|: (w^k \models \psi$$

$$\text{or there is } l \text{ with } 0 \leq l < k w^l \models \varphi)$$



## LTL for the working engineer??

Simple??

“LTL is for theoreticians—but for practitioners?”



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SALT

Structured Assertion Language for Temporal Logic

"Syntactic Sugar for LTL" [Bauer, L., Streit@ICFEM'06]



# SALT – <http://www.isp.uni-luebeck.de/salt>

The screenshot shows a web browser window with the following details:

- Title Bar:** SALT – Smart Assertion Language for Temporal Logic | ISP – Institute for Software Engineering and Programming Languages
- Address Bar:** isp <http://www.isp.uni-luebeck.de/salt>
- Search Bar:** Search
- Navigation Bar:** Apple, Yahoo!, Google Maps, YouTube, Wikipedia, News (1.257), Beliebt, Martin Leucker, Leo
- Right Side:** MY ACCOUNT, IMPRESS
- Header:** UNIVERSITY OF LÜBECK, INSTITUTE FOR SOFTWARE ENGINEERING AND PROGRAMMING LANGUAGES
- Footer:** NEWS, RESEARCH, TEACHING, STAFF, CONTACT

Home > Research > Projects >

## SALT - Smart Assertion Language for Temporal Logic

# SALT

### Goal

Do you want to specify the behavior of your program in a rigorously yet comfortable manner?  
Do you see the benefits of temporal specifications but are bothered by the awkward formalisms available?  
Do you want to use

- the power of a *Model Checker* to improve the quality of your systems or
- the powerful runtime reflection approach for bug hunting and elimination

## Runtime Verification for LTL

### Idea

Specify correctness properties in LTL

### Definition (Syntax of LTL formulae)

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## Truth Domains

### Lattice

- ▶ A **lattice** is a partially ordered set  $(\mathcal{L}, \sqsubseteq)$  where for each  $x, y \in \mathcal{L}$ , there exists
  1. a unique **greatest lower bound** (glb), which is called the **meet** of  $x$  and  $y$ , and is denoted with  $x \sqcap y$ , and
  2. a unique **least upper bound** (lub), which is called the **join** of  $x$  and  $y$ , and is denoted with  $x \sqcup y$ .
- ▶ A lattice is called **finite** iff  $\mathcal{L}$  is finite.
- ▶ Every finite lattice has a well-defined unique least element, called **bottom**, denoted with  $\perp$ ,
- ▶ and analogously a greatest element, called **top**, denoted with  $\top$ .

## Truth Domains (cont.)

### Lattice (cont.)

- ▶ A lattice is **distributive**, iff  $x \sqcap (y \sqcup z) = (x \sqcap y) \sqcup (x \sqcap z)$ , and, dually,  $x \sqcup (y \sqcap z) = (x \sqcup y) \sqcap (x \sqcup z)$ .
- ▶ In a **de Morgan** lattice, every element  $x$  has a unique **dual** element  $\bar{x}$ , such that  $\bar{\bar{x}} = x$  and  $x \sqsubseteq y$  implies  $\bar{y} \sqsubseteq \bar{x}$ .

### Definition (Truth domain)

We call  $\mathcal{L}$  a **truth domain**, if it is a finite distributive de Morgan lattice.

## LTL's semantics using truth domains

### Definition (LTL semantics (common part))

Semantics of LTL formulae over a finite or infinite word  $w = a_0 a_1 \dots \in \Sigma^\infty$

Boolean constants

Boolean combinations

$$\begin{array}{lll} [w \models \text{true}]_{\mathcal{L}} & = & \top \\ [w \models \text{false}]_{\mathcal{L}} & = & \perp \end{array} \quad \begin{array}{lll} [w \models \neg \varphi]_{\mathcal{L}} & = & \overline{[w \models \varphi]_{\mathcal{L}}} \\ [w \models \varphi \vee \psi]_{\mathcal{L}} & = & [w \models \varphi]_{\mathcal{L}} \sqcup [w \models \psi]_{\mathcal{L}} \\ [w \models \varphi \wedge \psi]_{\mathcal{L}} & = & [w \models \varphi]_{\mathcal{L}} \sqcap [w \models \psi]_{\mathcal{L}} \end{array}$$

atomic propositions

$$[w \models p]_{\mathcal{L}} = \begin{cases} \top & \text{if } p \in a_0 \\ \perp & \text{if } p \notin a_0 \end{cases} \quad [w \models \neg p]_{\mathcal{L}} = \begin{cases} \top & \text{if } p \notin a_0 \\ \perp & \text{if } p \in a_0 \end{cases}$$

next X/weak next X TBD

until/release

$$\begin{array}{lll} [w \models \varphi U \psi]_{\mathcal{L}} & = & \begin{cases} \top & \text{there is a } k, 0 \leq k < |w| : [w^k \models \psi]_{\mathcal{L}} = \top \text{ and} \\ & \text{for all } l \text{ with } 0 \leq l < k : [w^l \models \varphi]_{\mathcal{L}} = \top \\ \text{TBD} & \text{else} \end{cases} \\ \varphi R \psi & \equiv & \neg(\neg \varphi U \neg \psi) \end{array}$$



## Outline

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### Runtime Verification for LTL

LTL over Finite, Completed Words

LTL over Finite, Non-Completed Words: Impartiality

LTL over Non-Completed Words: Anticipation

Monitorable Properties

RV-LTL

LTL with a Predictive Semantics

LTL wrap-up

Extensions

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Steering

RV frameworks

jUnit<sup>RV</sup> – Testing Temporal Properties

Motivating Example

jUnit<sup>RV</sup> – Idea

Using jUnit<sup>RV</sup>

## LTL on finite words

Application area: Specify properties of finite word



## LTL on finite words

### Definition (FLTL)

Semantics of FLTL formulae over a word  $u = a_0 \dots a_{n-1} \in \Sigma^*$

next

$$[u \models X\varphi]_F = \begin{cases} [u^1 \models \varphi]_F & \text{if } u^1 \neq \epsilon \\ \perp & \text{otherwise} \end{cases}$$

weak next

$$[u \models \bar{X}\varphi]_F = \begin{cases} [u^1 \models \varphi]_F & \text{if } u^1 \neq \epsilon \\ \top & \text{otherwise} \end{cases}$$



## Monitoring LTL on finite words

(Bad) Idea

just compute semantics...



## Outline

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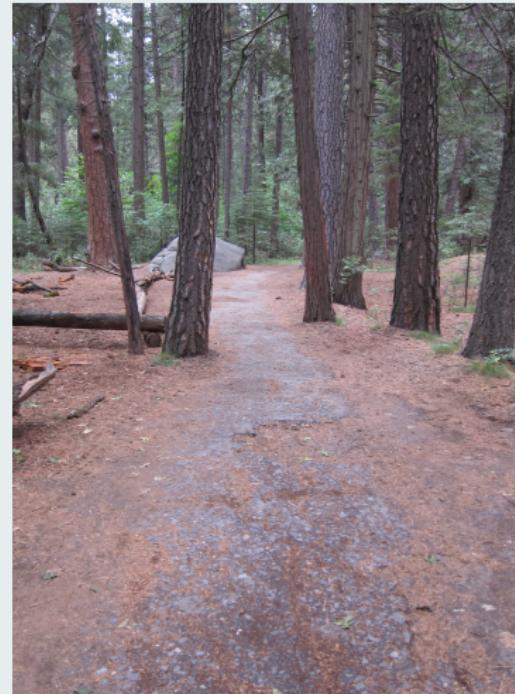
Motivating Example

jUnit<sup>RV</sup> – Idea

Using jUnit<sup>RV</sup>

## LTL on finite, but not completed words

Application area: Specify properties of finite but expanding word





## LTL on finite, but not completed words

### Be Impartial!

- ▶ go for a final verdict ( $\top$  or  $\perp$ ) only if you really know



## LTL on finite, but not completed words

### Be Impartial!

- ▶ go for a final verdict ( $\top$  or  $\perp$ ) only if you really know
- ▶ *stick to your word*

## LTL on finite, but not complete words

Impartiality implies multiple values

Every two-valued logic is not impartial.

### Definition (FLTL<sub>4</sub>)

Semantics of FLTL formulae over a word  $u = a_0 \dots a_{n-1} \in \Sigma^*$

next

$$[u \models X\varphi]_4 = \begin{cases} [u^1 \models \varphi]_4 & \text{if } u^1 \neq \epsilon \\ \perp^p & \text{otherwise} \end{cases}$$

weak next

$$[u \models \bar{X}\varphi]_4 = \begin{cases} [u^1 \models \varphi]_4 & \text{if } u^1 \neq \epsilon \\ \top^p & \text{otherwise} \end{cases}$$

## Monitoring LTL on finite but expanding words

Left-to-right!



## Monitoring LTL on finite but expanding words

### Rewriting

Idea: Use rewriting of formula

### Evaluating FTL4 for each subsequent letter

- ▶ evaluate atomic propositions
- ▶ evaluate next-formulas
- ▶ that's it thanks to

$$\varphi U \psi \equiv \psi \vee (\varphi \wedge X\varphi U \psi)$$

and

$$\varphi R \psi \equiv \psi \wedge (\varphi \vee \bar{X}\varphi R \psi)$$

- ▶ and remember what to evaluate for the next letter

## Evaluating FLTL4 for each subsequent letter

### Pseudo Code

```
evalFLTL4 true    a = (T, T)
evalFLTL4 false   a = (⊥, ⊥)
evalFLTL4 p       a = ((p in a), (p in a))
evalFLTL4 ¬φ     a = let (valPhi, phiRew) = evalFLTL4 φ a
                  in (valPhi, ¬phiRew)
evalFLTL4 φ ∨ ψ   a = let
                  (valPhi, phiRew) = evalFLTL4 φ a
                  (valPsi, psiRew) = evalFLTL4 ψ a
                  in (valPhi ∪ valPsi, phiRew ∨ psiRew)
evalFLTL4 φ ∧ ψ   a = let
                  (valPhi, phiRew) = evalFLTL4 φ a
                  (valPsi, psiRew) = evalFLTL4 ψ a
                  in (valPhi ∩ valPsi, phiRew ∧ psiRew)
evalFLTL4 φ U ψ   a = evalFLTL4 ψ ∨ (φ ∧ X(φ U ψ)) a
evalFLTL4 φ R ψ   a = evalFLTL4 ψ ∧ (φ ∨ X(φ R ψ)) a
evalFLTL4 Xφ     a = (⊥p, φ)
evalFLTL4 X̄φ    a = (Tp, φ)
```



## Monitoring LTL on finite but expanding words

### Automata-theoretic approach

- ▶ Synthesize automaton
- ▶ Monitoring = stepping through automaton

## Rewriting vs. automata

### Rewriting function defines transition function

```
evalFLTL4 true    a = ( $\top$ , true)
evalFLTL4 false   a = ( $\perp$ , false)
evalFLTL4 p       a = ((p in a), (p in a) ? true : false)
evalFLTL4  $\neg\varphi$  a = let (valPhi, phiRew) = evalFLTL4  $\varphi$  a
                      in (valPhi,  $\neg$ phiRew)
evalFLTL4  $\varphi \vee \psi$  a = let
                           (valPhi, phiRew) = evalFLTL4  $\varphi$  a
                           (valPsi, psiRew) = evalFLTL4  $\psi$  a
                           in (valPhi  $\sqcup$  valPsi, phiRew  $\vee$  psiRew)
evalFLTL4  $\varphi \wedge \psi$  a = let
                           (valPhi, phiRew) = evalFLTL4  $\varphi$  a
                           (valPsi, psiRew) = evalFLTL4  $\psi$  a
                           in (valPhi  $\sqcap$  valPsi, phiRew  $\wedge$  psiRew)
evalFLTL4  $\varphi U \psi$  a = evalFLTL4  $\psi \vee (\varphi \wedge X(\varphi U \psi))$  a
evalFLTL4  $\varphi R \psi$  a = evalFLTL4  $\psi \wedge (\varphi \vee \bar{X}(\varphi R \psi))$  a
evalFLTL4  $X\varphi$     a = ( $\perp^p$ ,  $\varphi$ )
evalFLTL4  $\bar{X}\varphi$   a = ( $\top^p$ ,  $\varphi$ )
```



