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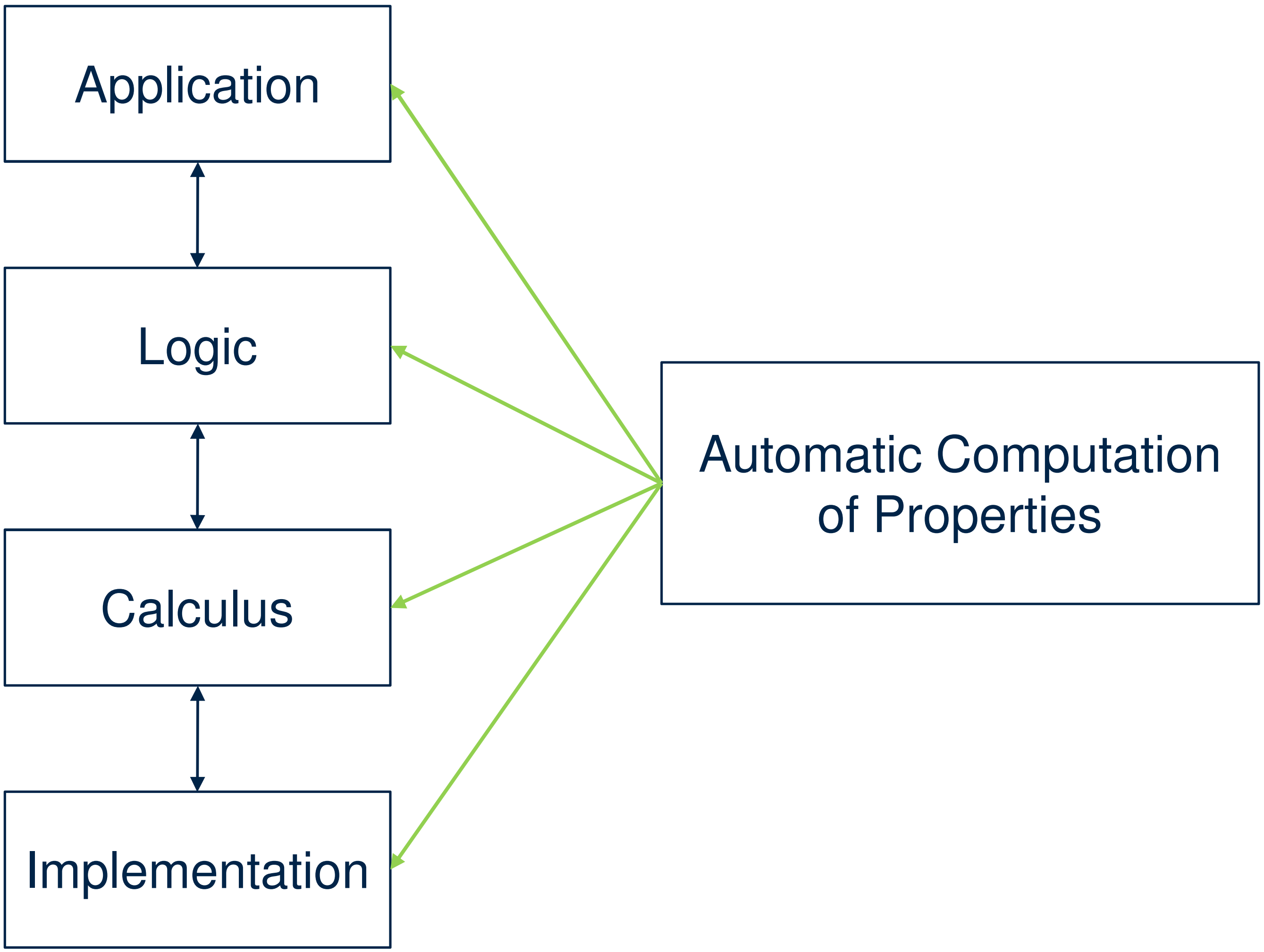
informatik