## Automata-theoretic approach

### The roadmap

- ▶ alternating Mealy machines



## Automata-theoretic approach

### The roadmap

- ▶ alternating Mealy machines
- ▶ Moore machines



## Automata-theoretic approach

### The roadmap

- ▶ alternating Mealy machines
- ▶ Moore machines
- ▶ alternating machines



## Automata-theoretic approach

### The roadmap

- ▶ alternating Mealy machines
- ▶ Moore machines
- ▶ alternating machines
- ▶ non-deterministic machines



## Automata-theoretic approach

### The roadmap

- ▶ alternating Mealy machines
- ▶ Moore machines
- ▶ alternating machines
- ▶ non-deterministic machines
- ▶ deterministic machines



## Automata-theoretic approach

### The roadmap

- ▶ alternating Mealy machines
- ▶ Moore machines
- ▶ alternating machines
- ▶ non-deterministic machines
- ▶ deterministic machines
- ▶ state sequence for an input word

## Supporting alternating finite-state machines

### Definition (Alternating Mealy Machine)

A **alternating Mealy machine** is a tupel  $\mathcal{M} = (Q, \Sigma, \Gamma, q_0, \delta)$  where

- ▶  $Q$  is a finite set of **states**,
- ▶  $\Sigma$  is the **input alphabet**,
- ▶  $\Gamma$  is a finite, distributive lattice, the **output lattice**,
- ▶  $q_0 \in Q$  is the **initial state** and
- ▶  $\delta : Q \times \Sigma \rightarrow B^+(\Gamma \times Q)$  is the **transition function**

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### Convention

Understand  $\delta : Q \times \Sigma \rightarrow B^+(\Gamma \times Q)$  as a function  $\delta : Q \times \Sigma \rightarrow \Gamma \times B^+(Q)$

## Supporting alternating finite-state machines

### Definition (Run of an Alternating Mealy Machine)

A **run** of an alternating Mealy machine  $\mathcal{M} = (Q, \Sigma, \Gamma, q_0, \delta)$  on a finite word  $u = a_0 \dots a_{n-1} \in \Sigma^+$  is a sequence  $t_0 \xrightarrow{(a_0, b_0)} t_1 \xrightarrow{(a_1, b_1)} \dots t_{n-1} \xrightarrow{(a_{n-1}, b_{n-1})} t_n$  such that

- ▶  $t_0 = q_0$  and
- ▶  $(t_i, b_{i-1}) = \hat{\delta}(t_{i-1}, a_{i-1})$

where  $\hat{\delta}$  is inductively defined as follows

- ▶  $\hat{\delta}(q, a) = \delta(q, a),$
- ▶  $\hat{\delta}(q \vee q', a) = (\hat{\delta}(q, a)|_1 \sqcup \hat{\delta}(q', a)|_1, \hat{\delta}(q, a)|_2 \vee \hat{\delta}(q', a)|_2),$  and
- ▶  $\hat{\delta}(q \wedge q', a) = (\hat{\delta}(q, a)|_1 \sqcap \hat{\delta}(q', a)|_1, \hat{\delta}(q, a)|_2 \wedge \hat{\delta}(q', a)|_2)$

The **output** of the run is  $b_{n-1}.$

## Transition function of an alternating Mealy machine

Transition function  $\delta_4^a : Q \times \Sigma \rightarrow B^+(\Gamma \times Q)$

$$\delta_4^a(true, a) = (\top, true)$$

$$\delta_4^a(false, a) = (\perp, false)$$

$$\delta_4^a(p, a) = (p \in a, [p \in a])$$

$$\delta_4^a(\varphi \vee \psi, a) = \delta_4^a(\varphi, a) \vee \delta_4^a(\psi, a)$$

$$\delta_4^a(\varphi \wedge \psi, a) = \delta_4^a(\varphi, a) \wedge \delta_4^a(\psi, a)$$

$$\begin{aligned}\delta_4^a(\varphi U \psi, a) &= \delta_4^a(\psi \vee (\varphi \wedge X(\varphi U \psi)), a) \\ &= \delta_4^a(\psi, a) \vee (\delta_4^a(\varphi, a) \wedge (\varphi U \psi))\end{aligned}$$

$$\begin{aligned}\delta_4^a(\varphi R \psi, a) &= \delta_4^a(\psi \wedge (\varphi \vee \bar{X}(\varphi R \psi)), a) \\ &= \delta_4^a(\psi, a) \wedge (\delta_4^a(\varphi, a) \vee (\varphi R \psi))\end{aligned}$$

$$\delta_4^a(X\varphi, a) = (\perp^p, \varphi)$$

$$\delta_4^a(\bar{X}\varphi, a) = (\top^p, \varphi)$$

## Outline

Runtime Verification

### Runtime Verification for LTL

LTL over Finite, Completed Words

LTL over Finite, Non-Completed Words: Impartiality

**LTL over Non-Completed Words: Anticipation**

Monitorable Properties

RV-LTL

LTL with a Predictive Semantics

LTL wrap-up

Extensions

Monitoring Systems/Logging

Steering

RV frameworks

jUnit<sup>RV</sup> – Testing Temporal Properties

Motivating Example

jUnit<sup>RV</sup> – Idea

Using jUnit<sup>RV</sup>

## Anticipatory Semantics

Consider possible extensions of the non-completed word





## LTL for RV [BLS@FSTTCS'06]

### Basic idea

- ▶ LTL over infinite words is commonly used for specifying correctness properties
- ▶ finite words in RV:  
prefixes of infinite, so-far unknown words
- ▶ **re-use existing semantics**

## LTL for RV [BLS@FSTTCS'06]

### Basic idea

- ▶ LTL over infinite words is commonly used for specifying correctness properties
- ▶ finite words in RV:  
prefixes of infinite, so-far unknown words
- ▶ re-use existing semantics

### 3-valued semantics for LTL over finite words

$$[u \models \varphi] = \begin{cases} \top & \text{if } \forall \sigma \in \Sigma^\omega : u\sigma \models \varphi \\ \perp & \text{if } \forall \sigma \in \Sigma^\omega : u\sigma \not\models \varphi \\ ? & \text{else} \end{cases}$$



# Impartial Anticipation

## Impartial

- ▶ Stay with  $\top$  and  $\perp$

## Impartial Anticipation

### Impartial

- ▶ Stay with  $\top$  and  $\perp$

### Anticipatory

- ▶ Go for  $\top$  or  $\perp$
- ▶ Consider  $XXX\text{false}$

$$\epsilon \models XXX\text{false}$$

## Impartial Anticipation

### Impartial

- ▶ Stay with  $\top$  and  $\perp$

### Anticipatory

- ▶ Go for  $\top$  or  $\perp$
- ▶ Consider  $XXX\text{false}$

$$\epsilon \models XXX\text{false}$$

$$a \models XX\text{false}$$

## Impartial Anticipation

### Impartial

- ▶ Stay with  $\top$  and  $\perp$

### Anticipatory

- ▶ Go for  $\top$  or  $\perp$
- ▶ Consider  $XXX\text{false}$

$$\epsilon \models XXX\text{false}$$

$$a \models XX\text{false}$$

$$aa \models X\text{false}$$

## Impartial Anticipation

### Impartial

- ▶ Stay with  $\top$  and  $\perp$

### Anticipatory

- ▶ Go for  $\top$  or  $\perp$
- ▶ Consider  $XXX\text{false}$

$$\epsilon \models XXX\text{false}$$

$$a \models XX\text{false}$$

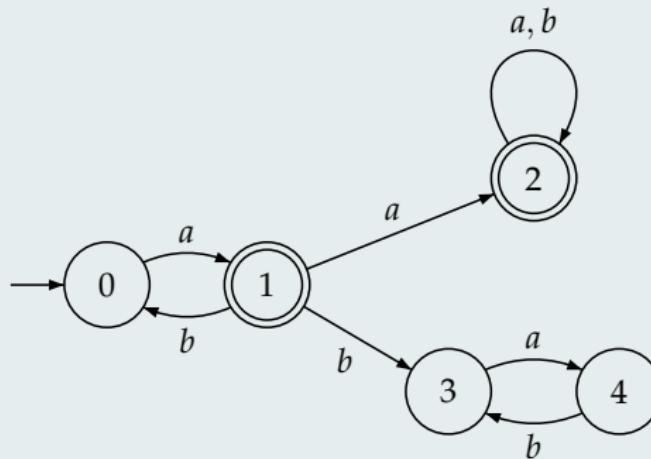
$$aa \models X\text{false}$$

$$aaa \models \text{false}$$

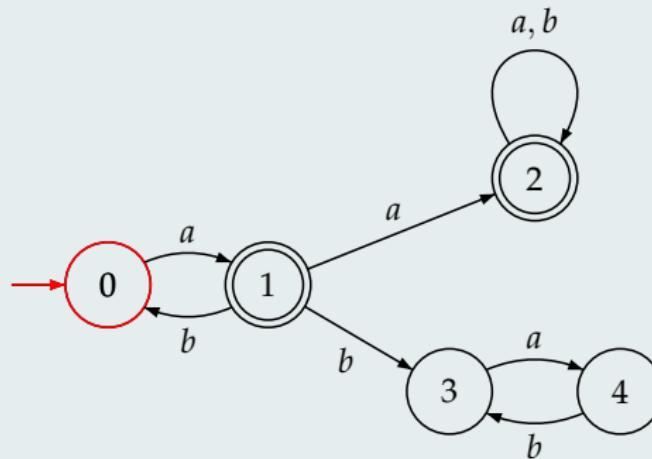
$$[\epsilon \models XXX\text{false}] = \begin{cases} \top & \text{if } \forall \sigma \in \Sigma^\omega : \epsilon\sigma \models XXX\text{false} \\ \perp & \text{if } \forall \sigma \in \Sigma^\omega : \epsilon\sigma \not\models XXX\text{false} \\ ? & \text{else} \end{cases}$$



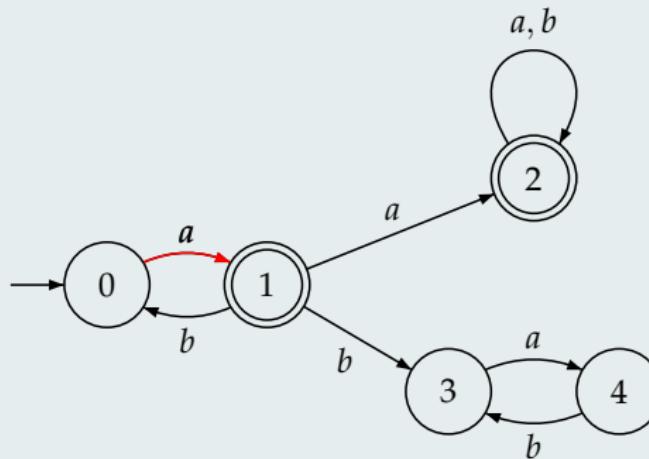
## Büchi automata (BA)