Variability Management

Prof. Dr. Christoph Weidenbach

Automation of Logic



Examples by PhD Thesis

- Dr. Matthias Horbach: second-order logic decidability
- Dr. Carsten Ihlemann: local theory extensions
- Tinxiang Lu: verifying correctness of PASTRY
- Arnaud Fietzke: combining first-order and prob. reasoning
- Patrick Wischnewski: reasoning in large ontologies
- ?: variability management (PROSTEP, Siemens)

Reasoning in Large Ontologies

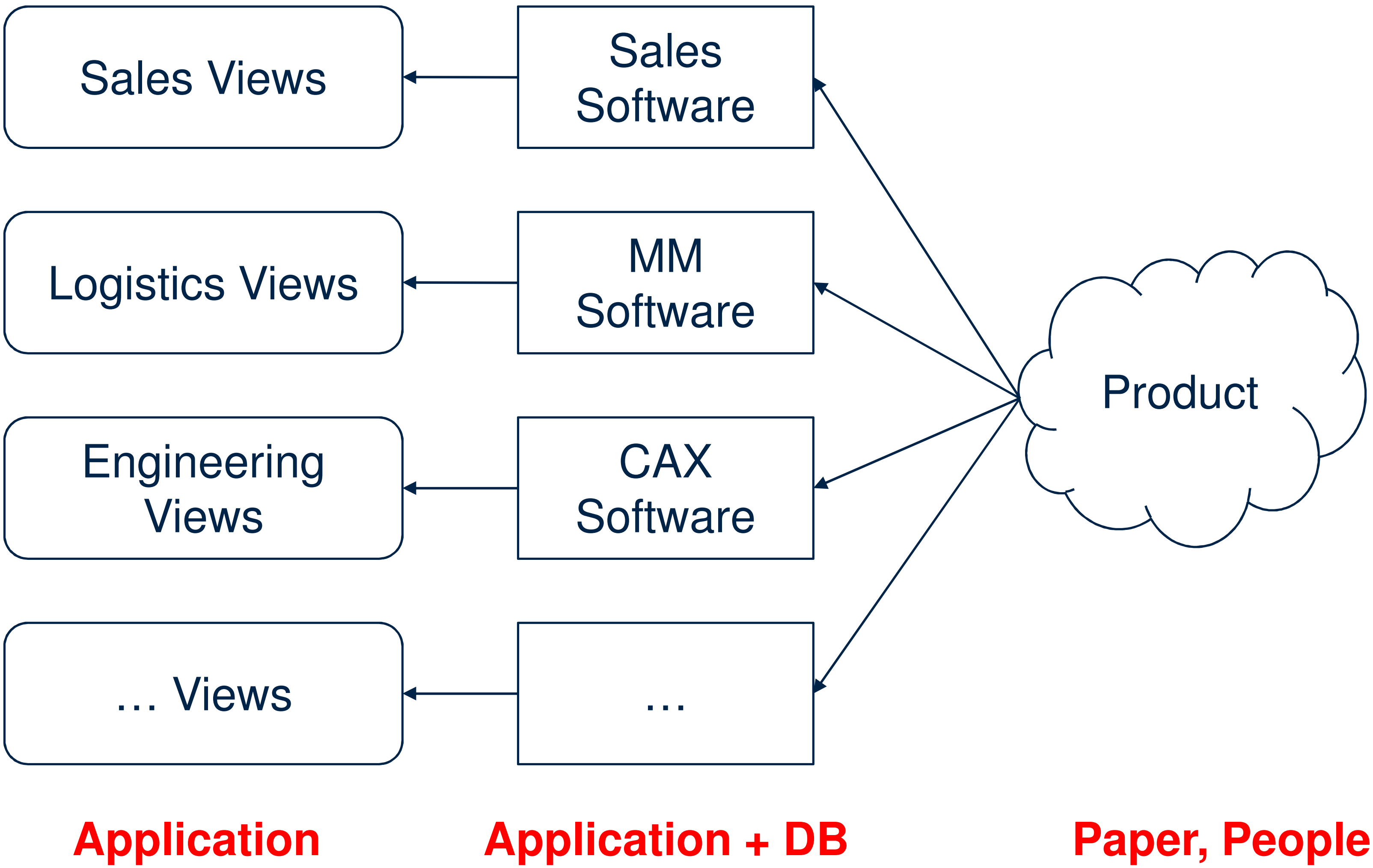
develop “semantic” GOOGLE

Configuration Today

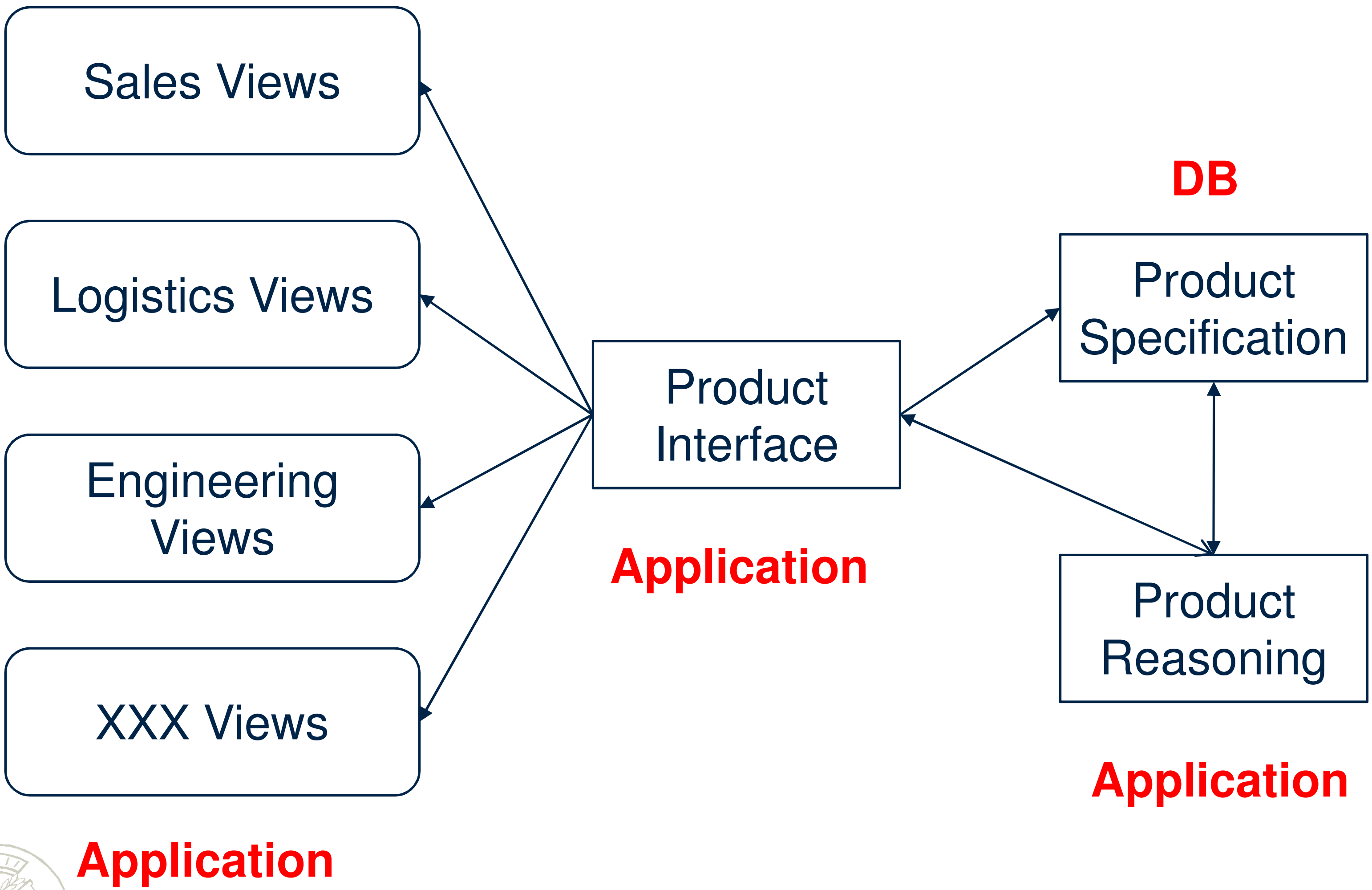
The car industry:

Opel Corsa

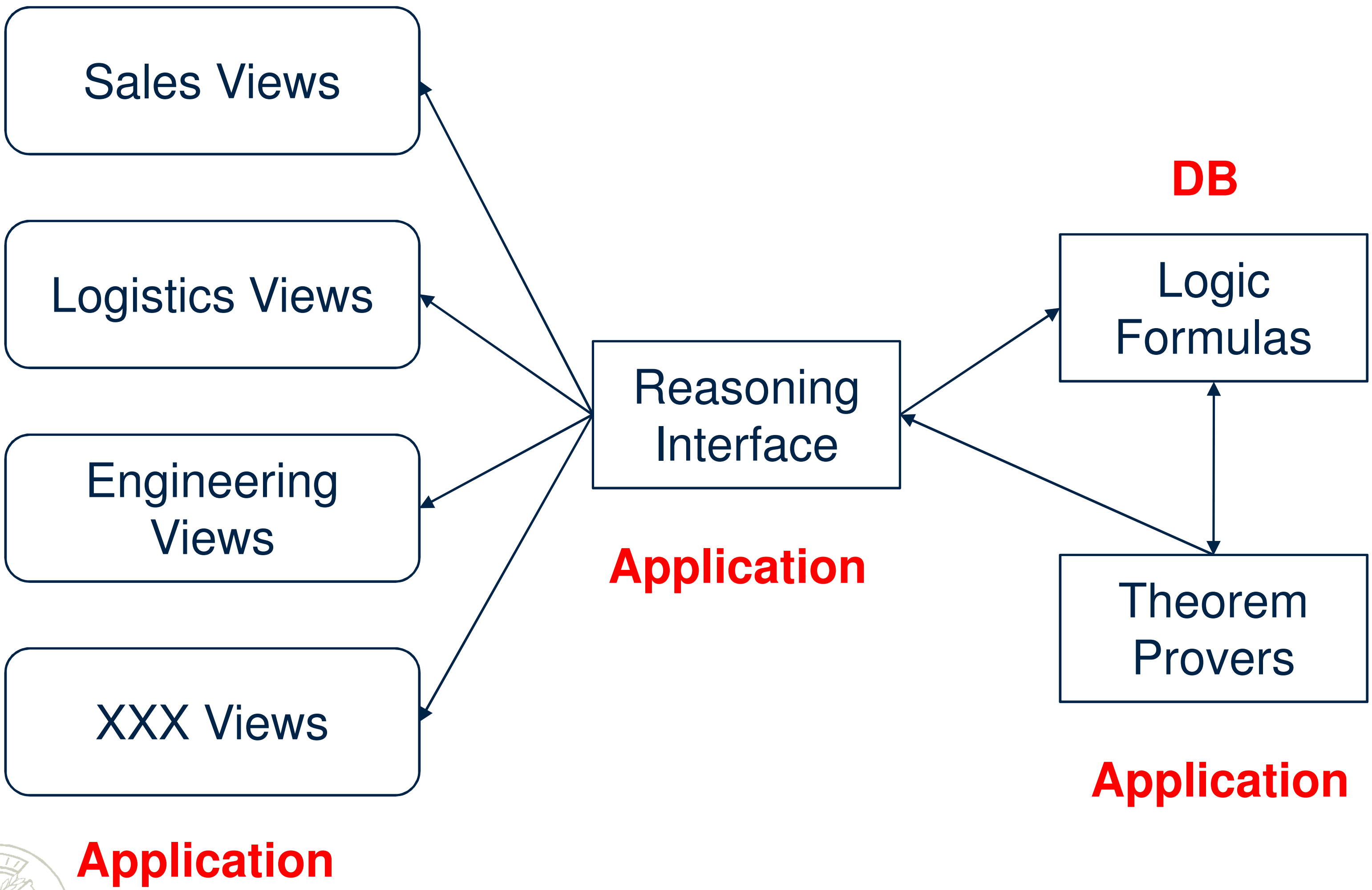
Today's Architecture



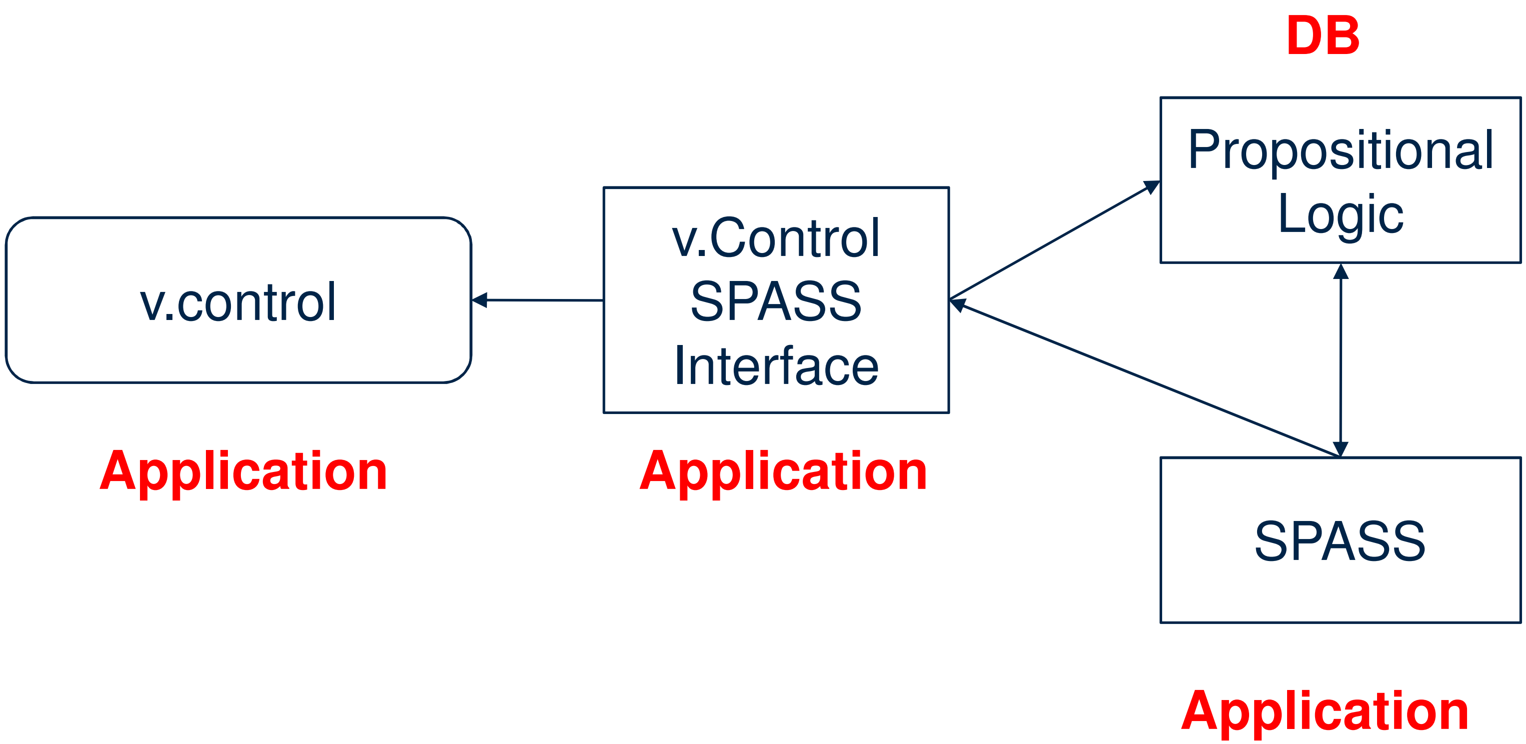
Future's Architecture



Scientific View



Concrete Example



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Opel Corsa

PROSTEP IMP

in cooperation with

Prof. Dr. Georg Rock, Uni App Sc Trier, PROSTEP IMP

Daniel Doenigus, PROSTEP IMP

Propositional Logic

- Language: propositional variables can be true (1) or false (0)
- Connectives: $\Rightarrow$ implication, $\neg$ negation, $\vee$ disjunction, $\wedge$ conjunction
- Clause: disjunction of variables or their negations (literal)
- Validity: a formula is valid iff it is true for all possible assignments
- Assignment: setting all propositional variables 1 or 0, can also be expressed by showing the true literals
- we write $M \models C$ if the clause C is true by assignment M
- SAT: propositional satisfiability, find an assignment such that for a set of clauses all clauses are valid in the assignment

Unit Propagation

UProp(N,M)
  while (there is a clause $C' \lor L \in N$ such that