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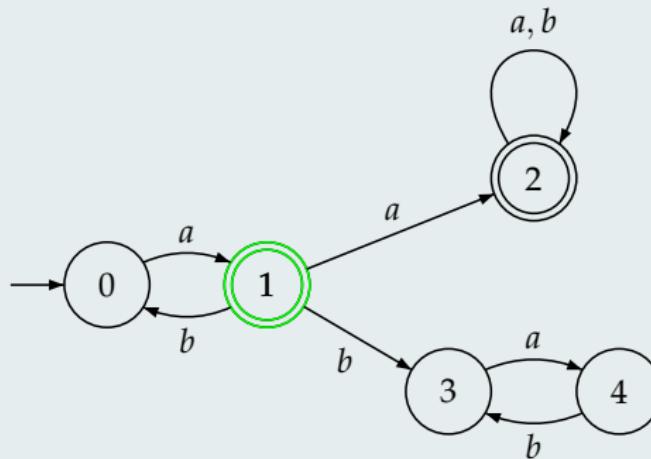


## Büchi automata (BA)



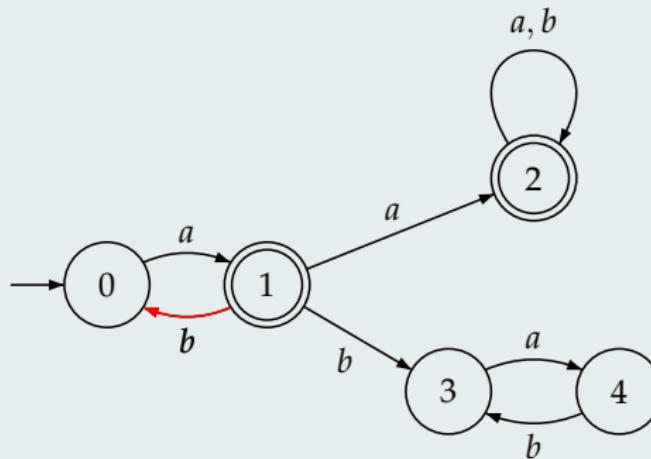
a

## Büchi automata (BA)



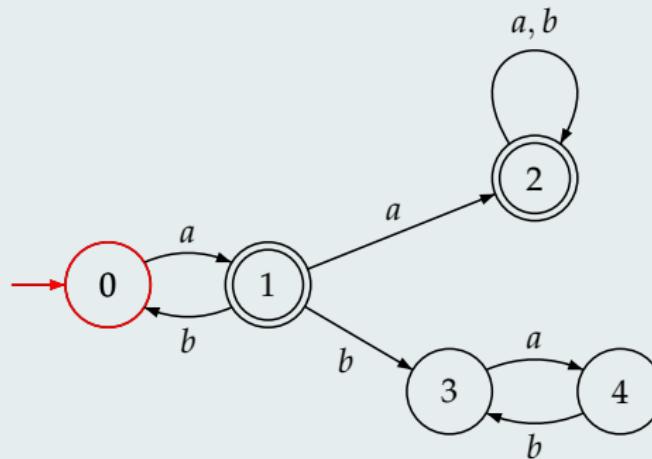
$a$

## Büchi automata (BA)



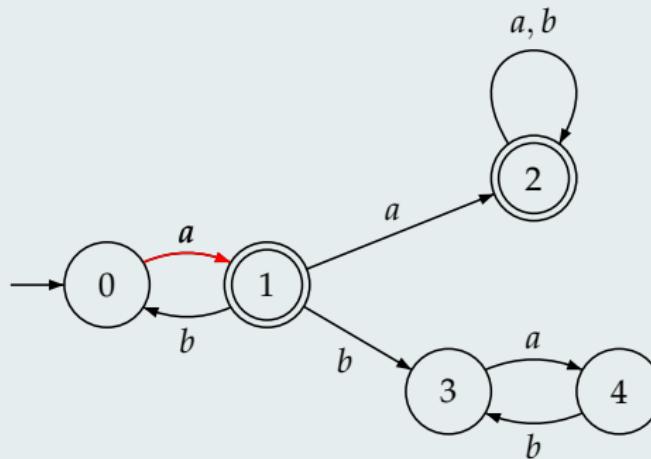
$a\ b$

## Büchi automata (BA)



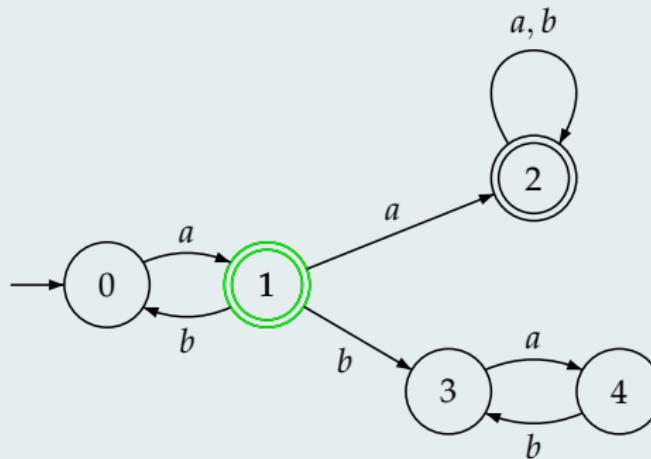
a b

## Büchi automata (BA)



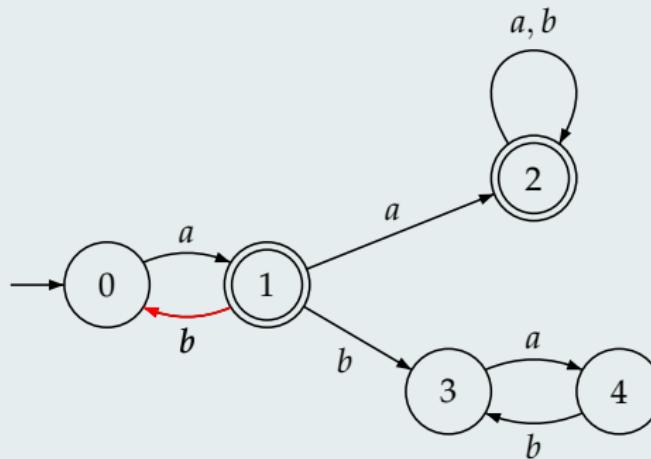
$a\ b\ a$

## Büchi automata (BA)



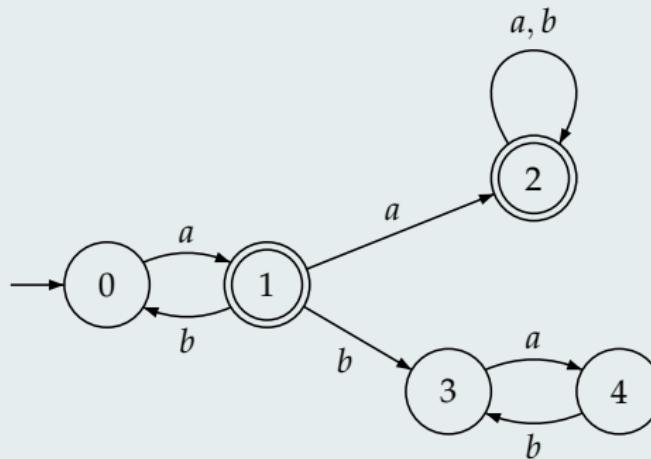
a b a

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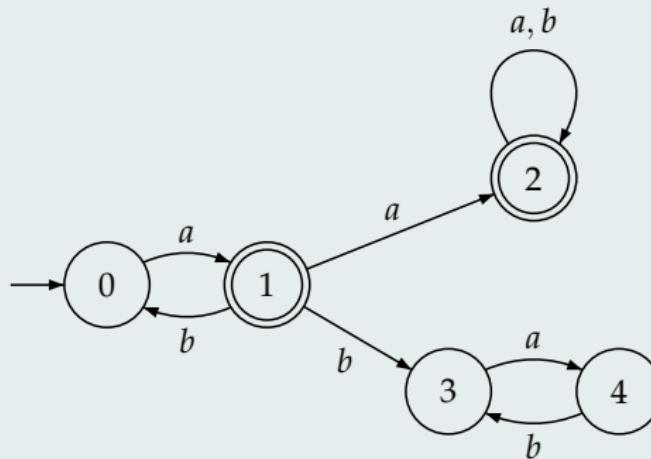
a b a b

## Büchi automata (BA)



a b a b ...

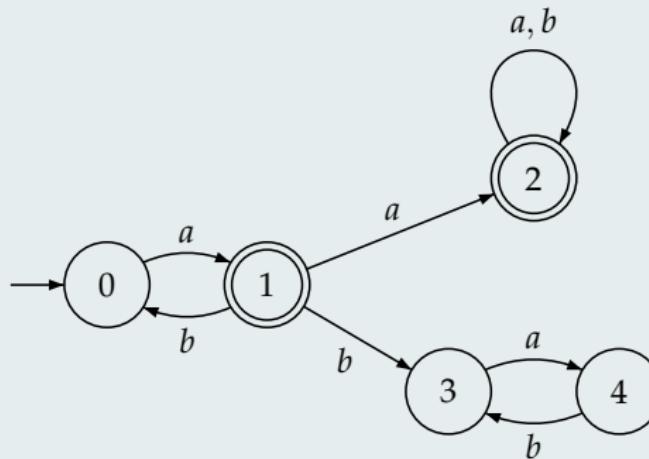
## Büchi automata (BA)



$a\ b\ a\ b\ \dots$

$(ab)^\omega \in \mathcal{L}(\mathcal{A})$

## Büchi automata (BA)



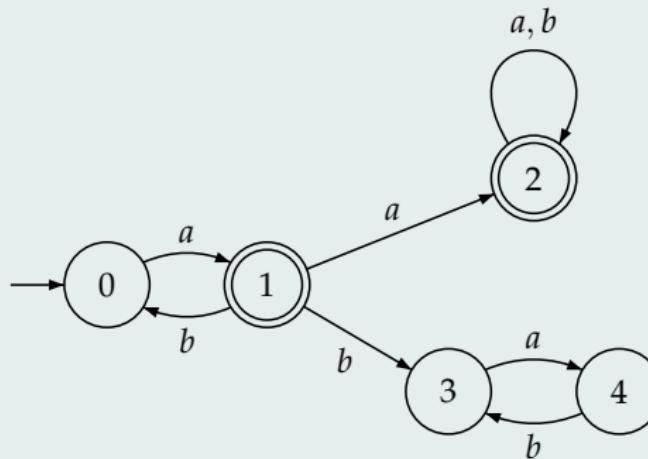
a b a b ...

$(ab)^\omega \in \mathcal{L}(\mathcal{A})$

$(ab)^* aa \{a, b\}^\omega \subseteq \mathcal{L}(\mathcal{A})$

## Büchi automata (BA)

Emptiness test:



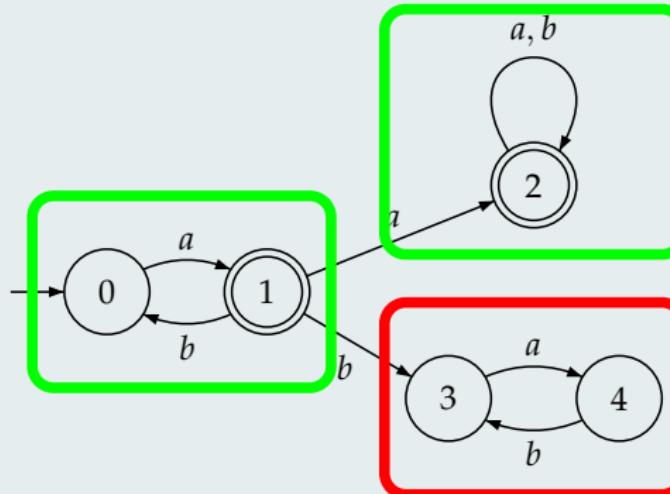
a b a b ...

$$(ab)^\omega \in \mathcal{L}(\mathcal{A})$$

$$(ab)^* aa \{a, b\}^\omega \subseteq \mathcal{L}(\mathcal{A})$$

## Büchi automata (BA)

Emptiness test: SCCC, Tarjan



$a b a b \dots$

$$(ab)^\omega \in \mathcal{L}(\mathcal{A})$$

$$(ab)^* aa \{a, b\}^\omega \subseteq \mathcal{L}(\mathcal{A})$$



## LTL to BA

[Vardi & Wolper '86]

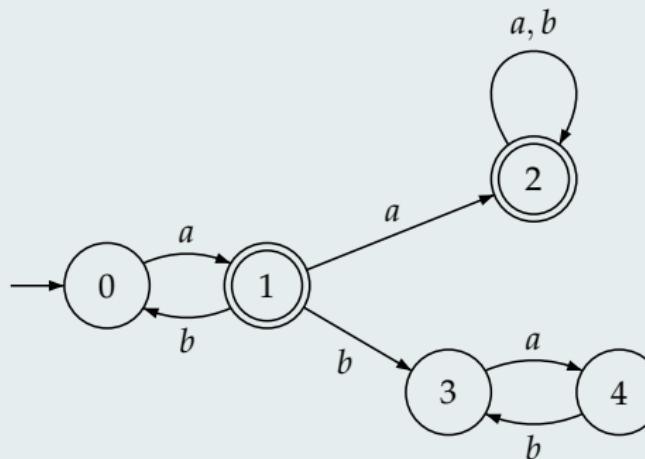
- ▶ Translation of an LTL formula  $\varphi$  into Büchi automata  $\mathcal{A}_\varphi$  with

$$\mathcal{L}(\mathcal{A}_\varphi) = \mathcal{L}(\varphi)$$

- ▶ Complexity: Exponential in the length of  $\varphi$

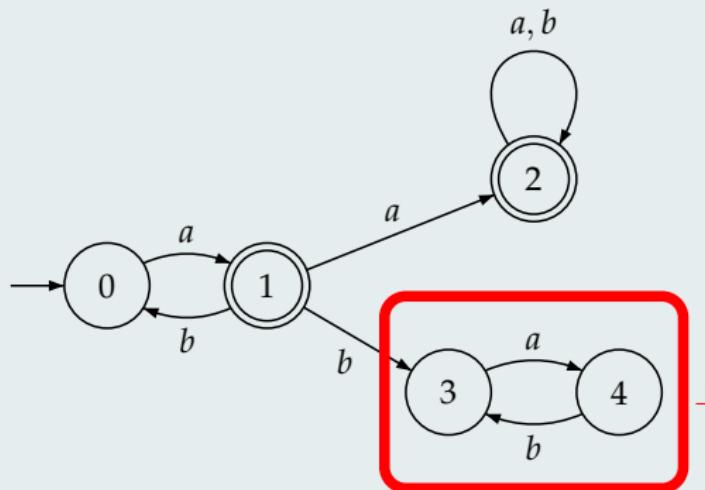
## Monitor construction – Idea I

$$[u \models \varphi] = \begin{cases} \top & \text{if } \forall \sigma \in \Sigma^\omega : u\sigma \models \varphi \\ \perp & \text{if } \forall \sigma \in \Sigma^\omega : u\sigma \not\models \varphi \\ ? & \text{else} \end{cases}$$



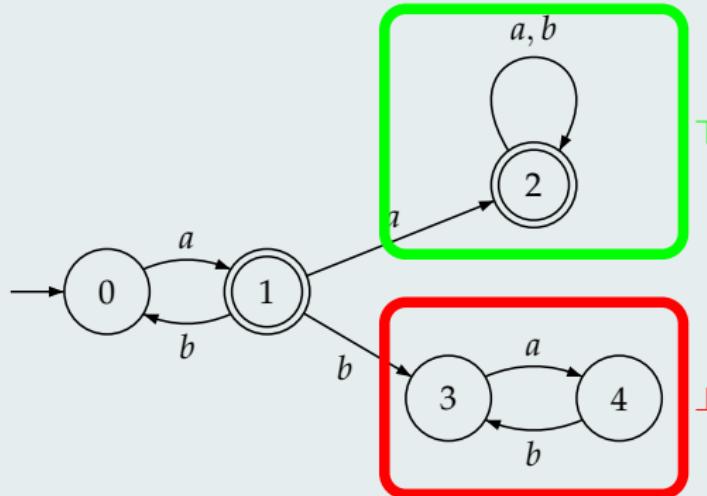
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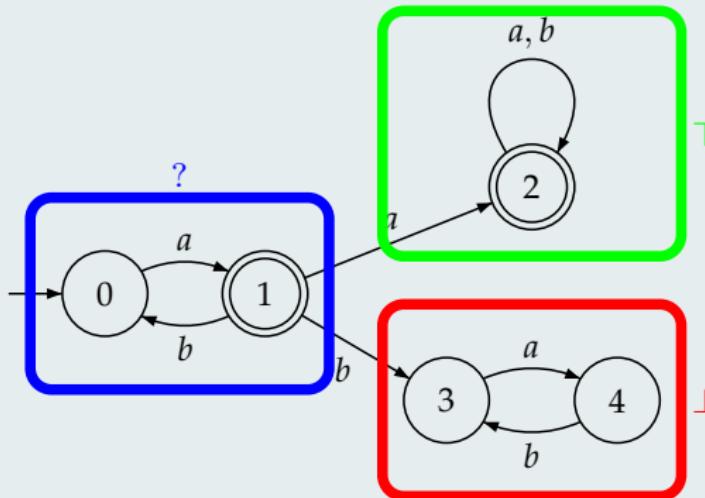
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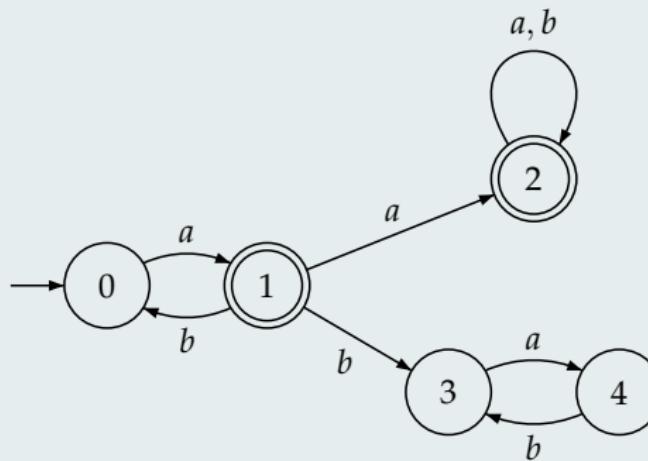


## Monitor construction – Idea I

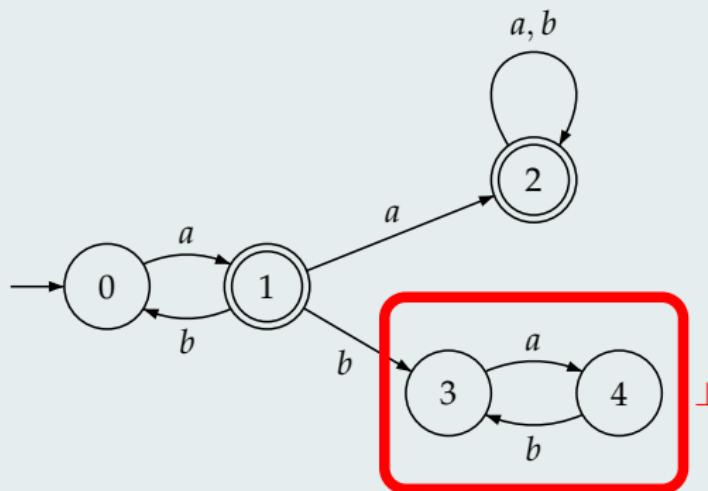
$$[u \models \varphi] = \begin{cases} \top & \text{if } \forall \sigma \in \Sigma^\omega : u\sigma \models \varphi \\ \perp & \text{if } \forall \sigma \in \Sigma^\omega : u\sigma \not\models \varphi \\ ? & \text{else} \end{cases}$$



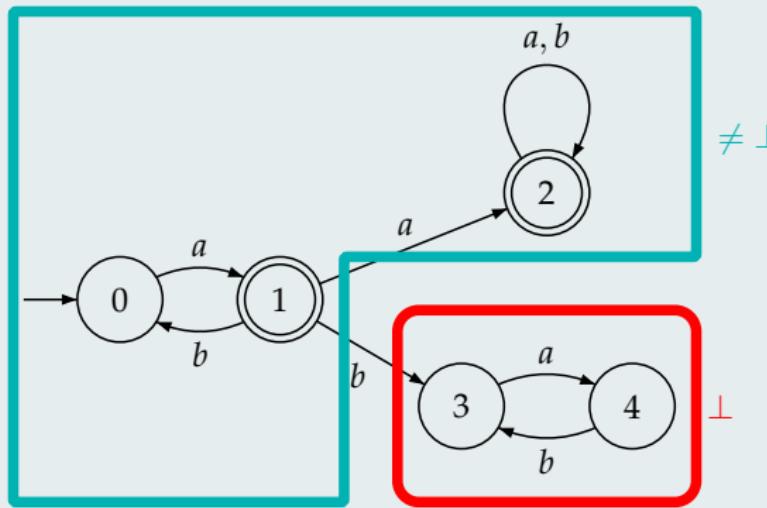
## monitor construction – Idea II



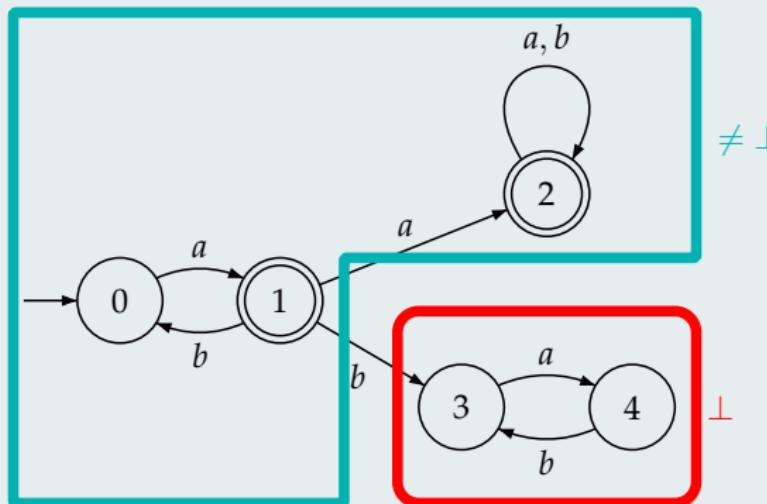
## monitor construction – Idea II



## monitor construction – Idea II



## monitor construction – Idea II



## NFA

$$\mathcal{F}_\varphi : Q_\varphi \rightarrow \{\top, \perp\}$$
 Emptiness per state

## The complete construction

### The construction

$$\varphi \longrightarrow \text{BA}^\varphi \longrightarrow \mathcal{F}^\varphi \longrightarrow \text{NFA}^\varphi$$

### Lemma

$$[u \models \varphi] = \begin{cases} \top & \\ \perp & \text{if } u \notin \mathcal{L}(\text{NFA}^\varphi) \\ ? & \end{cases}$$

## The complete construction

### The construction

$$\varphi \longrightarrow \text{BA}^\varphi \longrightarrow \mathcal{F}^\varphi \longrightarrow \text{NFA}^\varphi$$

$$\neg\varphi$$

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$$\varphi \longrightarrow \text{BA}^\varphi \longrightarrow \mathcal{F}^\varphi \longrightarrow \text{NFA}^\varphi$$

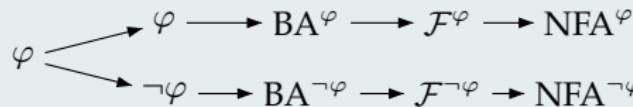
$$\neg\varphi \longrightarrow \text{BA}^{\neg\varphi} \longrightarrow \mathcal{F}^{\neg\varphi} \rightarrow \text{NFA}^{\neg\varphi}$$