      $M \models \neg C'$ and $L \notin M$ and $\neg L \notin M$)
    $M := M \cup \{L\}$;
  return M;

UProp($\{\neg A \lor \neg B \lor E,\quad \neg A \lor B,\quad \neg E,\quad D,\quad A\}$,$\emptyset$)

$\rightarrow M = \emptyset$
$\rightarrow M = \{\neg E\}$
$\rightarrow M = \{\neg E, D\}$
$\rightarrow M = \{\neg E, D, A\}$
$\rightarrow M = \{\neg E, D, A, B\}$

DPLL Procedure

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DPLL(N,M)
  if for all $C \in N$ we have $M \models C$ return true;
  if there is some $C \in N$ with $M \models \neg C$ return false;
  select a variable P occuring in N but not in M;
  if (DPLL(N, UProp(N, $M \cup \{P\}$))) then
    return true;
  else
    return DPLL(N, UProp(N, $M \cup \{\neg P\}$));

$\neg A \vee \neg B \vee E$
$\neg A \vee B$
$\neg E$
$A \vee D$

DPLL(N, $\emptyset$)

DPLL(N, UProp(N,$\{A\}$)) DPLL(N, UProp(N,$\{\neg A\}$))

DPLL(N, $\{A, B, \neg E\}$) DPLL(N, $\{\neg A, D, \neg E\}$)

DPLL is sound and complete and terminating for SAT.

Propositional Logic Formulas

$$\text{Corsa} \Rightarrow \text{Wheels} \wedge \text{Engines}$$