### Lemma

$$[u \models \varphi] = \begin{cases} \top & \text{if } u \notin \mathcal{L}(\text{NFA}^{\neg\varphi}) \\ \perp & \text{if } u \notin \mathcal{L}(\text{NFA}^\varphi) \\ ? & \text{else} \end{cases}$$

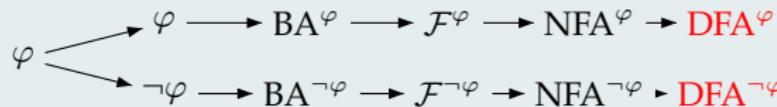
## The complete construction

### The construction



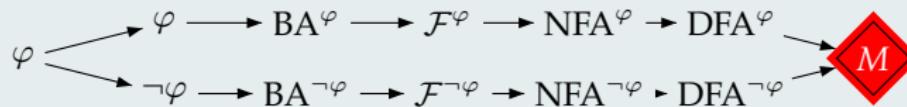
## The complete construction

### The construction



## The complete construction

### The construction





## Static initialisation order fiasco

$\neg spawnUinit$

$\neg(\neg spawnUinit)$



## Static initialisation order fiasco

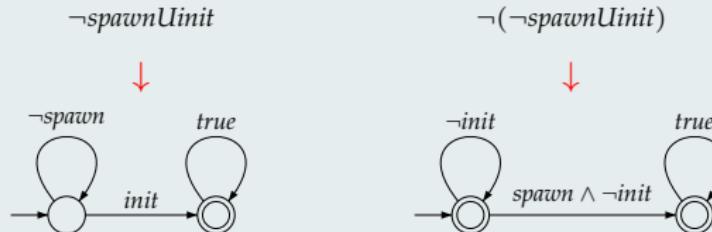
$\neg \text{spawnUinit}$



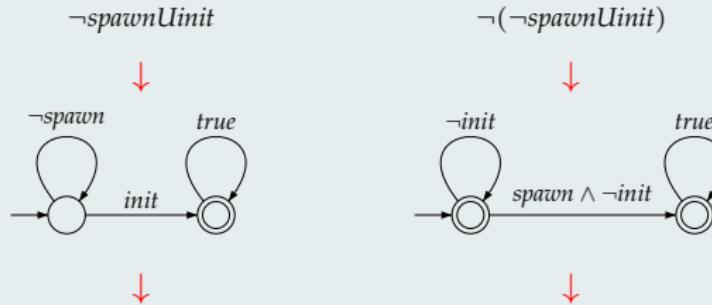
$\neg(\neg \text{spawnUinit})$



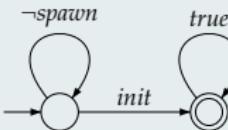
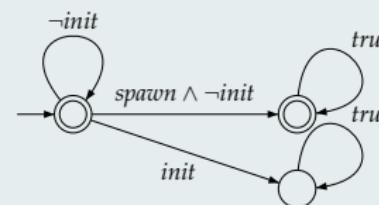
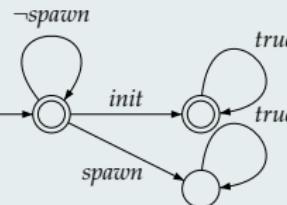
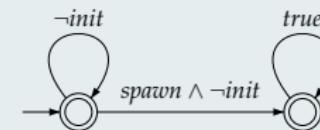
## Static initialisation order fiasco



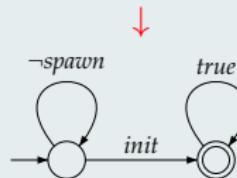
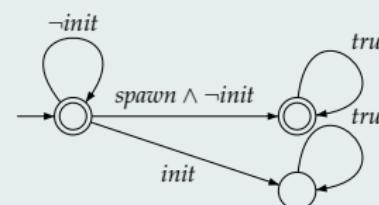
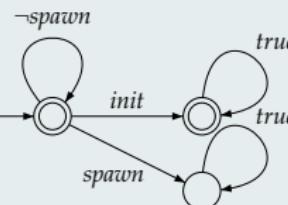
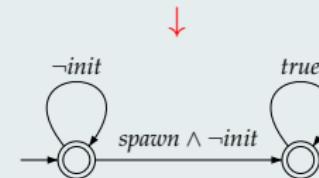
## Static initialisation order fiasco



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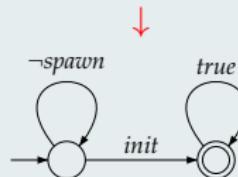
 $\neg \text{spawnUinit}$  $\neg(\neg \text{spawnUinit})$ 

## Static initialisation order fiasco

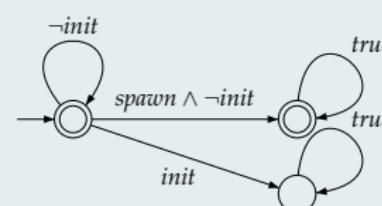
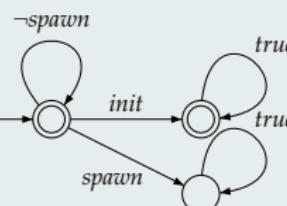
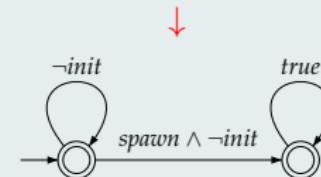
 $\neg \text{spawnUinit}$  $\neg(\neg \text{spawnUinit})$ 

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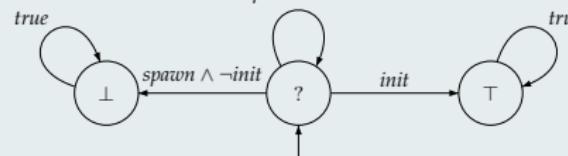
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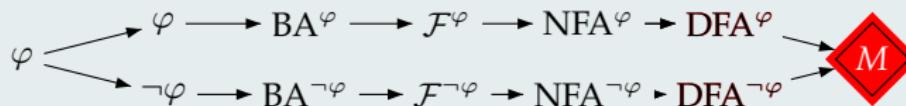


$\text{true}$



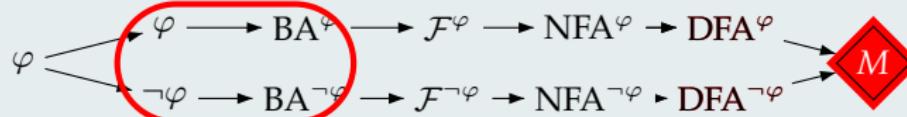
# Complexity

## The construction



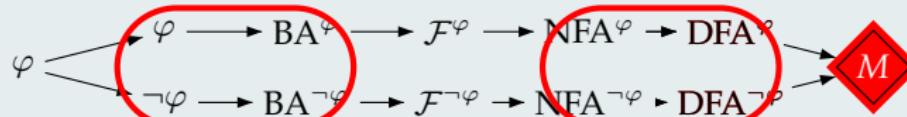
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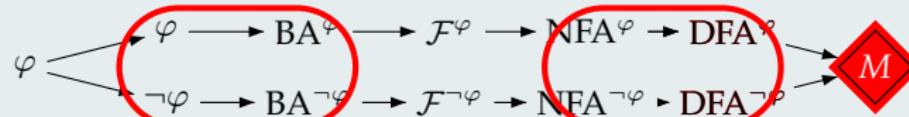
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## The construction



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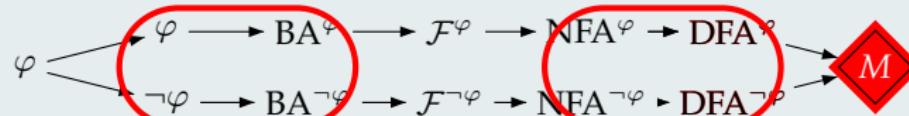


### Complexity

$$|M| \leq 2^{2^{|\varphi|}}$$

# Complexity

## The construction



## Complexity

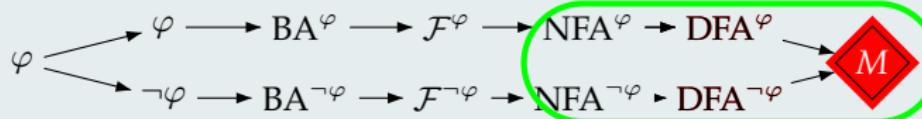
$$|M| \leq 2^{2^{|\varphi|}}$$

## Optimal result!

FSM can be minimised (Myhill-Nerode)

## On-the-fly Construction

### The construction



## Outline

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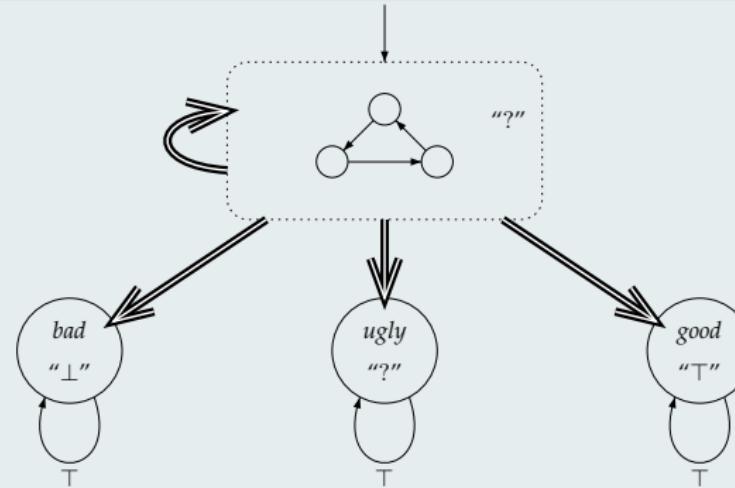
## Monitorability

When does anticipation help?



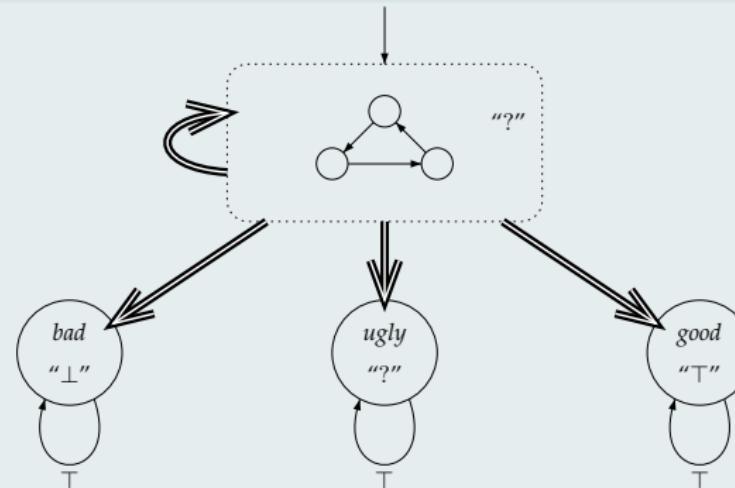
## Monitors revisited

### Structure of Monitors



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### Structure of Monitors



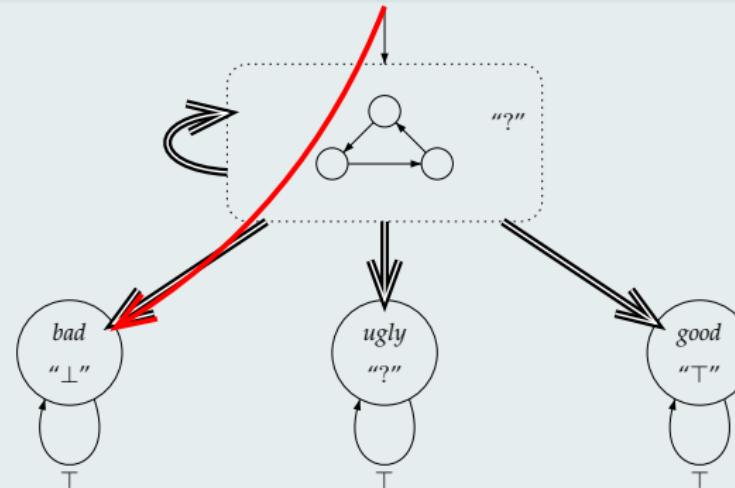
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- ▶ Bad prefixes

[Kupferman & Vardi'01]

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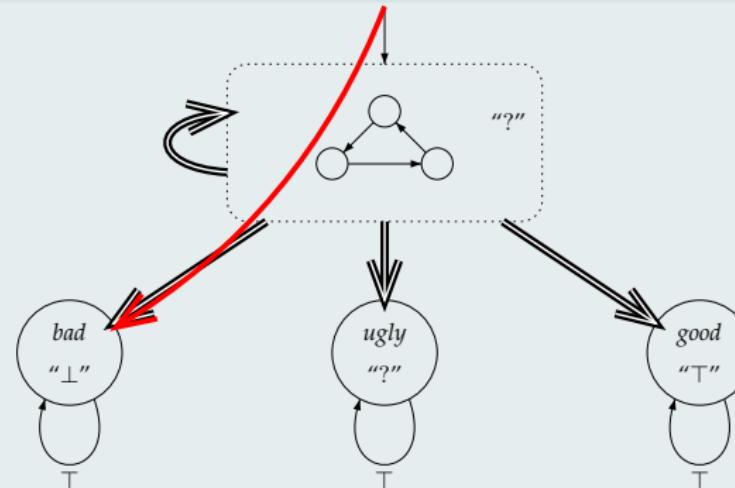
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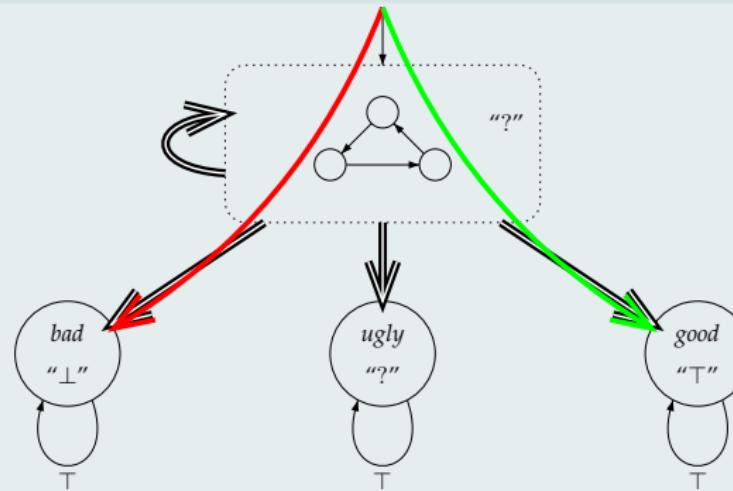
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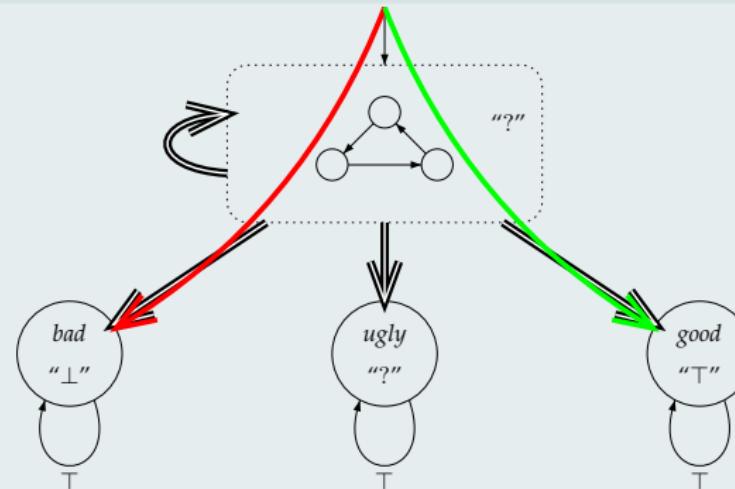


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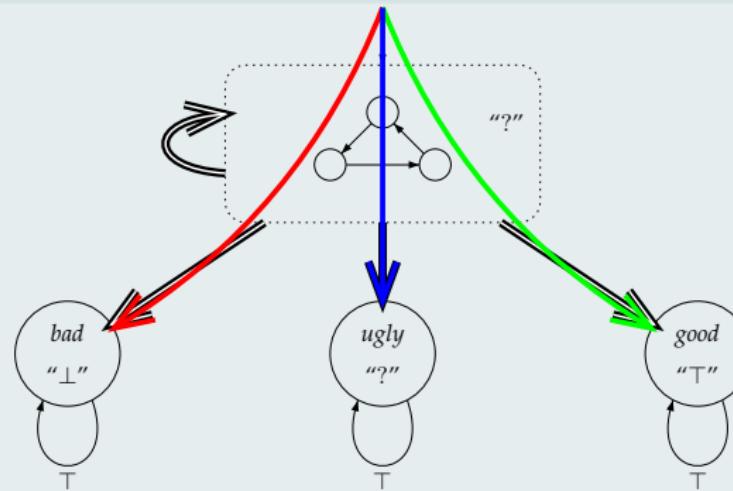
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## Monitorable

### Non-Monitorable [Pnueli & Zaks'07]

$\varphi$  is **non-monitorable after  $u$** , if  $u$  cannot be extended to a bad oder good prefix.

### Monitorable

$\varphi$  is monitorable if there is no such  $u$ .

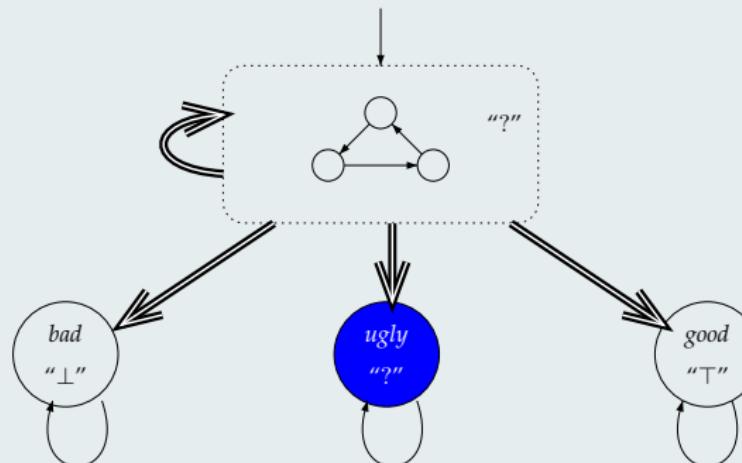
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## Monitorable Properties

### Safety Properties



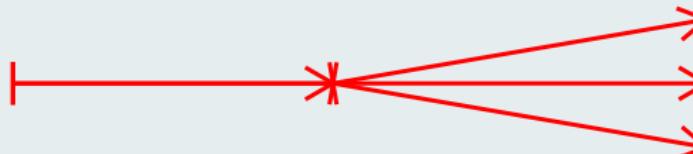
## Monitorable Properties

### Safety Properties



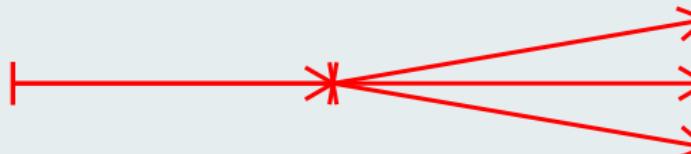
## Monitorable Properties

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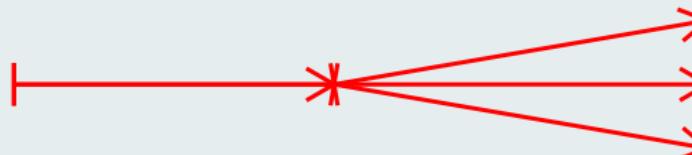


### Co-Safety Properties



## Monitorable Properties

### Safety Properties

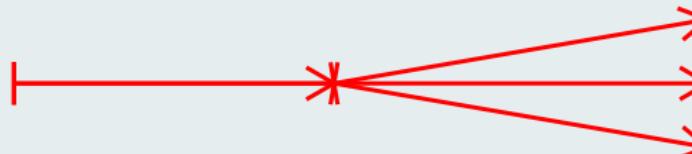


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## Monitorable Properties

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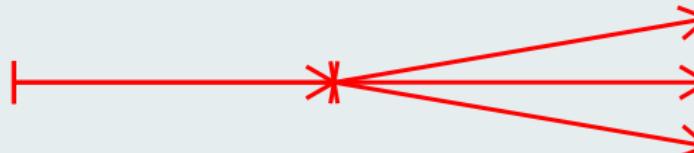


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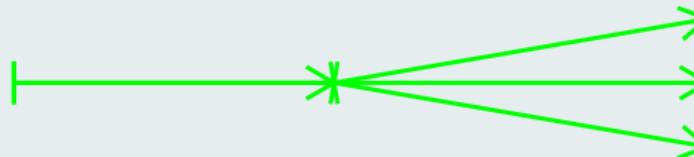


## Monitorable Properties

### Safety Properties



### Co-Safety Properties



### Note

Safety and Co-Safety Properties are monitorable

## Safety- and Co-Safety-Properties

### Theorem

The class of **monitorable properties**

- ▶ comprises safety- and co-safety properties, but
- ▶ is strictly larger than their union.

### Proof

Consider  $((p \vee q)Ur) \vee Gp$

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## RV-LTL

### Basic idea

- ▶ Use LTL<sub>3</sub> for  $\top$  and  $\perp$ , use FLTL<sub>4</sub> or FLTL to refine ?

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## Basic idea

- ▶ Use LTL<sub>3</sub> for  $\top$  and  $\perp$ , use FLTL<sub>4</sub> or FLTL to refine ?

## 4-valued semantics for LTL over finite words

$$[u \models \varphi]_{RV} = \begin{cases} \top & \text{if } [u \models \varphi]_3 = \top \\ \perp & \text{if } [u \models \varphi]_3 = \perp \\ \top^p & \text{if } [u \models \varphi]_3 = ? \text{ and } [u \models \varphi]_4 = \top^p \\ \perp^p & \text{if } [u \models \varphi]_3 = ? \text{ and } [u \models \varphi]_4 = \perp^p \end{cases}$$

Monitor: Combine corresponding Moore and Mealy machines...

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## Fusing model checking and runtime verification

### LTL with a predictive semantics



## Recall anticipatory LTL semantics

The truth value of a  $\text{LTL}_3$  formula  $\varphi$  wrt.  $u$ , denoted by  $[u \models \varphi]$ , is an element of  $\mathbb{B}_3$  defined by

$$[u \models \varphi] = \begin{cases} \top & \text{if } \forall \sigma \in \Sigma^\omega : u\sigma \models \varphi \\ \perp & \text{if } \forall \sigma \in \Sigma^\omega : u\sigma \not\models \varphi \\ ? & \text{otherwise.} \end{cases}$$

## Assumptions about environment

### Definition (Semantics of LTL with Assumptions)

Let  $\hat{\mathcal{P}}$  be an assumption on possible runs of the underlying system. Let  $u \in \Sigma^*$  denote a finite trace. The *truth value* of  $u$  and an LTL<sub>3</sub> formula  $\varphi$  wrt.  $\hat{\mathcal{P}}$ , denoted by  $[u \models_{\hat{\mathcal{P}}} \varphi]$ , is an element of  $\mathbb{B}_3 \uplus \{\downarrow\}$  and defined as follows:

$$[u \models_{\hat{\mathcal{P}}} \varphi] = \begin{cases} \downarrow & u \notin \omega \hat{\mathcal{P}}, \text{ else,} \\ \top & \text{if } \forall \sigma \in \Sigma^\omega \text{ with } u\sigma \in \hat{\mathcal{P}} : u\sigma \models \varphi \\ \perp & \text{if } \forall \sigma \in \Sigma^\omega \text{ with } u\sigma \in \hat{\mathcal{P}} : u\sigma \not\models \varphi \\ ? & \text{else} \end{cases}$$

## Assuming program is known, applied to the empty word

### Empty word $\epsilon$

$$[\epsilon \models \varphi]_{\mathcal{P}} = \top$$

iff  $\forall \sigma \in \Sigma^\omega \text{ with } \epsilon\sigma \in \mathcal{P} : \epsilon\sigma \models \varphi$

iff  $\mathcal{L}(\mathcal{P}) \models \varphi$

### RV more difficult than MC?

Then runtime verification implicitly answers model checking



## Abstraction

An **over-abstraction** or and **over-approximation** of a program  $\mathcal{P}$  is a program  $\hat{\mathcal{P}}$  such that  $\mathcal{L}(\mathcal{P}) \subseteq \mathcal{L}(\hat{\mathcal{P}}) \subseteq \Sigma^\omega$ .