$$\begin{aligned}
&\text{4-Holes} \Rightarrow \text{Wheels} \\
&\text{5-Holes} \Rightarrow \text{Wheels} \\
&\text{4-Holes} \Rightarrow \neg\text{5-Holes} \\
&\text{5-Holes} \Rightarrow \neg\text{4-Holes}
\end{aligned}$$

$$\begin{aligned}
&\text{Diesel} \Rightarrow \text{Engines} \\
&\text{Gasoline} \Rightarrow \text{Engines} \\
&\text{Diesel} \Rightarrow \neg\text{Gasoline} \\
&\text{Gasoline} \Rightarrow \neg\text{Diesel}
\end{aligned}$$

$$\text{Diesel} \Rightarrow \neg\text{4-Holes}$$

Reasoning: $\text{Corsa} \rightarrow \text{Wheels}, \text{Engines}$

$\text{4-Holes} \rightarrow \neg\text{5-Holes}, \neg\text{Diesel}, \text{Gasoline}$

$\text{Gasoline} \rightarrow \neg\text{Diesel}$

Challenge: Scalability

- worst case SAT searches 2^n nodes
- before 2009: approx. 1500 nodes
- in 2009: v.control + SPASS approx. 3000 nodes
- in x years: for a reasonable product approx. 60000 nodes

- SAT Seminar:

  http://www.mpi-inf.mpg.de/departments/rg1/teaching/sat-ws10/

- contact us on student assistant jobs, bachelor-master-PhD thesis

Thank you for your attention