## Predictive Semantics

### Definition (Predictive semantics of LTL)

Let  $\mathcal{P}$  be a program and let  $\hat{\mathcal{P}}$  be an over-approximation of  $\mathcal{P}$ . Let  $u \in \Sigma^*$  denote a finite trace. The *truth value* of  $u$  and an LTL<sub>3</sub> formula  $\varphi$  wrt.  $\hat{\mathcal{P}}$ , denoted by  $[u \models_{\hat{\mathcal{P}}} \varphi]$ , is an element of  $\mathbb{B}_3$  and defined as follows:

$$[u \models_{\hat{\mathcal{P}}} \varphi] = \begin{cases} \text{?} & u \notin \omega \hat{\mathcal{P}}, \text{ else,} \\ \top & \text{if } \forall \sigma \in \Sigma^\omega \text{ with } u\sigma \in \hat{\mathcal{P}} : u\sigma \models \varphi \\ \perp & \text{if } \forall \sigma \in \Sigma^\omega \text{ with } u\sigma \in \hat{\mathcal{P}} : u\sigma \not\models \varphi \\ \text{?} & \text{else} \end{cases}$$

We write  $LTL_{\mathcal{P}}$  whenever we consider LTL formulas with a predictive semantics.

## Properties of Predictive Semantics

Let  $\hat{\mathcal{P}}$  be an over-approximation of a program  $\mathcal{P}$  over  $\Sigma$ ,  $u \in \Sigma^*$ , and  $\varphi \in \text{LTL}$ .

- ▶ Model checking is more precise than RV with the predictive semantics:

$$\mathcal{P} \models \varphi \text{ implies } [u \models_{\hat{\mathcal{P}}} \varphi] \in \{\top, ?\}$$

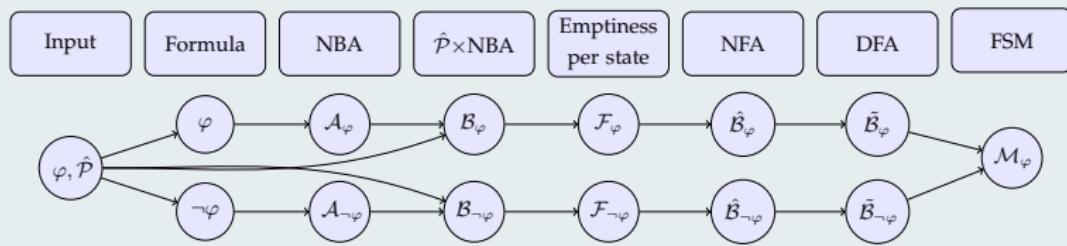
- ▶ RV has no false negatives:  $[u \models_{\hat{\mathcal{P}}} \varphi] = \perp$  implies  $\mathcal{P} \not\models \varphi$
- ▶ The predictive semantics of an LTL formula is more precise than  $\text{LTL}_3$ :

$$\begin{aligned}[u \models \varphi] = \top &\quad \text{implies} & [u \models_{\hat{\mathcal{P}}} \varphi] = \top \\ [u \models \varphi] = \perp &\quad \text{implies} & [u \models_{\hat{\mathcal{P}}} \varphi] = \perp\end{aligned}$$

The reverse directions are in general not true.

## Monitor generation

The procedure for getting  $[u \models_{\hat{\mathcal{P}}} \varphi]$  for a given  $\varphi$  and over-approximation  $\hat{\mathcal{P}}$





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jUnit<sup>RV</sup> – Testing Temporal Properties

Motivating Example

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Using jUnit<sup>RV</sup>

## Intermediate Summary

### Semantics

- ▶ completed traces
  - ▶ two valued semantics
- ▶ non-completed traces
  - ▶ Impartiality
    - ▶ at least three values
  - ▶ Anticipation
    - ▶ finite traces
    - ▶ infinite traces
    - ▶ ...
    - ▶ monitorability
- ▶ Prediction

### Monitors

- ▶ left-to-right
- ▶ time versus space trade-off
  - ▶ rewriting
  - ▶ alternating automata
  - ▶ non-deterministic automata
  - ▶ deterministic automata



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## Extensions

LTL is just half of the story





## Extensions

### LTL with data

- ▶ J-LO



## Extensions

### LTL with data

- ▶ J-LO
- ▶ MOP (parameterized LTL)



## Extensions

### LTL with data

- ▶ J-LO
- ▶ MOP (parameterized LTL)
- ▶ RV for LTL with integer constraints



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### Further “rich” approaches

- ▶ LOLA

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- ▶ Eagle (etc.)

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- ▶ Eagle (etc.)

### Further dimensions

- ▶ real-time

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### Further “rich” approaches

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### Further dimensions

- ▶ real-time
- ▶ concurrency

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- ▶ J-LO
- ▶ MOP (parameterized LTL)
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### Further “rich” approaches

- ▶ LOLA
- ▶ Eagle (etc.)

### Further dimensions

- ▶ real-time
- ▶ concurrency
- ▶ distribution



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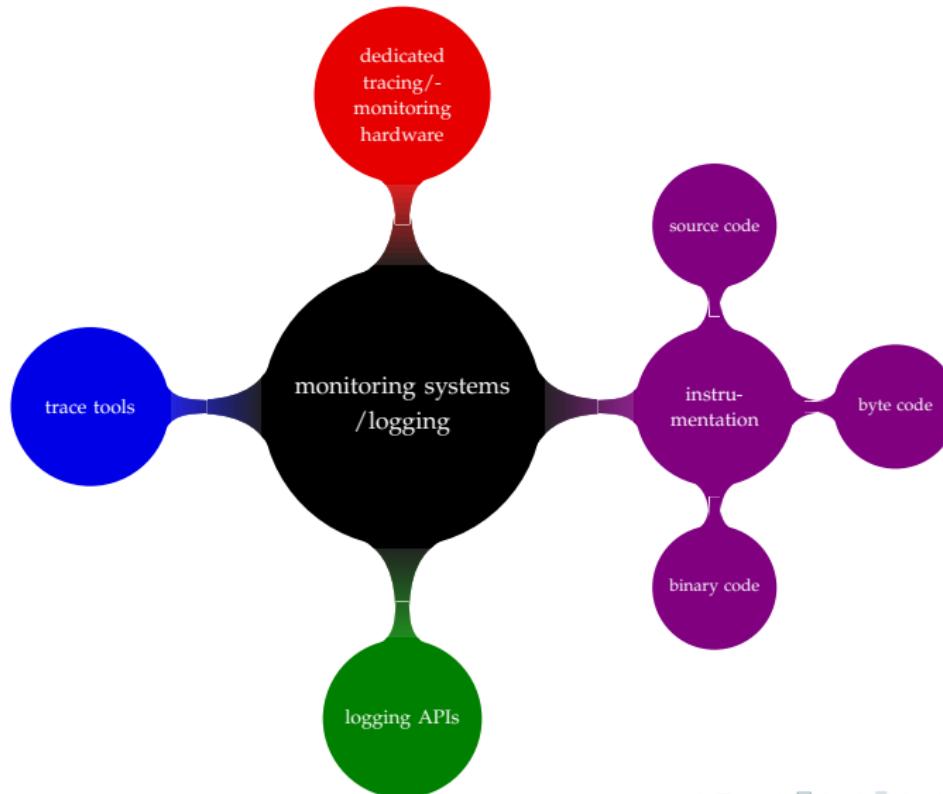
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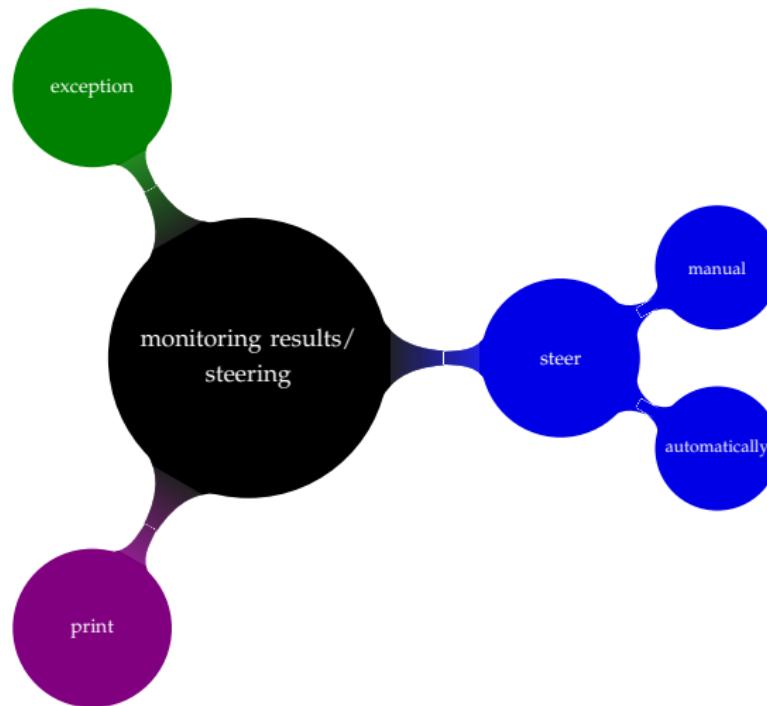
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## Monitoring Systems/Logging: Overview



# React!

## Runtime Verification

Observe—do not react

## Realising dynamic systems

- ▶ self-healing systems
- ▶ adaptive systems, self-organising systems
- ▶ ...



# React!

## Runtime Verification

Observe—do not react

## Realising dynamic systems

- ▶ self-healing systems
- ▶ adaptive systems, self-organising systems
- ▶ ...
- ▶ **use monitors for observation—then react**

## jMOP [Rosu et al.]

## Java Implementation

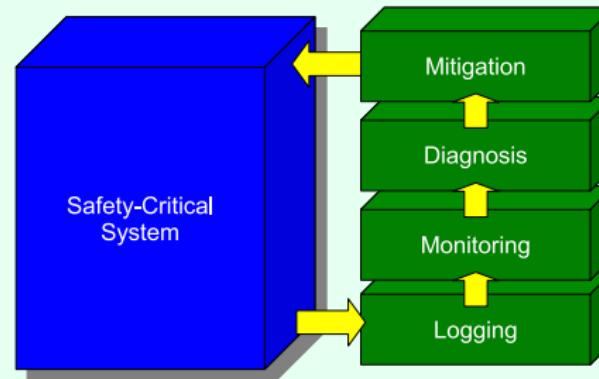
```
class Resource {  
    /*@  
     * Where → scope = class  
     * How → logic = PTLTL  
     * {  
     *     Event authenticate: end(exec(*  
     * what → authenticate()));  
     *     Event use: begin(exec(* access()));  
     *     Formula : use -> <*> authenticate  
     * }  
     * What if → {  
     *     violation Handler {  
     *         @this.authenticate();  
     *     }  
     *     */  
    void authenticate() {...}  
    void access() {...}  
    ...  
}
```



## Runtime Reflection [Bauer, L., Schallhart@ASWEC'06]

### Monitor-based Runtime Reflection

#### Software Architecture Pattern



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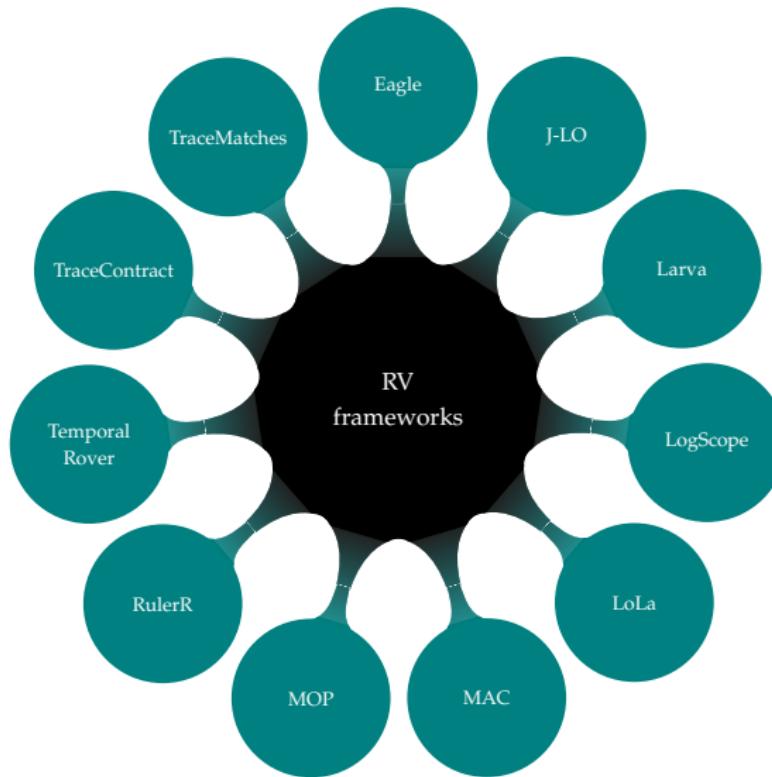
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## Example Application

- ▶ Some application for data entry
- ▶ Connects to a server
- ▶ Data can be read, modified and committed

## Example Application

- ▶ Frontend handles GUI
- ▶ Backend handles communication to the server
- ▶ Frontend and backend communicate via the following interface:

### Example

```
public interface DataService {  
    void connect(String userID) throws UnknownUserException;  
    void disconnect();  
    Data readData(String field);  
    void modifyData(String field, Data data);  
    void commit() throws CommitException;  
}
```

## A “simple” Test

- ▶ Frontend has to use backend *correctly*
- ▶ Data has to be committed before disconnecting

### Example

```
@Test
public void test1() {
    DataService service = new MyDataService("http://myserver.net");
    MyDataClient client = new MyDataClient(service);

    client.authenticate("daniel");
    client.addPatient("Mr. Smith");
    client.switchToUser("ruth");
    assertTrue(service.debug_committed()); // switching means logout
    client.getPatientFile("miller-2143-1");
    client.setPhone("miller-2143-1", "012345678");
    client.exit();
    assertTrue(service.debug_committed());
}
```

## Observations

- ▶ Test inputs are *interleaved* with assertions
  - ▶ Requires internal knowledge about the class under scrutiny
  - ▶ Requires refactoring of interfaces between components
  - ▶ Components might need additional logic to track temporal properties
  - ▶ Production code is polluted by test code
  - ▶ Program logic for temporal properties can be complicated
- ⇒ Classical unit testing is not suitable to assure temporal properties on internal interfaces

## Outline

Runtime Verification

Runtime Verification for LTL

LTL over Finite, Completed Words

LTL over Finite, Non-Completed Words: Impartiality

LTL over Non-Completed Words: Anticipation

Monitorable Properties

RV-LTL

LTL with a Predictive Semantics

LTL wrap-up

Extensions

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Steering

RV frameworks

## jUnit<sup>RV</sup> – Testing Temporal Properties

Motivating Example

jUnit<sup>RV</sup> – Idea

Using jUnit<sup>RV</sup>

## Main Ideas

- ▶ separate test as sequence of actions to do be carried out during test execution
- ▶ and monitor specification in FLTL<sub>4</sub>
  - ▶ false can be used to abort a test immediately
  - ▶ true can be used to abort monitoring
  - ▶ true<sub>p</sub>/false<sub>p</sub> determines the verdict for completed test runs



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## Events and Propositions

- ▶ Formal runs consist of discrete steps in time
- ▶ When does a program perform a step?
- ▶ Explicitly specify events triggering time steps
- ▶ Only one event occurs at a point of time
- ▶ Propositions may be evaluated in the current state

## Events and Propositions

### Example (Specifying Events)

```
String dataService = "myPackage.DataService";
private static Event modify = called(dataService, "modify");
private static Event committed = returned(dataService, "commit");
private static Event disconnect = called(dataService, "disconnect");
```

### Example (Specifying Propositions)

```
private static Proposition auth
    = new Proposition(eq(invoke($this, "getStatus"), AUTH);
```

## Temporal Assertion

- ▶ LTL is used to specify temporal properties
- ▶ Generated monitors only observe the specified events
- ▶  $G(\text{modify} \rightarrow \neg \text{disconnect} U \text{committed})$

### Example (Specifying Monitors)

```
private static Monitor commitBeforeDisconnect = new FLTL4Monitor(  
    Always(implies(  
        modify,  
        Until(not(disconnect), committed)  
    ))  
);
```

## Testcase

### Example

```
@Test
@Monitors({"commitBeforeDisconnect"})
public void test1() {
    DataService service = new MyDataService("http://myserver.net");
    MyDataClient client = new MyDataClient(service);

    client.authenticate("daniel");
    client.addPatient("Mr. Smith");
    client.switchToUser("ruth");
    client.getPatientFile("miller-2143-1");
    client.setPhone("miller-2143-1", "012345678");
    client.exit();
}
```

# The Complete Picture

```
@RunWith(RVRunner.class)
public class MyDataClientTest {

    private static final String dataServiceQname = "junitrvexamples.DataService";
    private static Event modify = called(dataServiceQname, "modifyData");
    private static Event committed = returned(dataServiceQname, "commit");
    private static Event disconnect = invoke(dataServiceQname, "disconnect");

    // create a monitor for LTL4 property G(modify -> !close U commit)
    private static Monitor commitBeforeClose = new FLTL4Monitor(
        Always(
            implies(
                modify,
                until(not(disconnect), committed))));

    @Test
    @Monitors({"commitBeforeClose", "authWhenModify"})
    public void test1() {
        ...
    }
}
```



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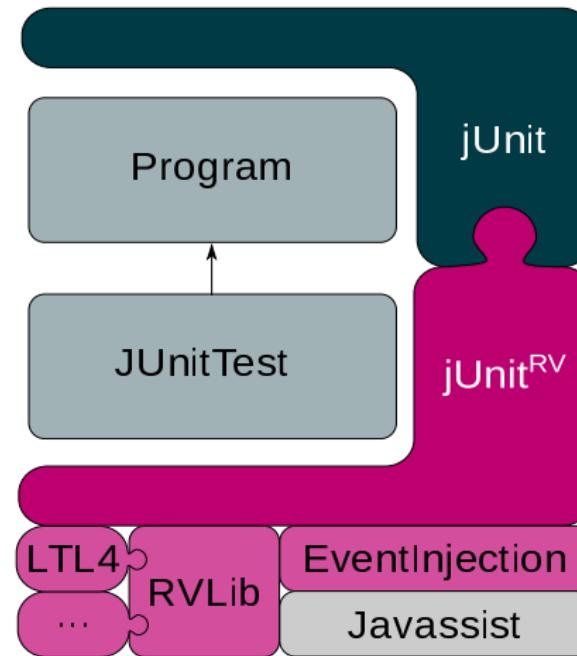
## jUnit<sup>RV</sup> – Testing Temporal Properties

Motivating Example

jUnit<sup>RV</sup> – Idea

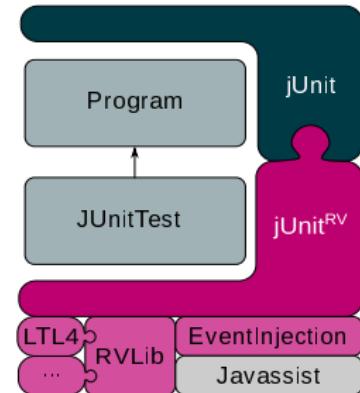
Using jUnit<sup>RV</sup>

## Architecture



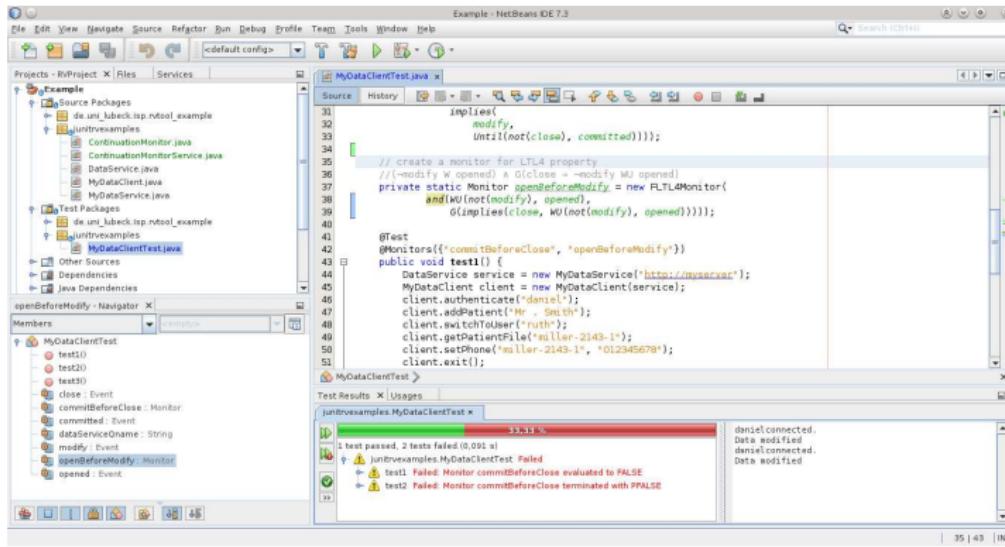
## Runners and Classloaders

- ▶ jUnit uses test runners to execute tests
- ▶ jUnit provides a default implementation
- ▶ jUnit<sup>RV</sup> provides RVRunner extending the default implementation
- ▶ jUnit<sup>RV</sup> provides a custom Classloader
- ▶ Class loading by program under scrutiny is intercepted
- ▶ Bytecode is manipulated to intercept events



## Features

- ▶ jUnit<sup>RV</sup> is provided as single class jar file that has to be made available on the Java class path
- ▶ It can easily integrated into build systems and IDEs
- ▶ It may be used to test third party components where no byte code is available
- ▶ It may be extended with custom specification formalisms
- ▶ Test failures are reported as soon as a monitor fails
- ▶ Stack traces show the exact location of the failure in the program under scrutiny

jUnit<sup>RV</sup> Running in Netbeans



## jUnitRV – Summary

- ▶ Unit testing and runtime verification are combined
- ▶ jUnit is extended by temporal assertions
- ▶ Testing temporal properties is less cumbersome
- ▶ jUnit<sup>RV</sup> integrates easily in existing projects and environments



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## Conclusion

### Summary

- ▶ RV needs similar temporal logics as model checking, but adaptions for
  - ▶ finite runs
  - ▶ impartiality
  - ▶ anticipation
  - ▶ prediction
- ▶ Application jUnit<sup>RV</sup>

That's it!

Thanks! - Questions?

